

# GRAVITATIONAL LENSING

## LECTURE 12

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*Docente: Massimo Meneghetti*  
*AA 2015-2016*

# TODAY'S LECTURE

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- Lensing by multiple point masses
  - Binary lenses
    - Planetary microlensing

# PLANETARY MICROLENSING

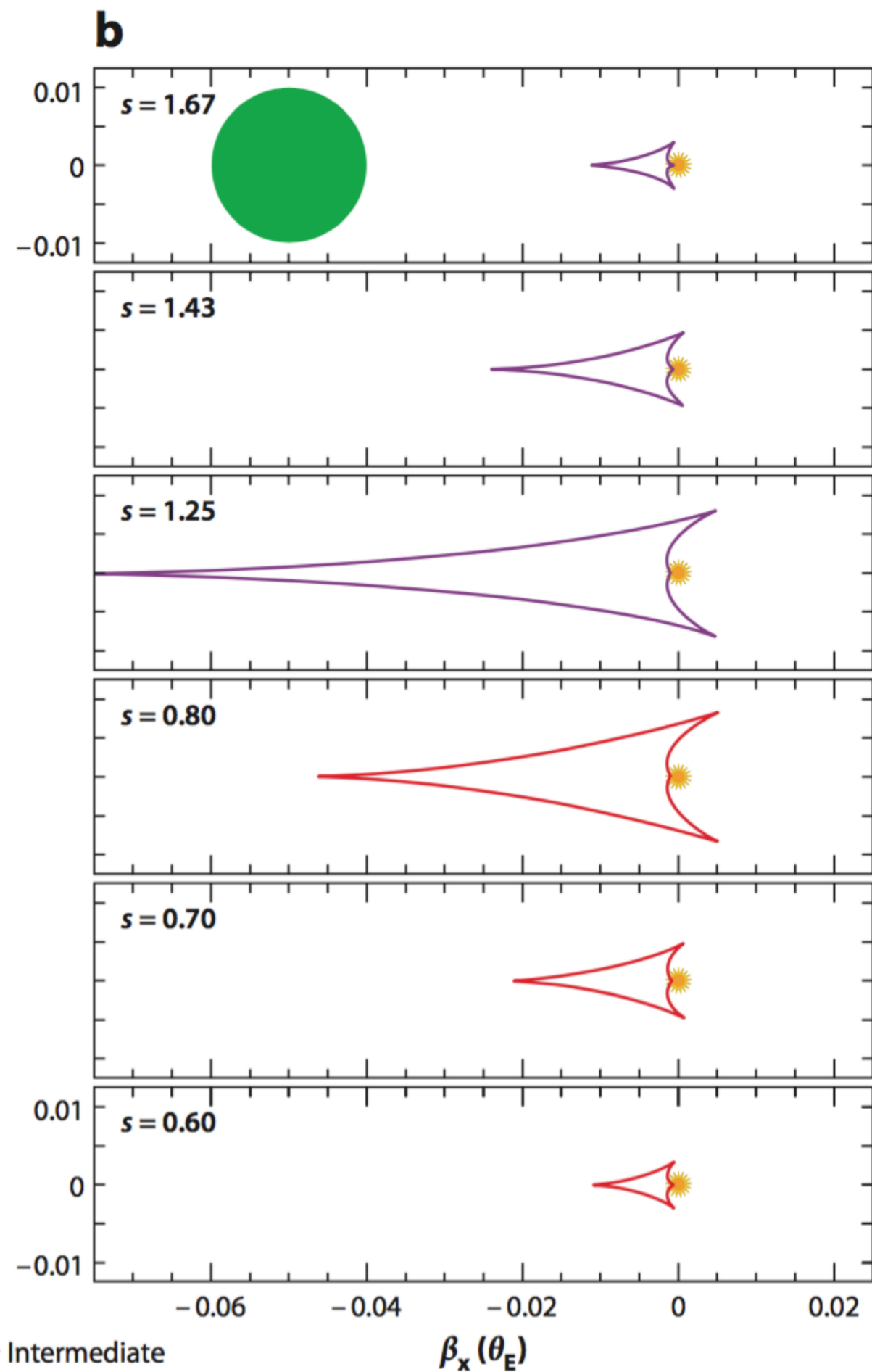
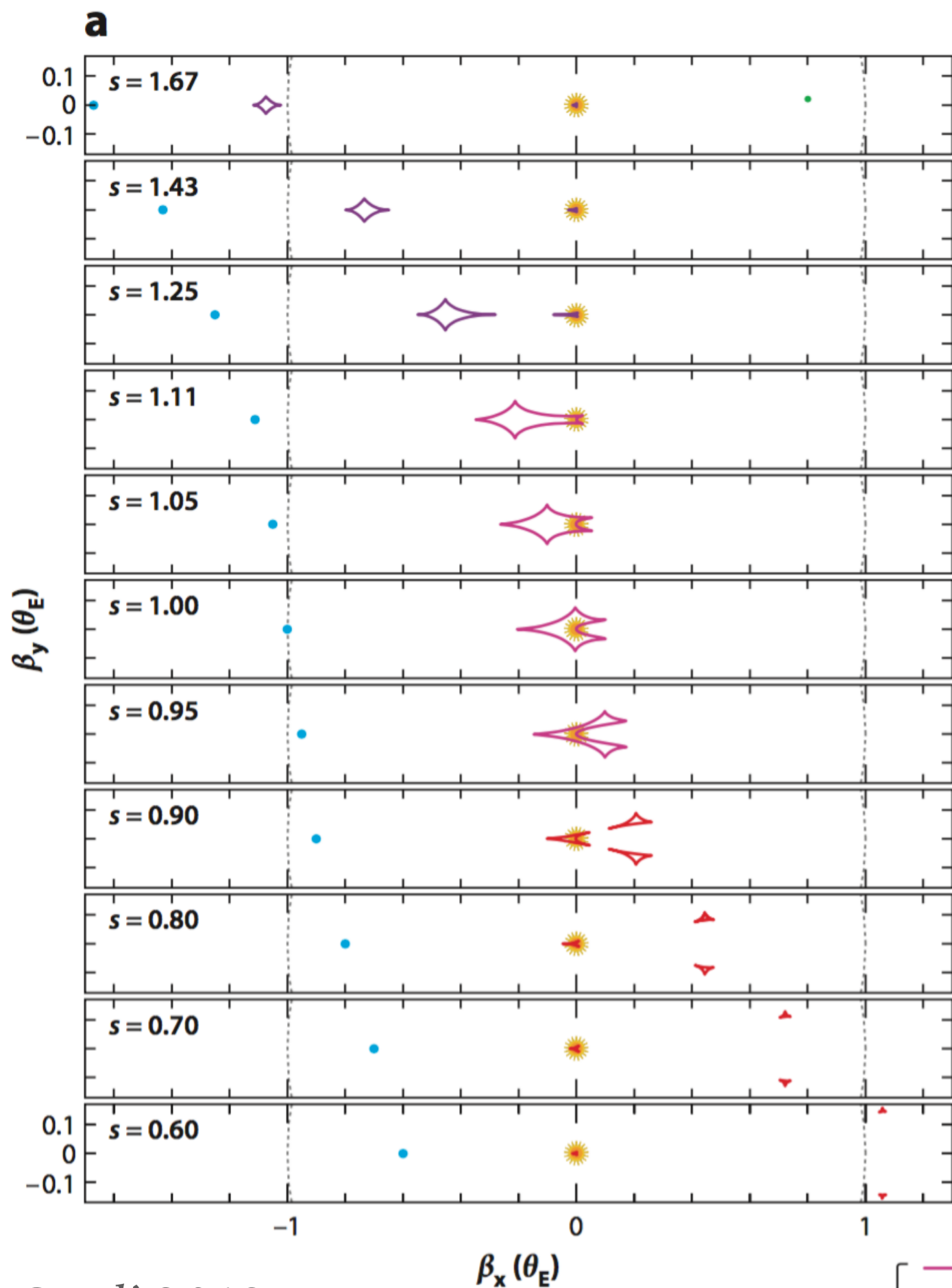
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- Let us consider the system consisting of an host star and a planet orbiting around it.
- This is an example of **binary** lens
- The host star is of course much heavier than the planet!
  - example: for a Jupiter-like planet  $q=0.001$
  - example: for a Earth-like planet  $q=0.000003$

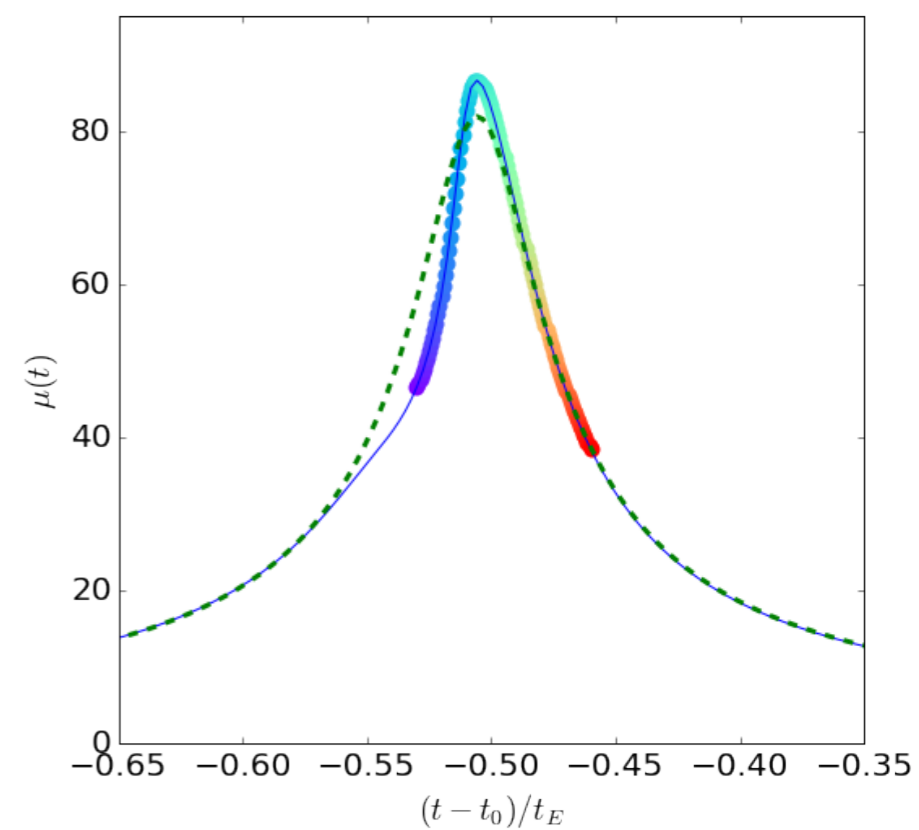
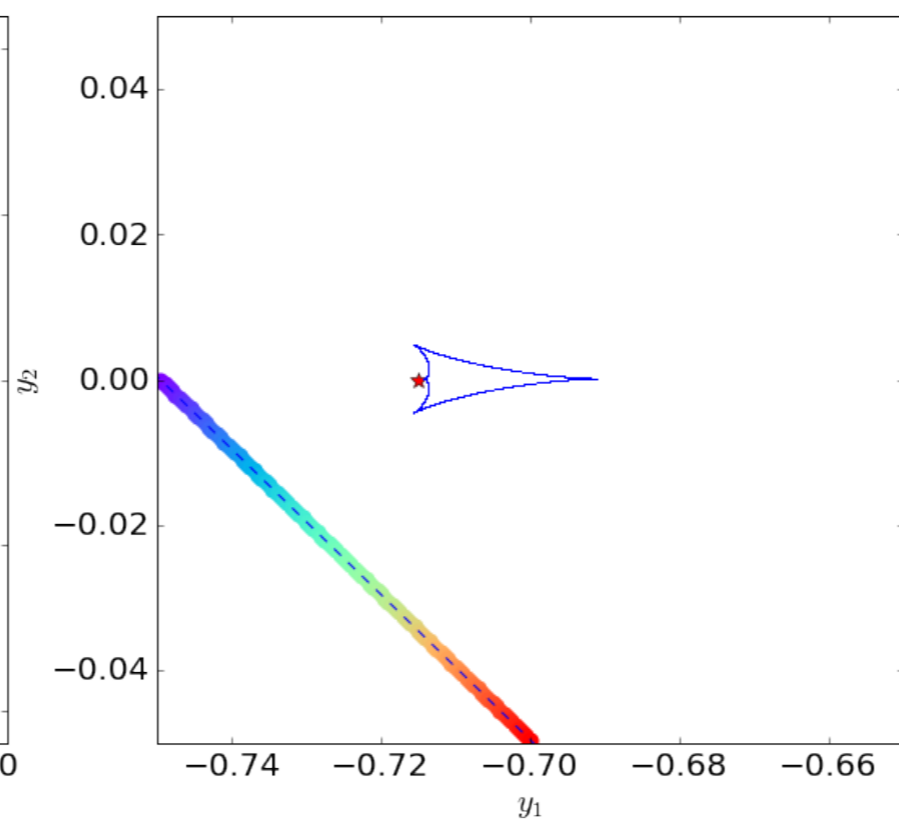
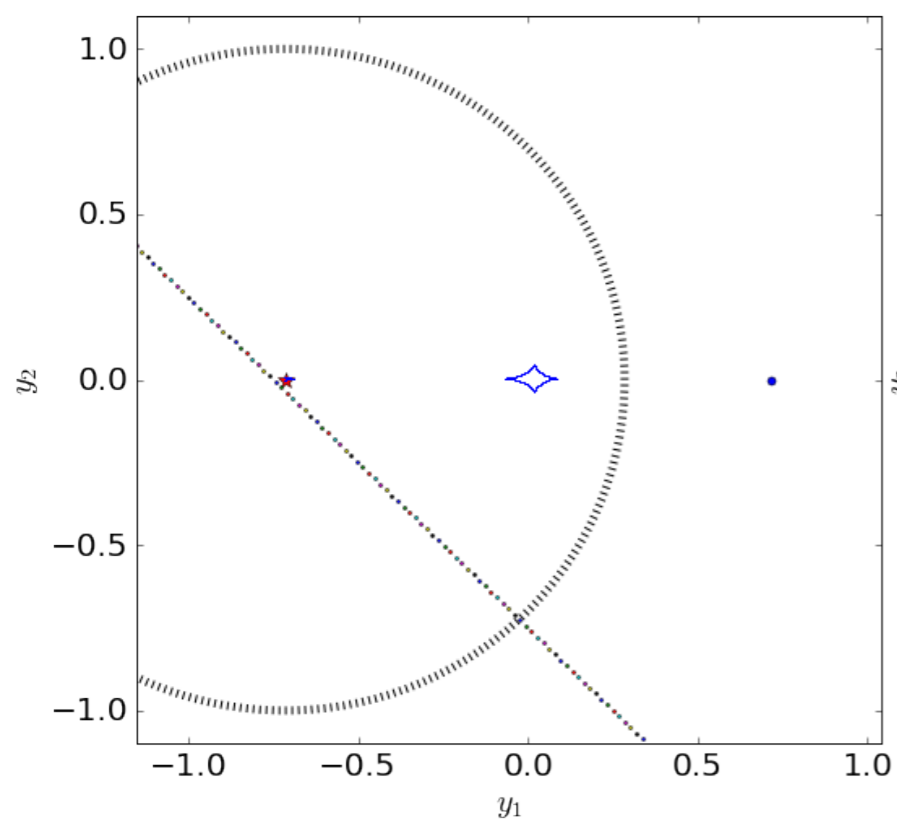
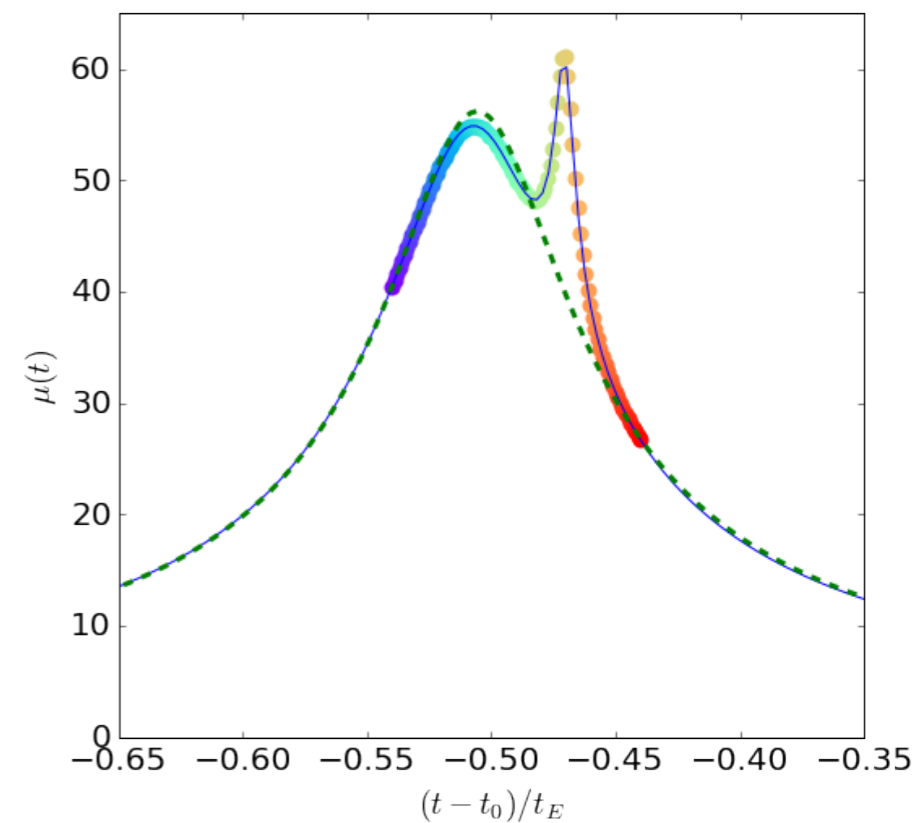
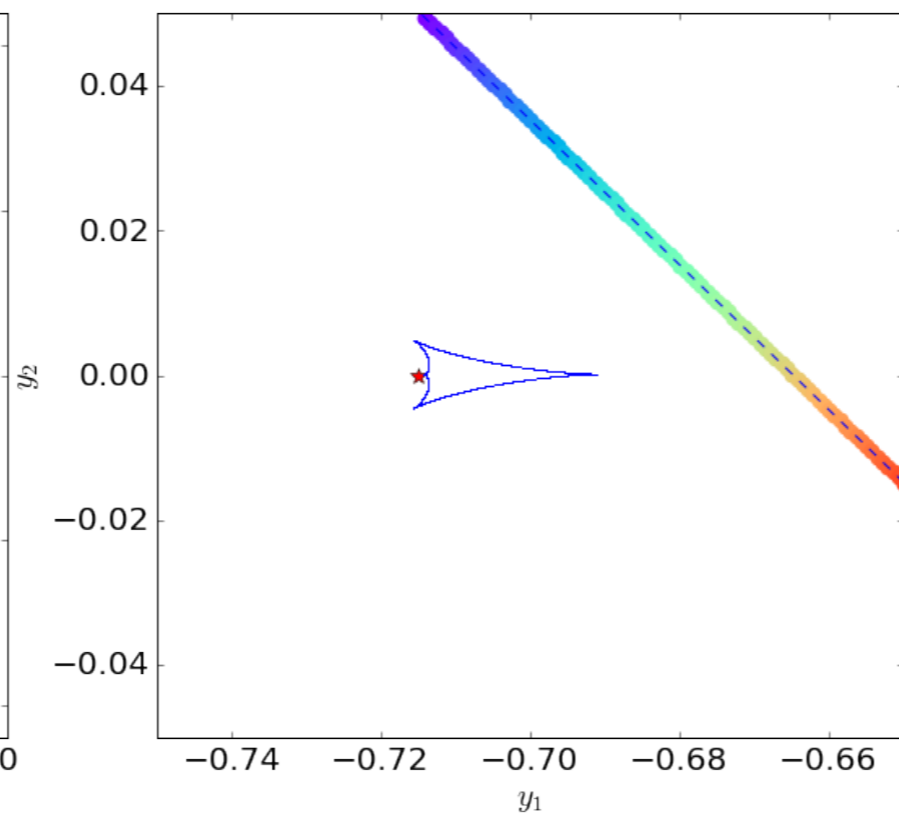
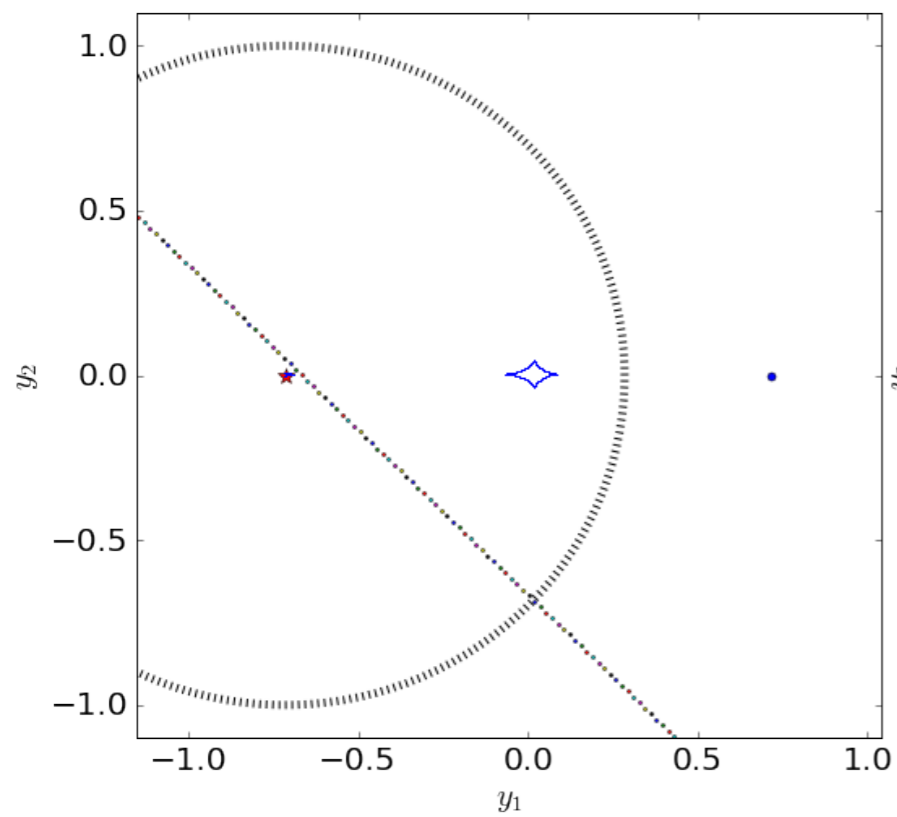
# WHAT KIND OF SIGNAL?

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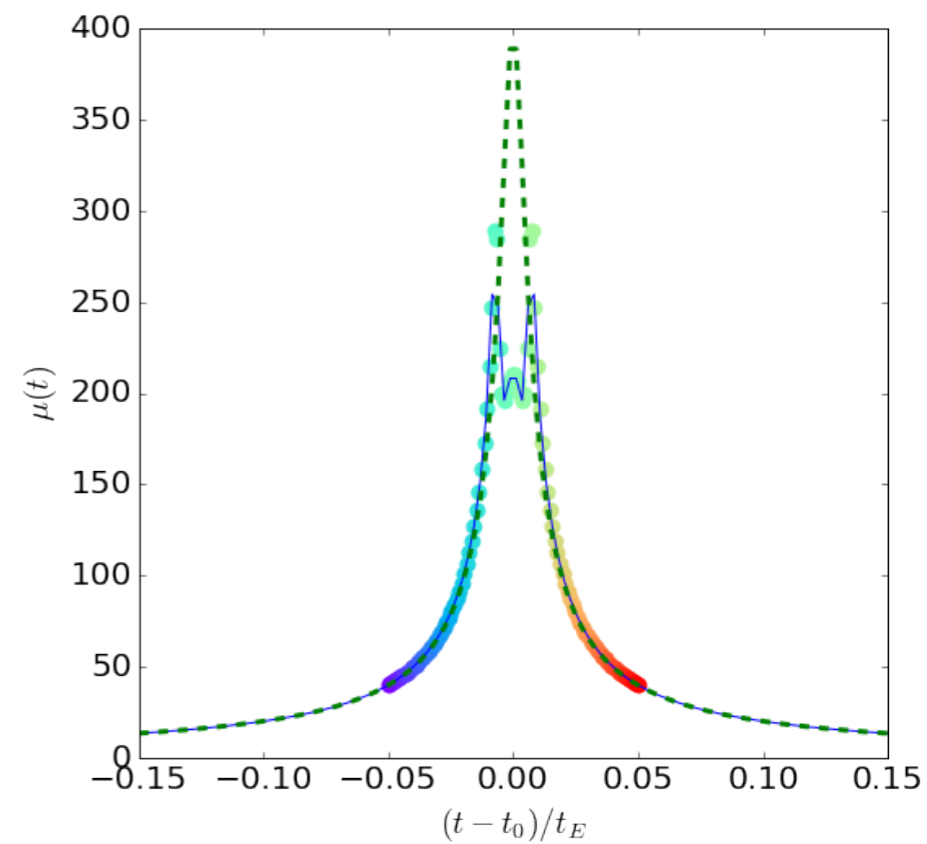
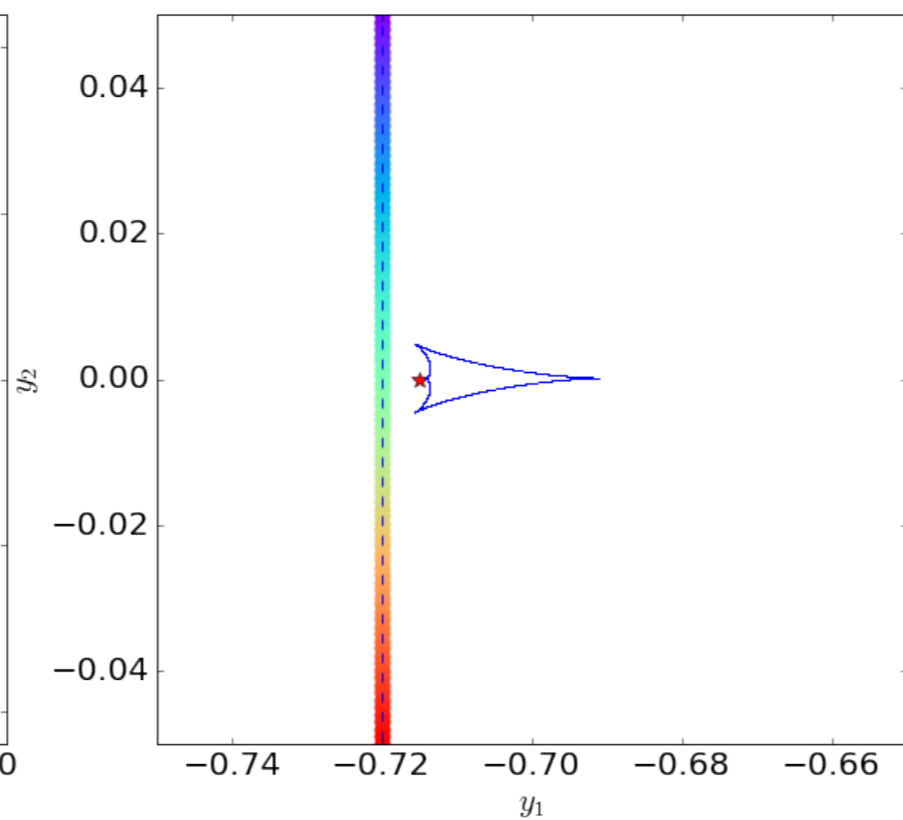
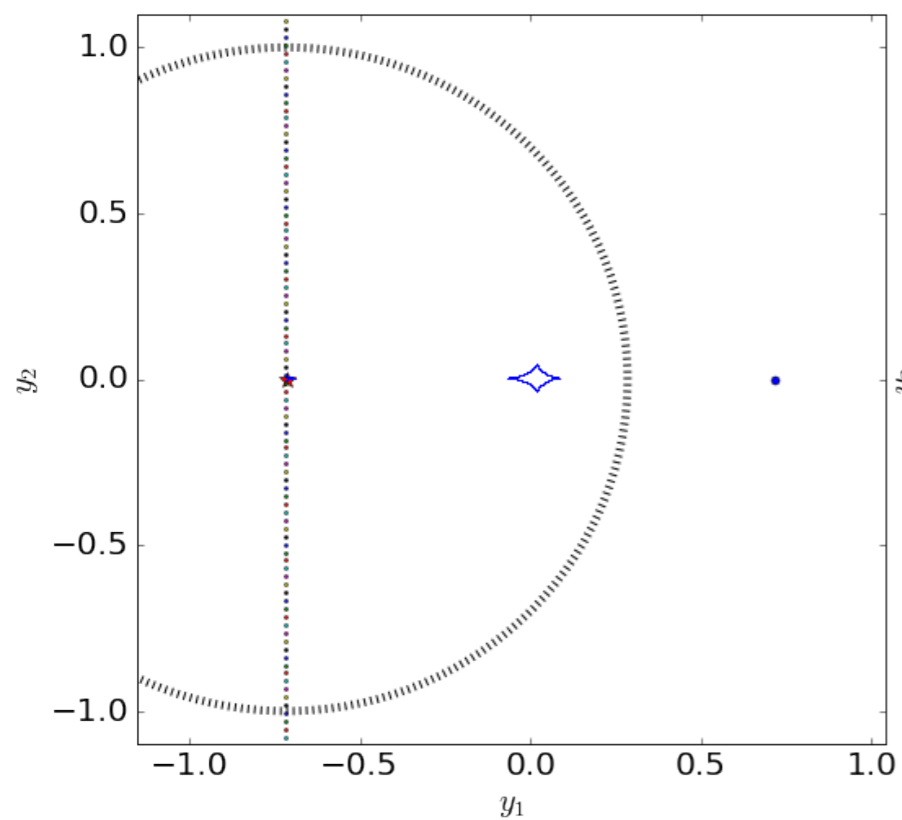
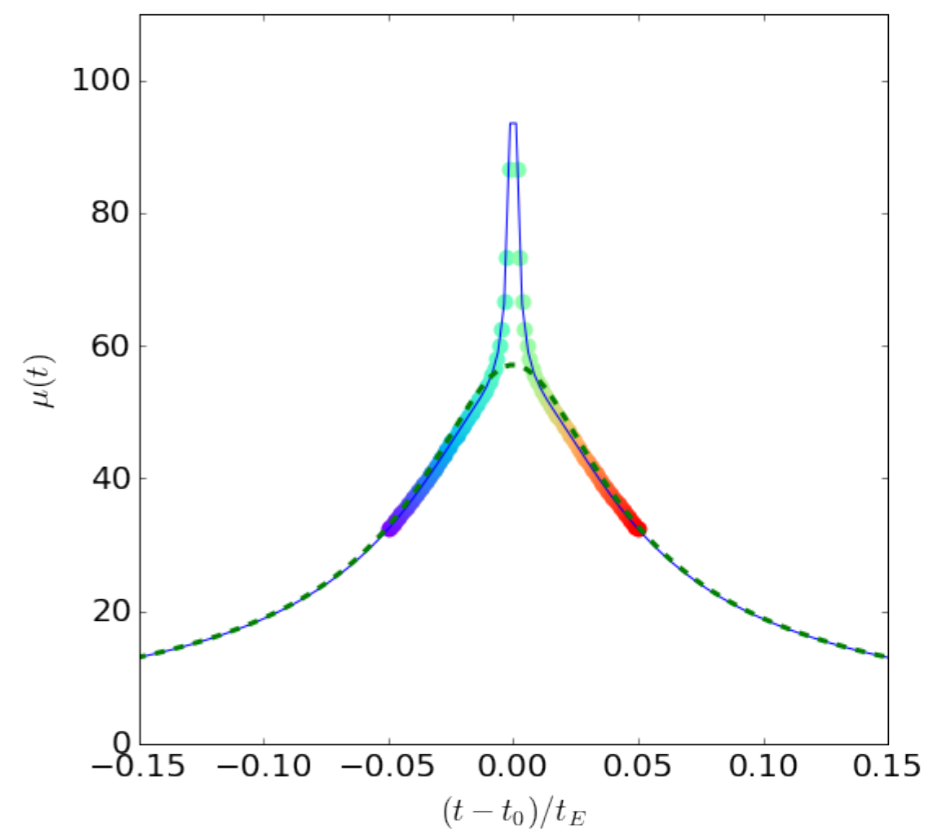
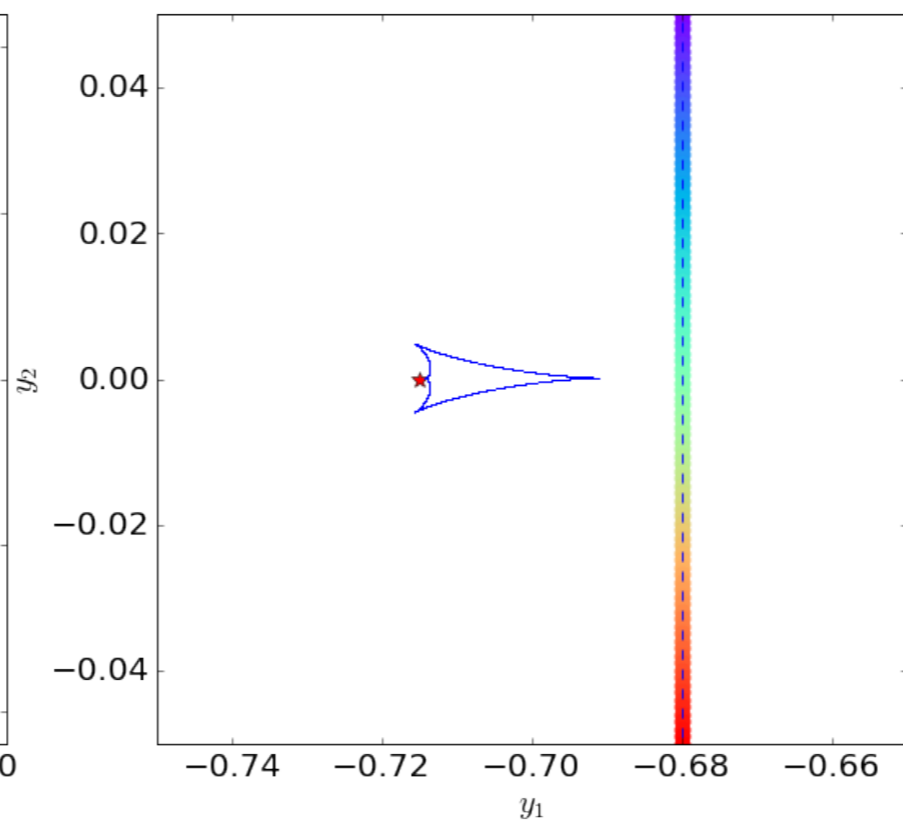
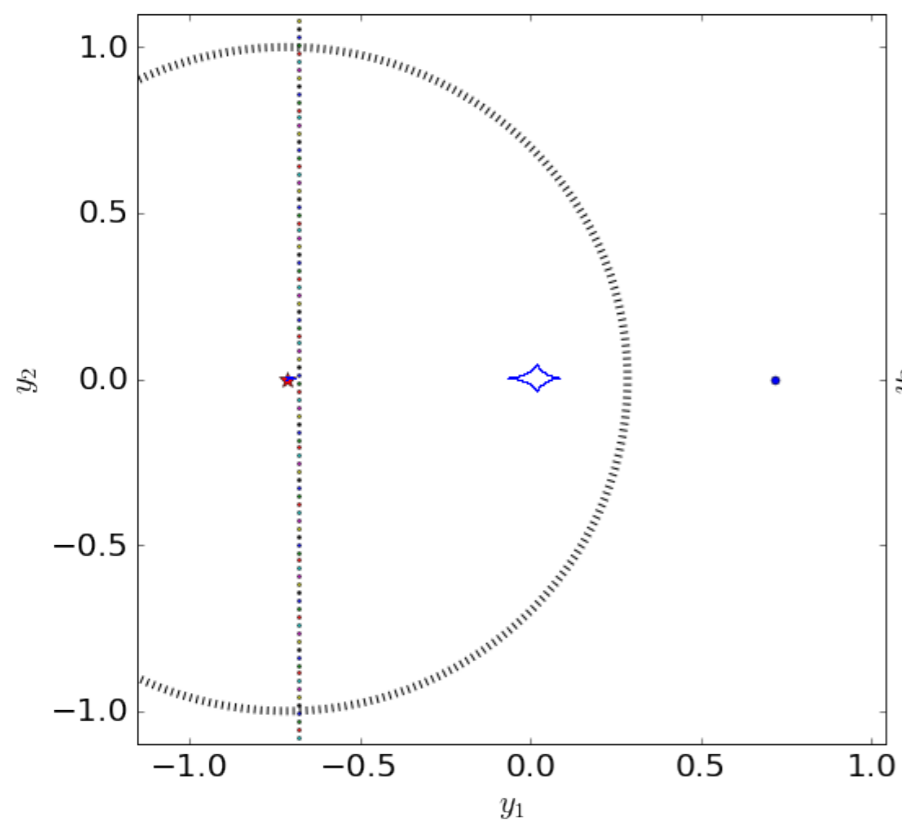
- The light curve is that of the star...
- The planet produces only a small perturbation to the magnification pattern, localized in a small region around the caustics
- Must cross one of these perturbed regions in order for the planet to be detected.
- The shape of the perturbation is determined by the caustic configuration...



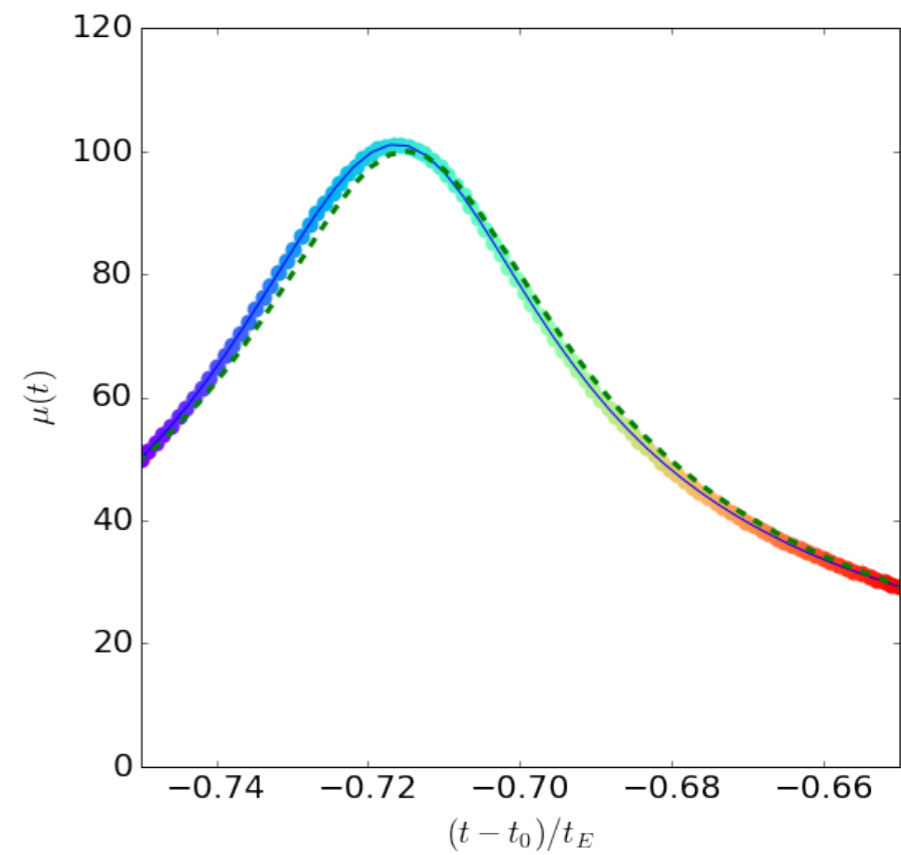
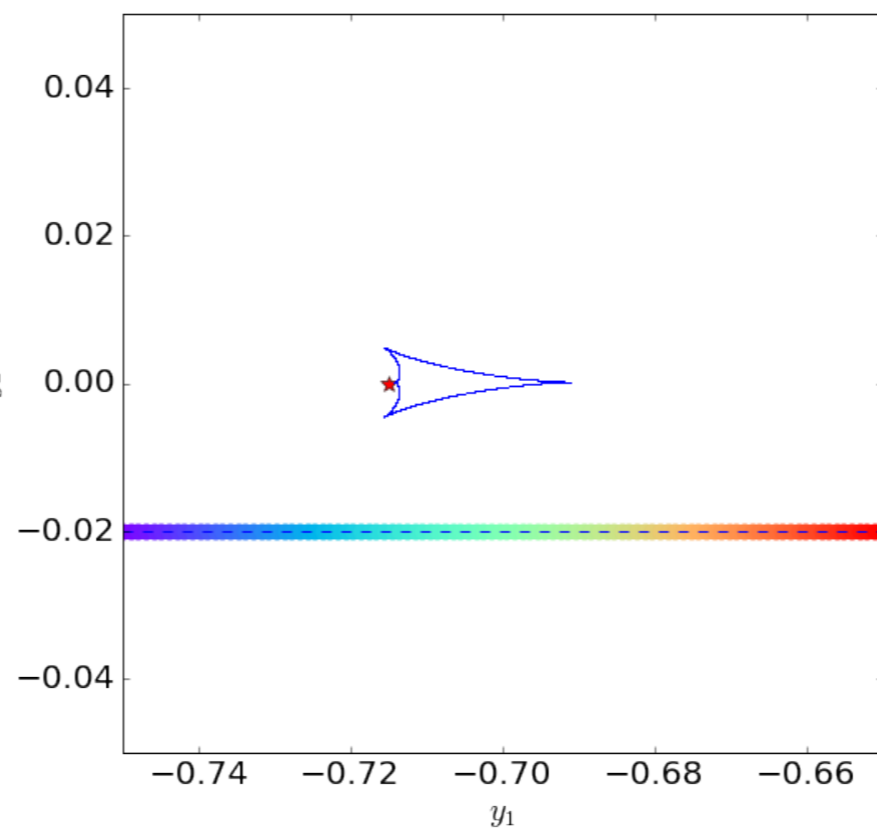
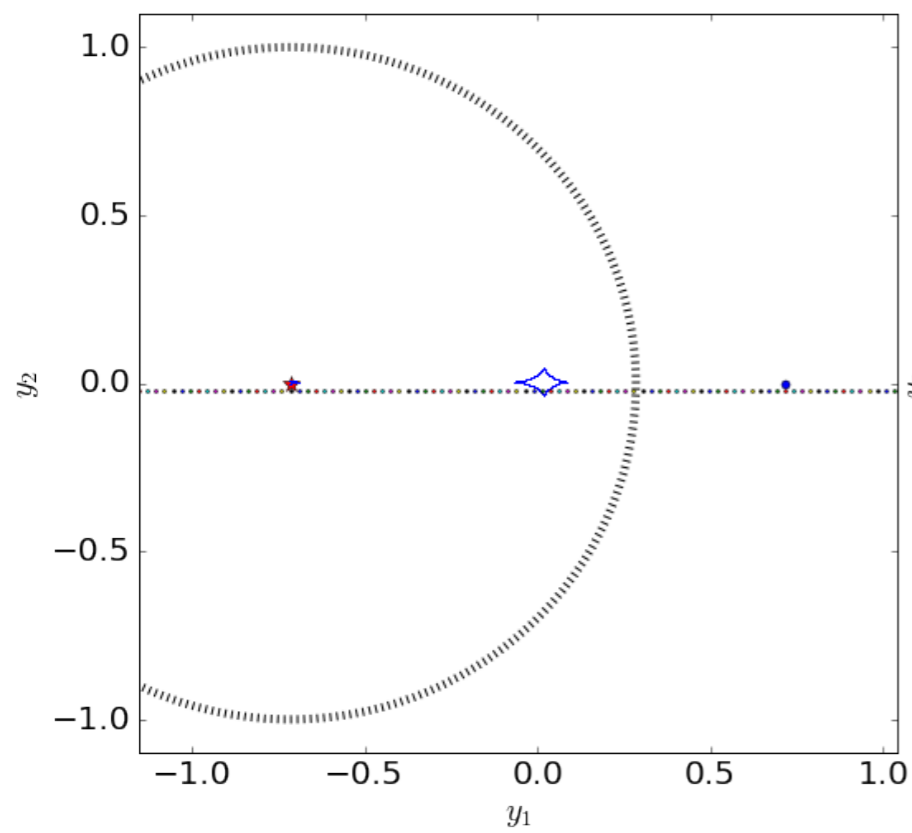
# CENTRAL CUSP PERTURBATIONS



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# PLANET DETECTION THROUGH CENTRAL CUSP PERTURBATIONS

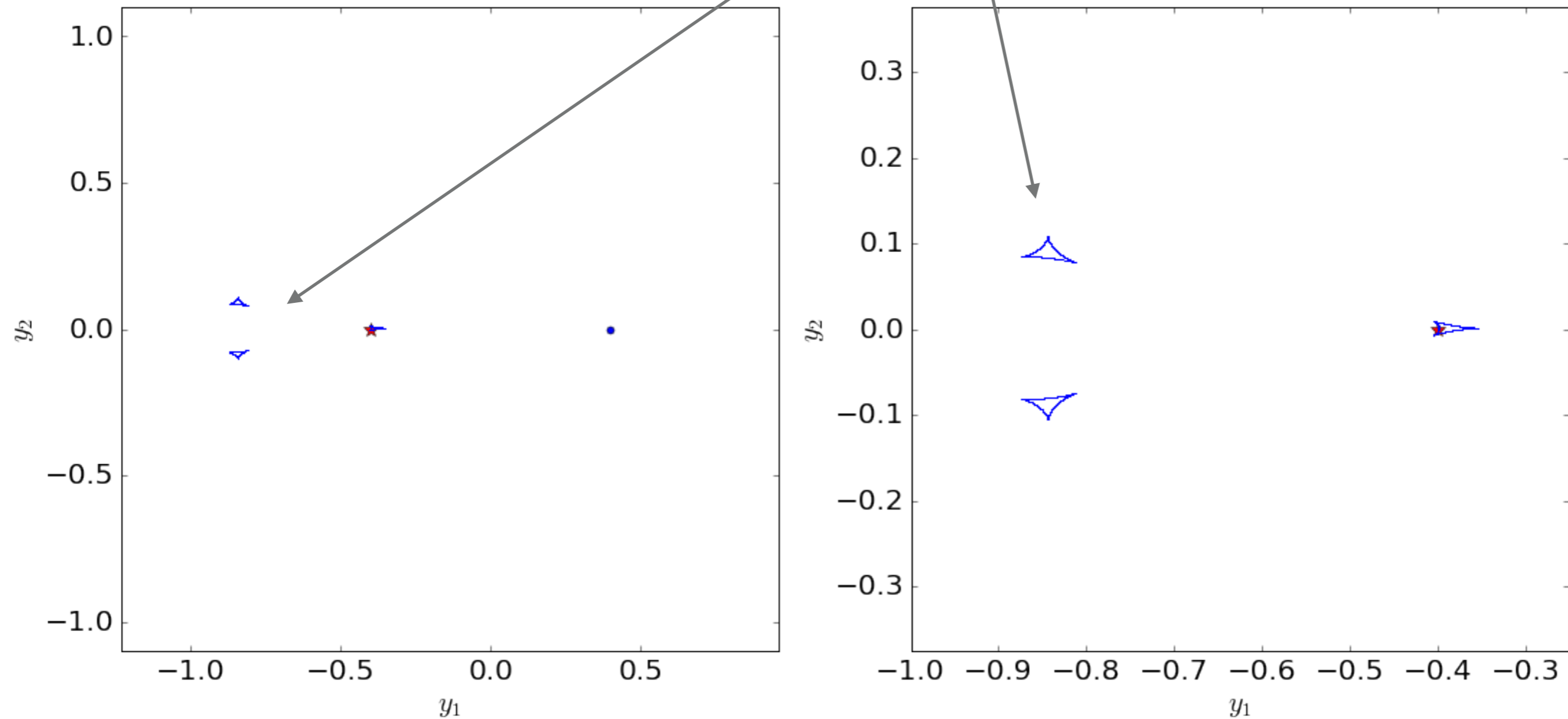
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- Only possible in the case of high magnification events (sources passing very close to the host stars)
- For this reason, they are rare events
- Advantages:
  - near the peak of the event
  - can sometimes be predicted in advance
  - high magnification makes possible to follow-up the events using small telescopes
  - more accurate photometry (and easier separation of source and lens)
- Disadvantages:
  - degeneracy wide-close topologies

# PLANETARY CAUSTICS IN CLOSE TOPOLOGIES

*planetary caustics*

*Han 2006*

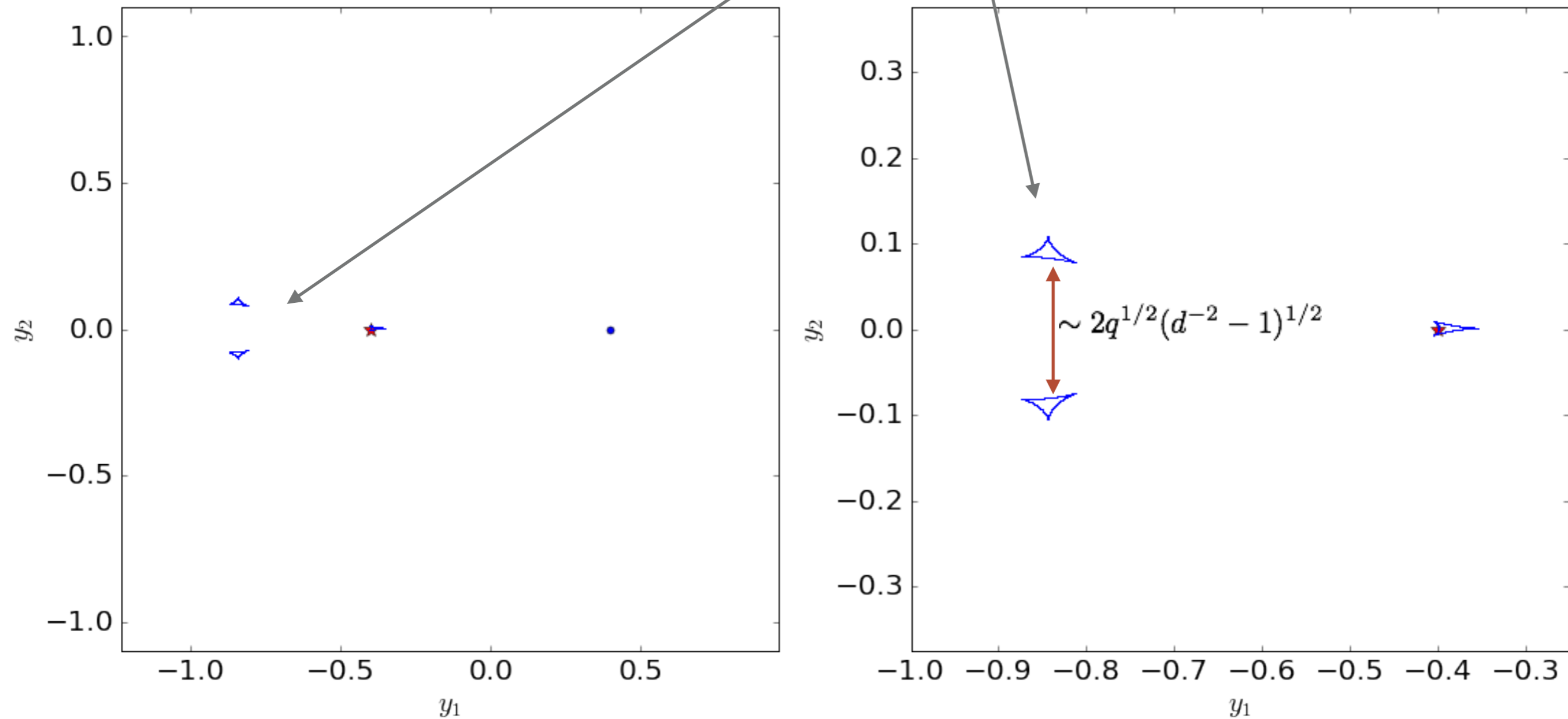


*Recommended reading: Han, C., 2006, ApJ, 638, 1080*

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Han 2006

*planetary caustics*

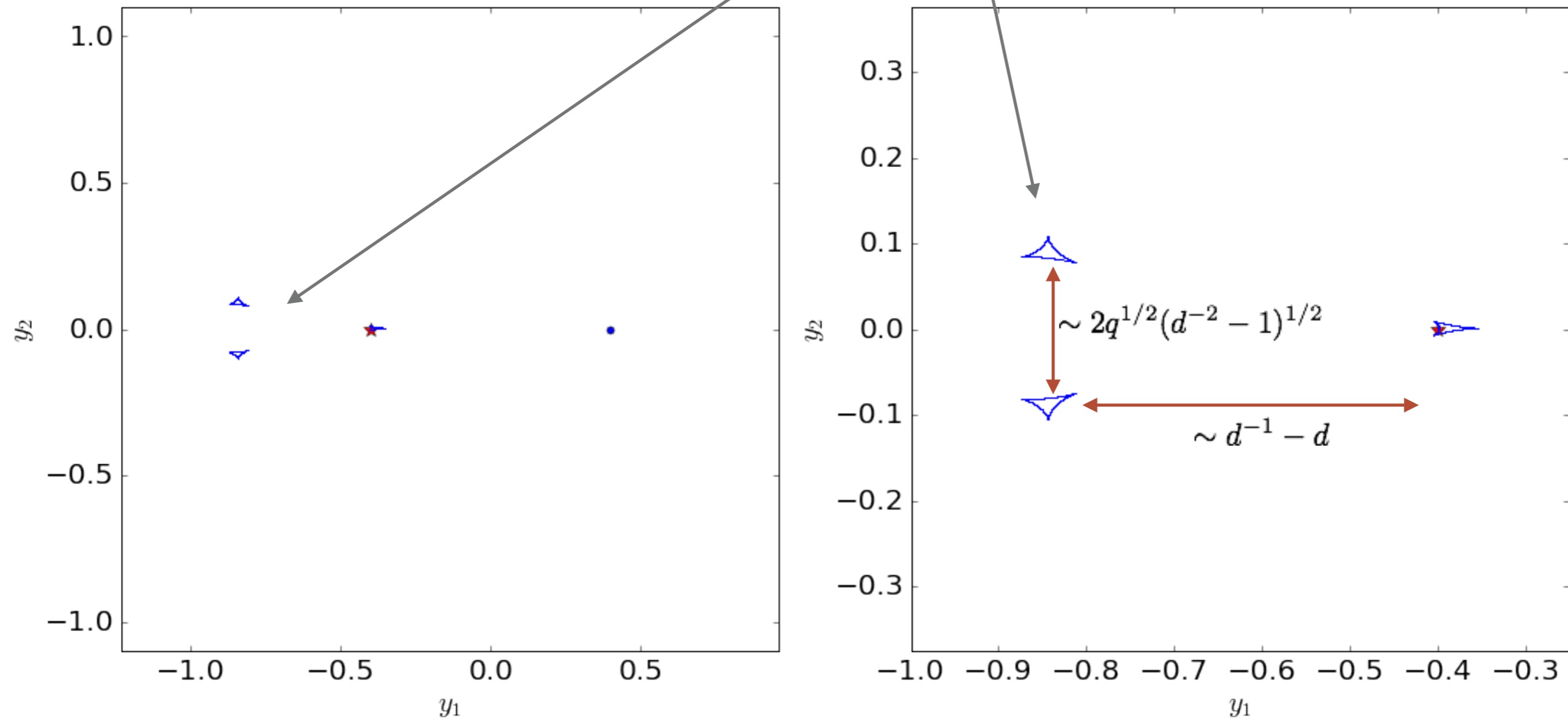


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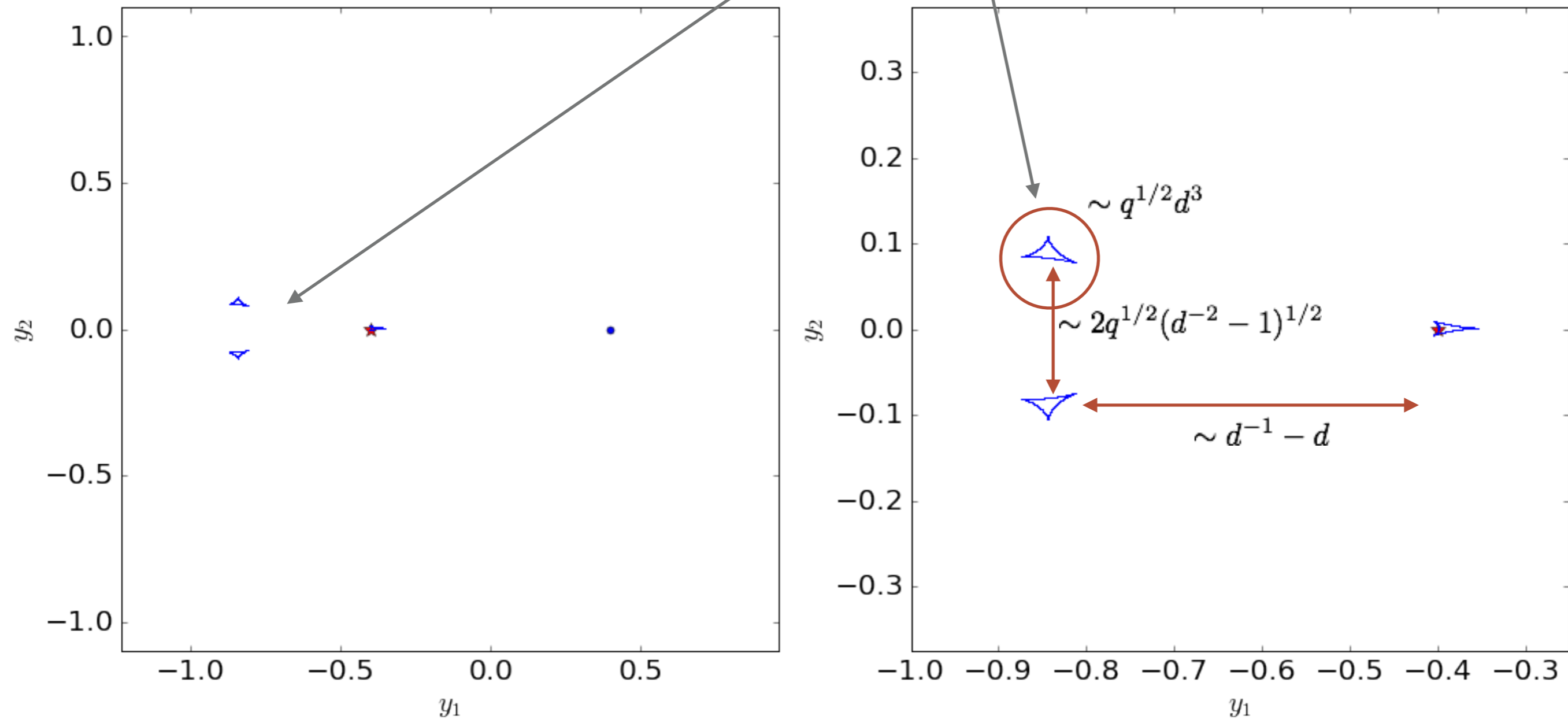


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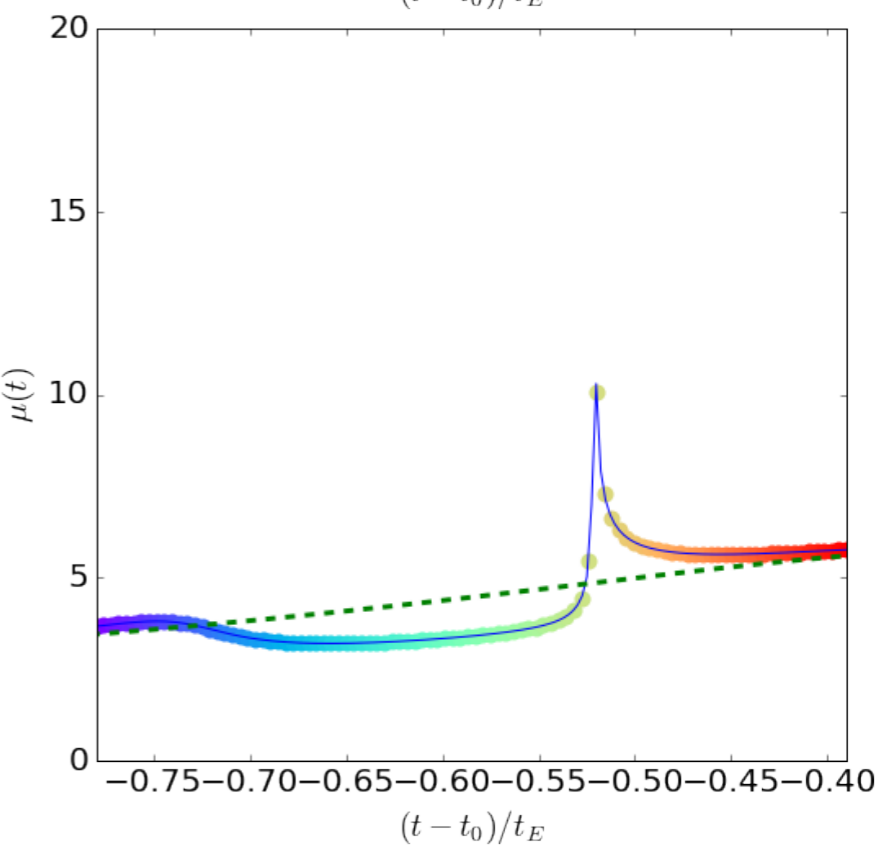
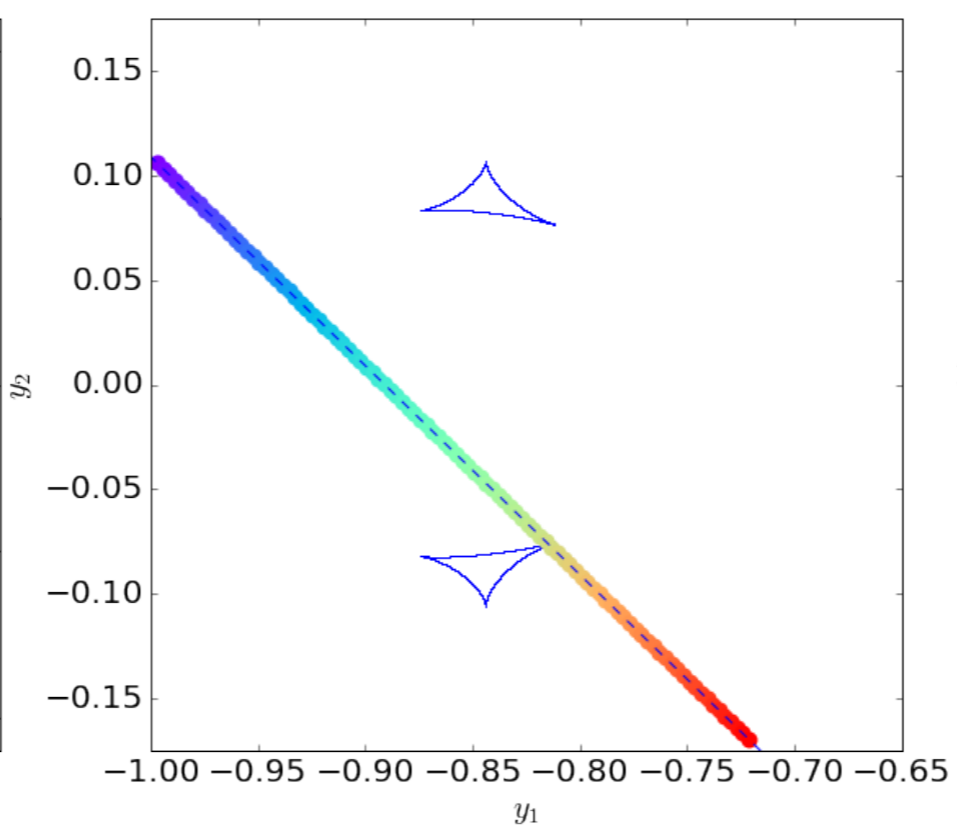
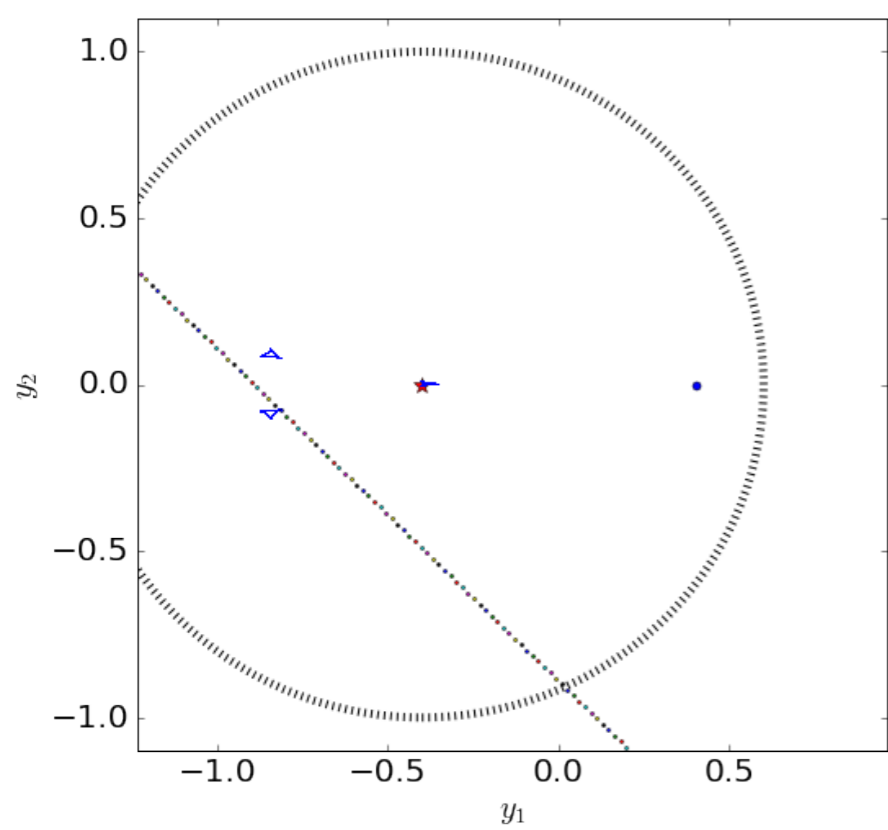
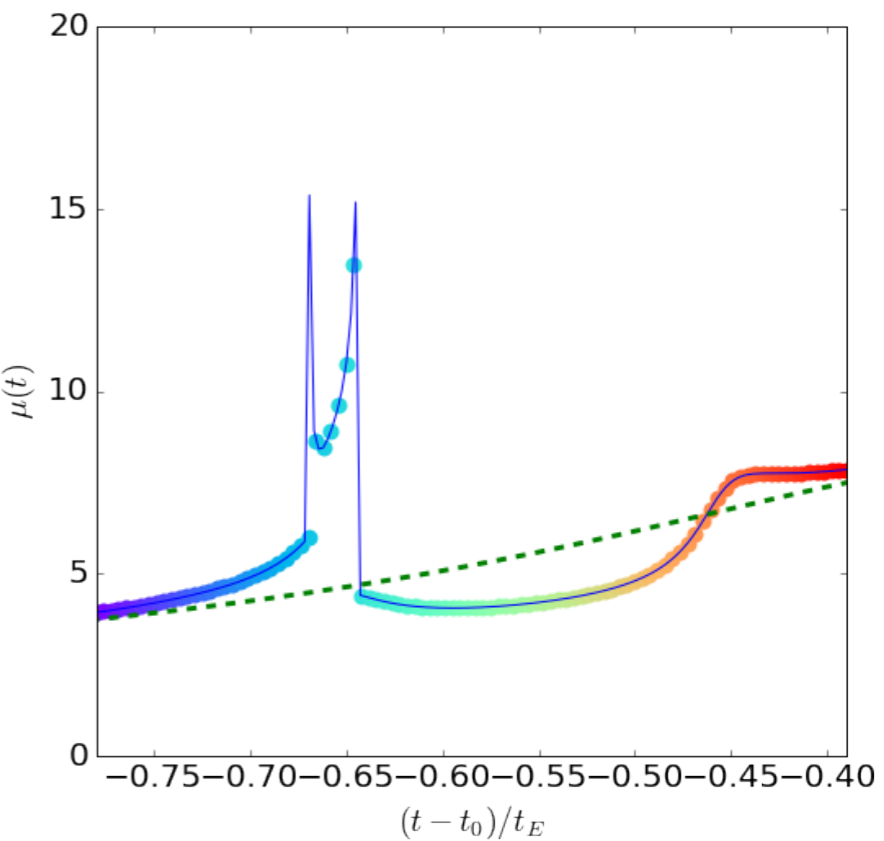
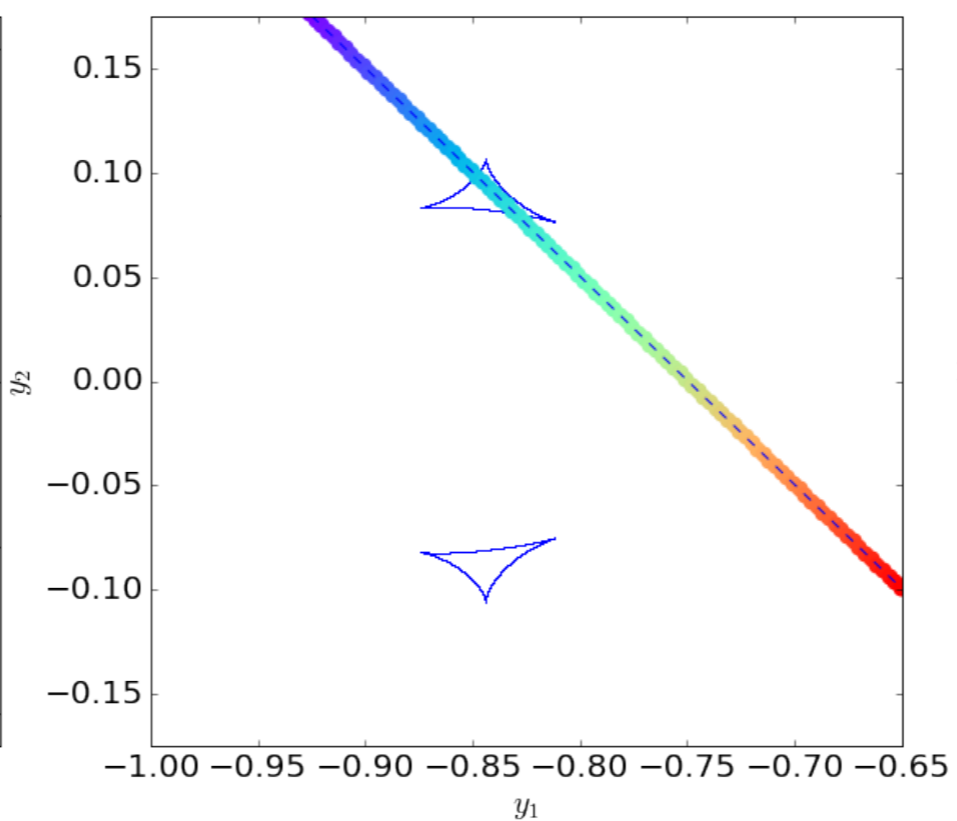
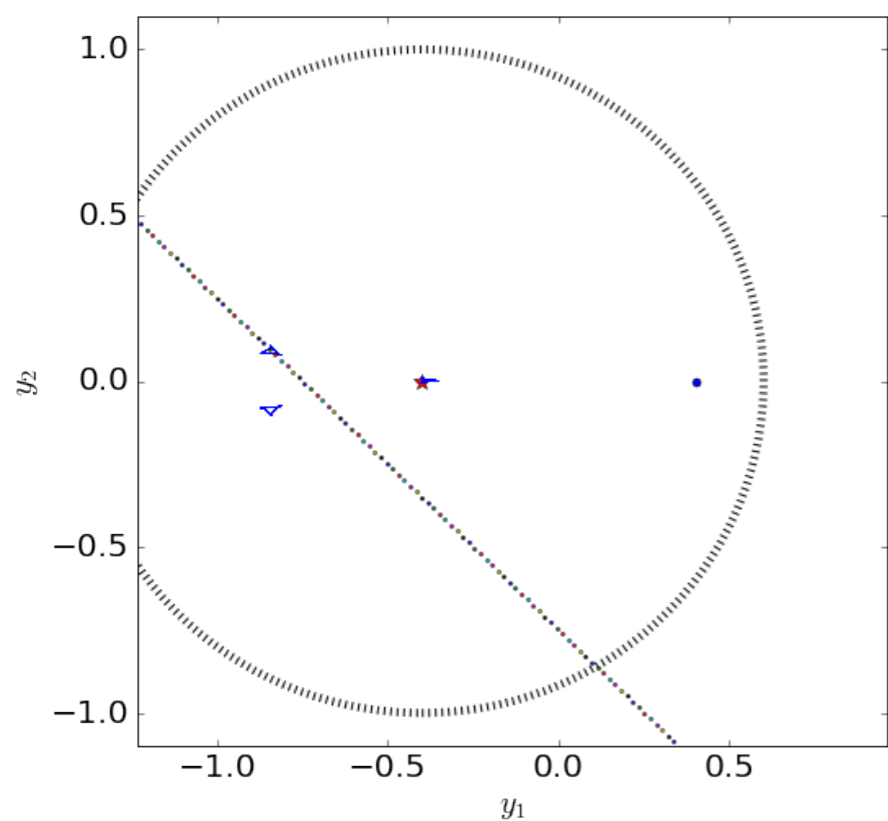
Han 2006

planetary caustics

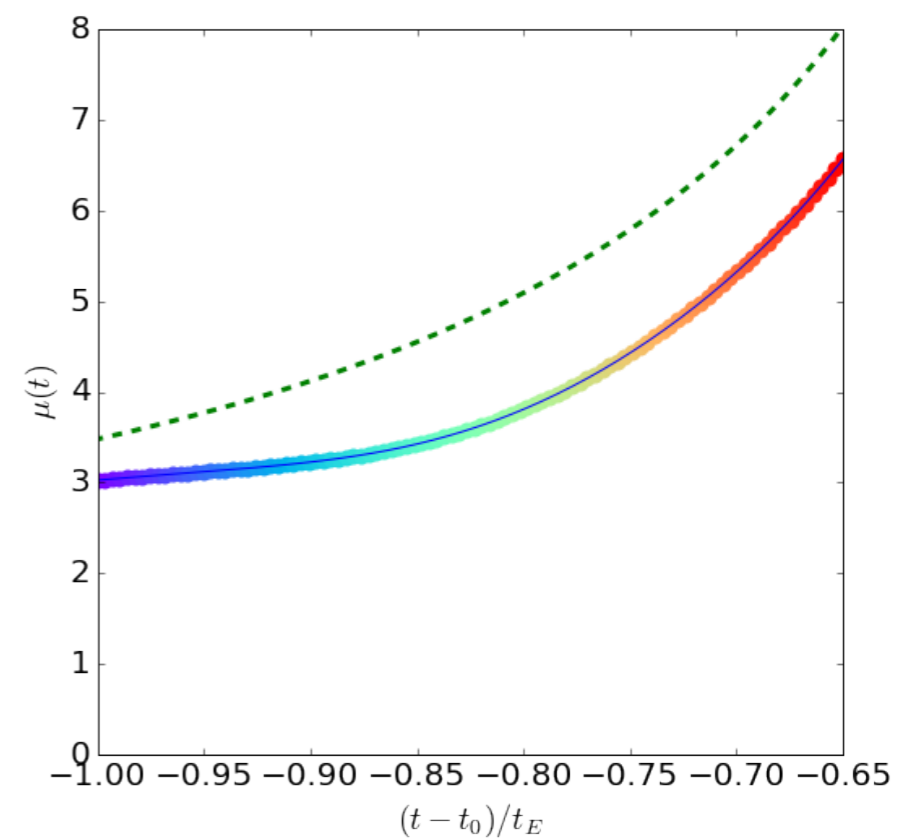
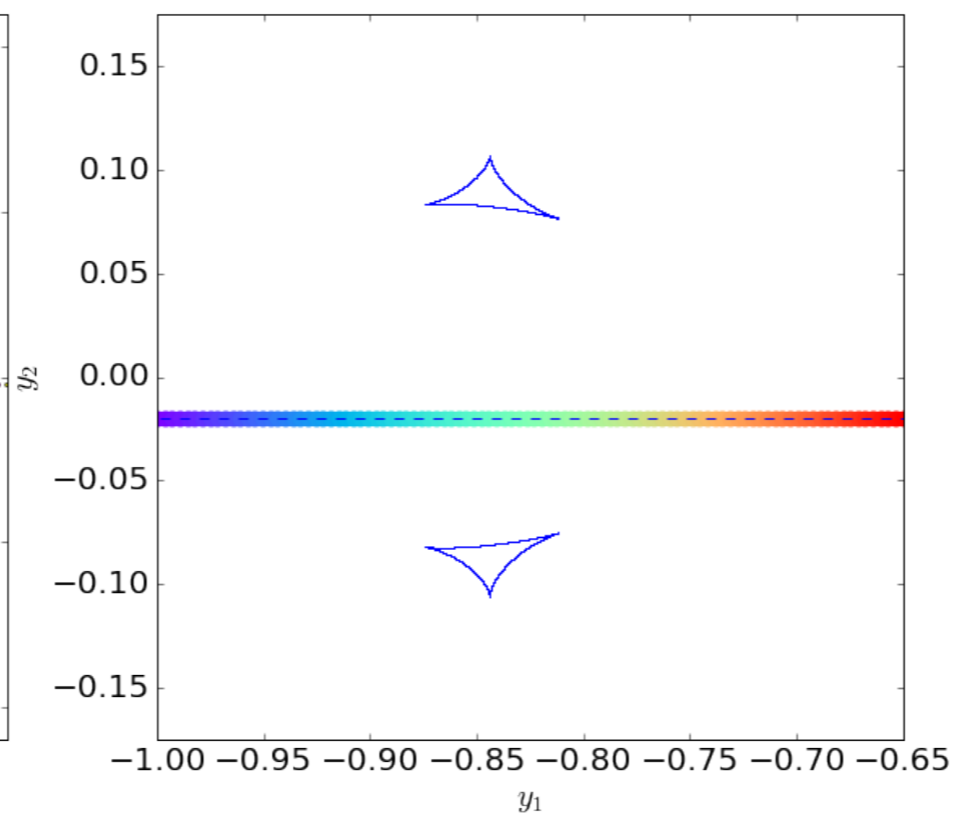
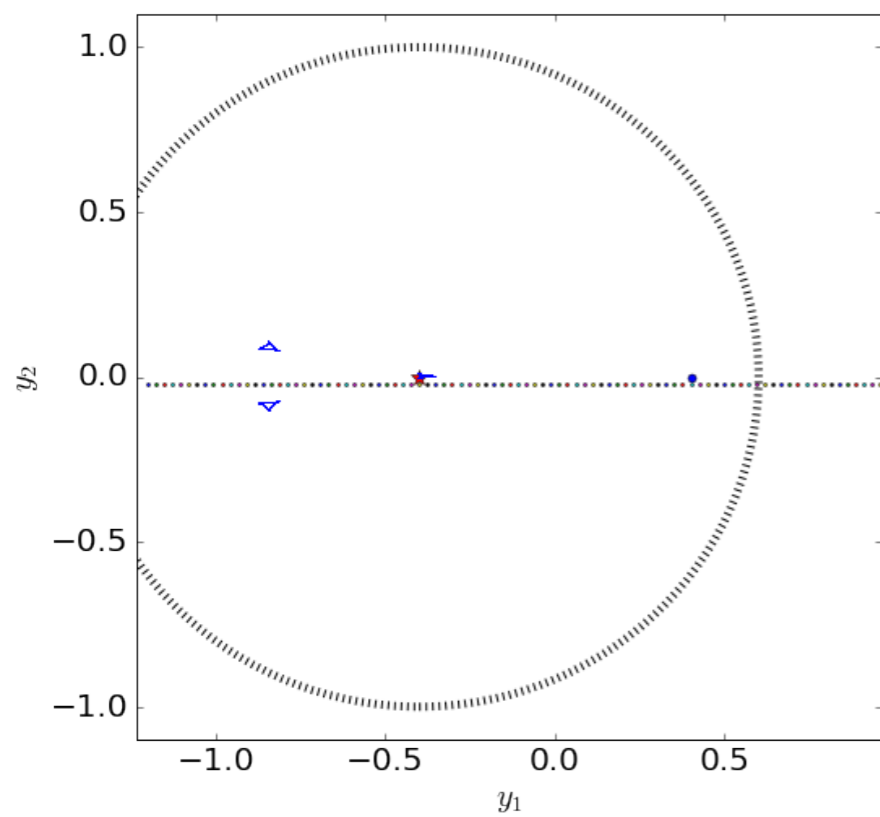
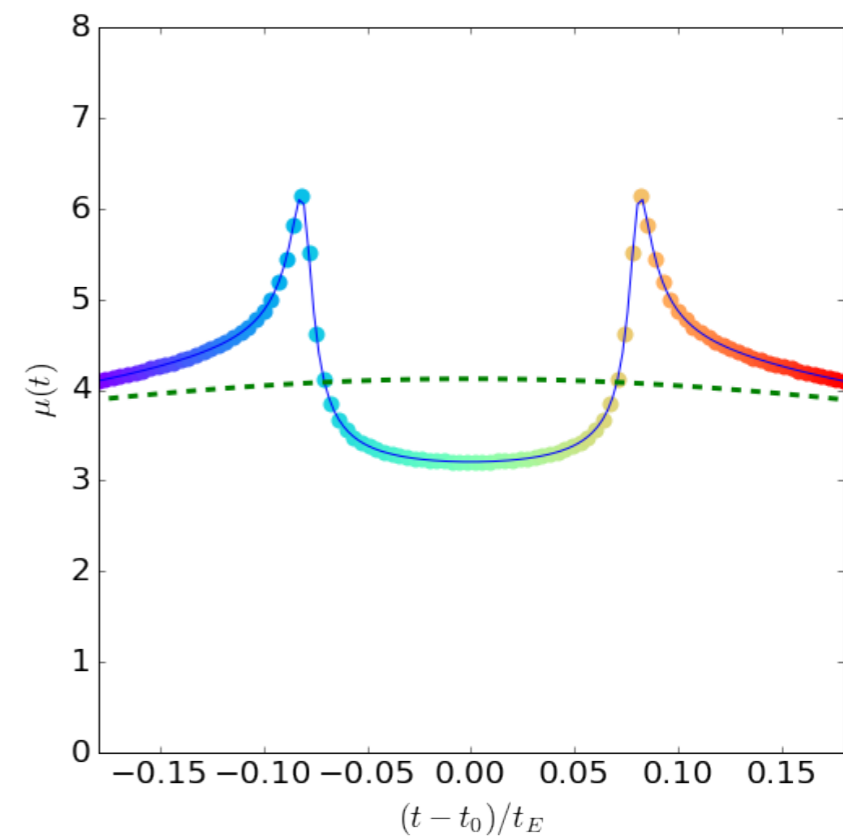
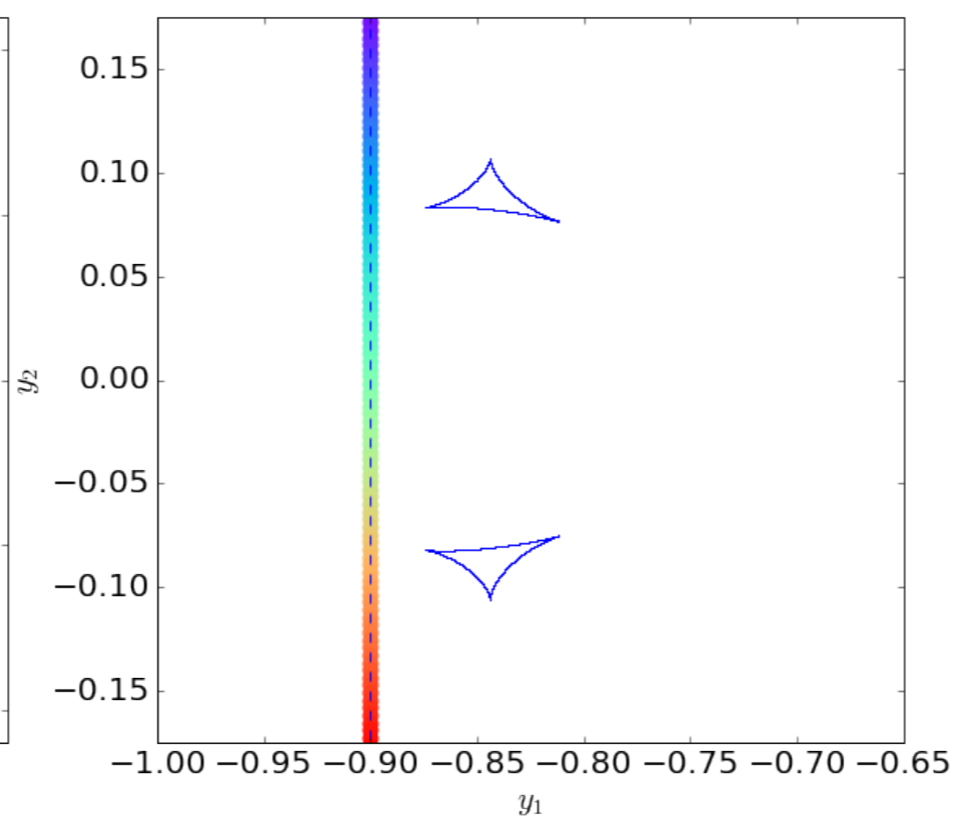
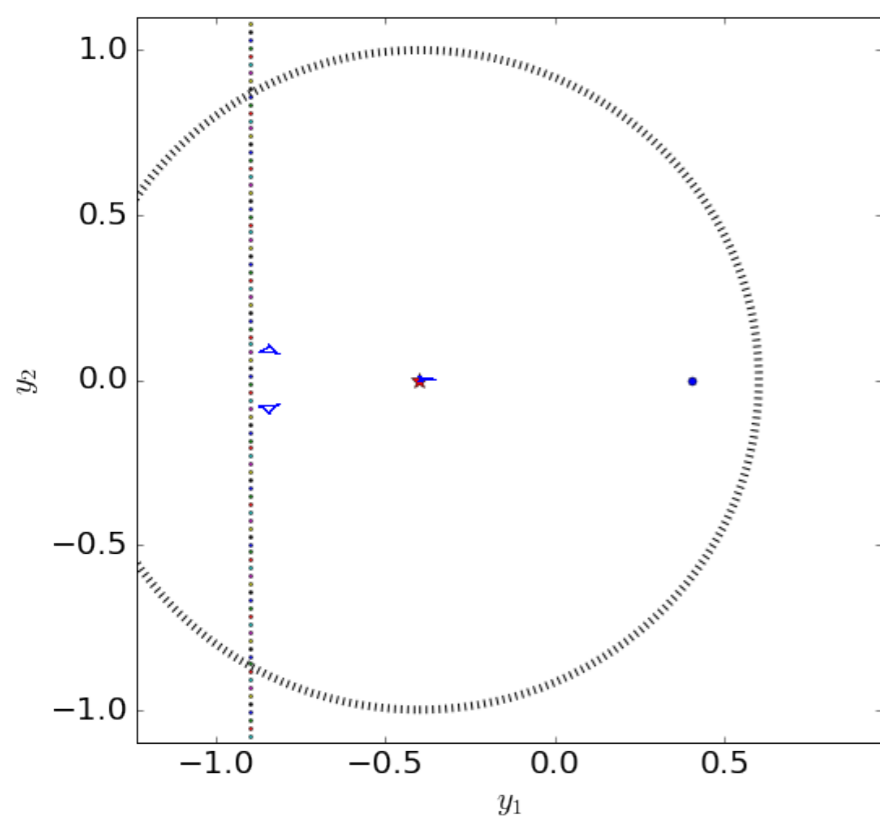


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# PLANETARY CAUSTICS PERTURBATIONS IN CLOSE TOPOLOGIES

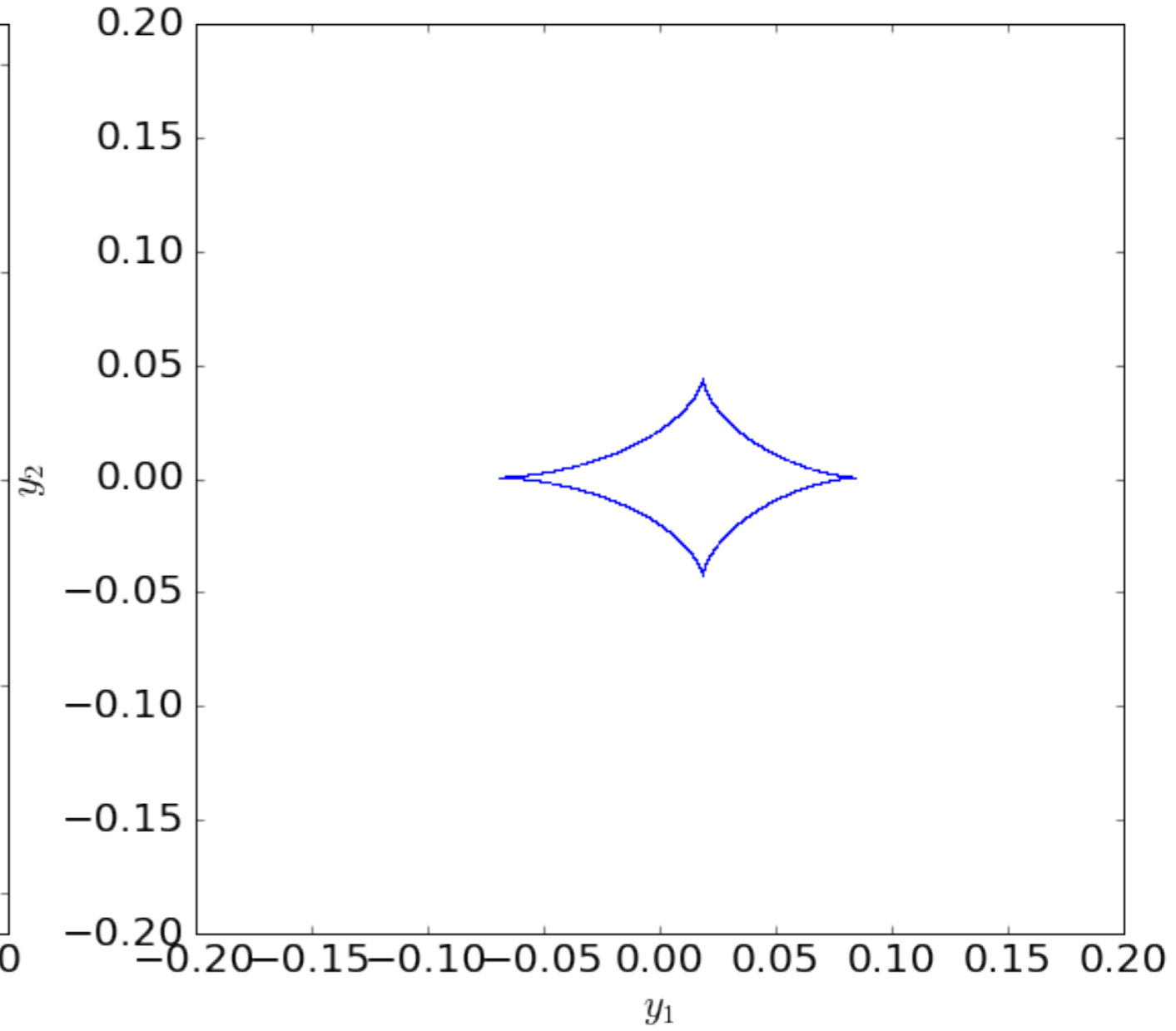
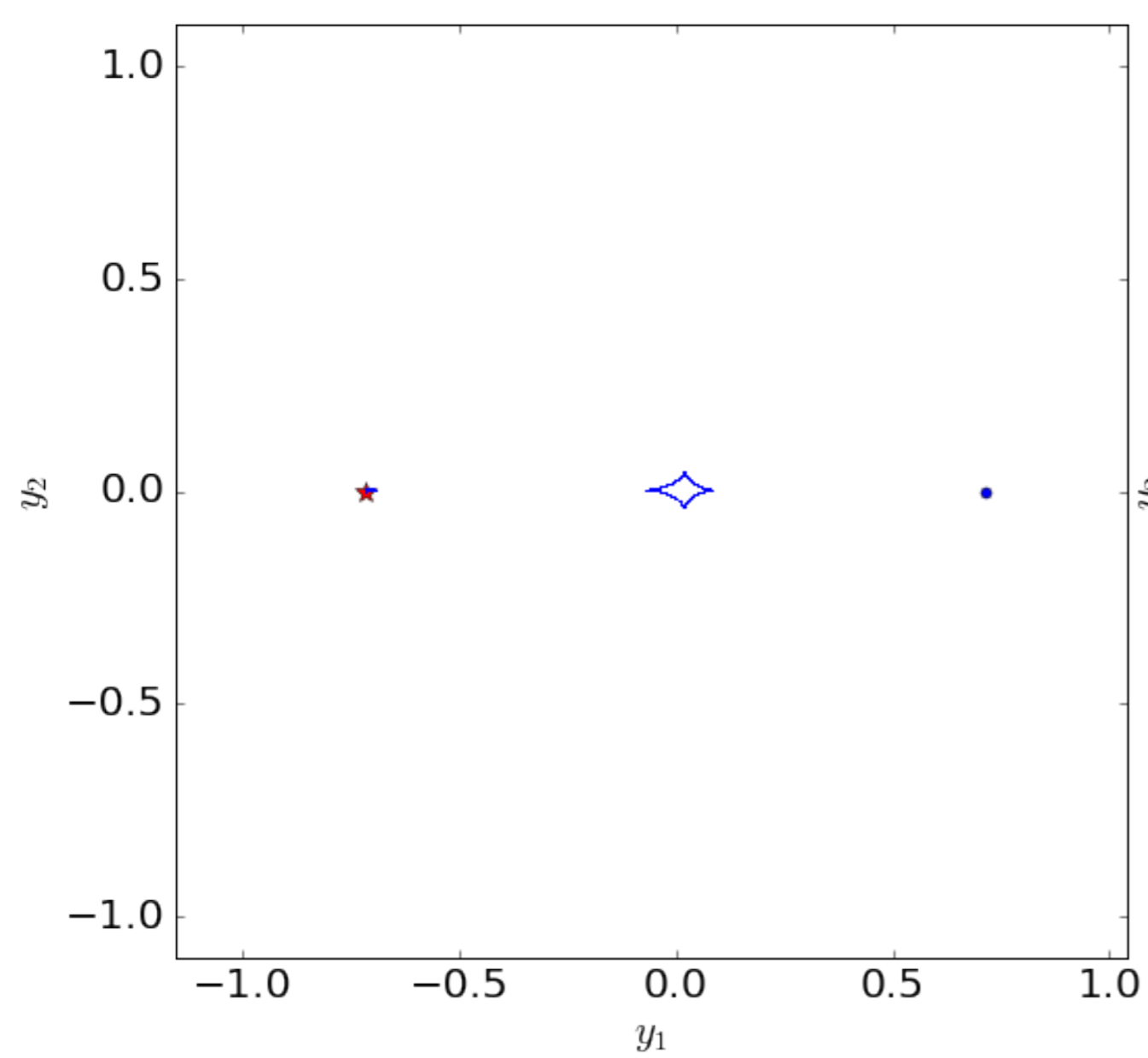


# PLANETARY CAUSTICS PERTURBATIONS IN CLOSE TOPOLOGIES



# PLANETARY CAUSTICS IN WIDE TOPOLOGIES

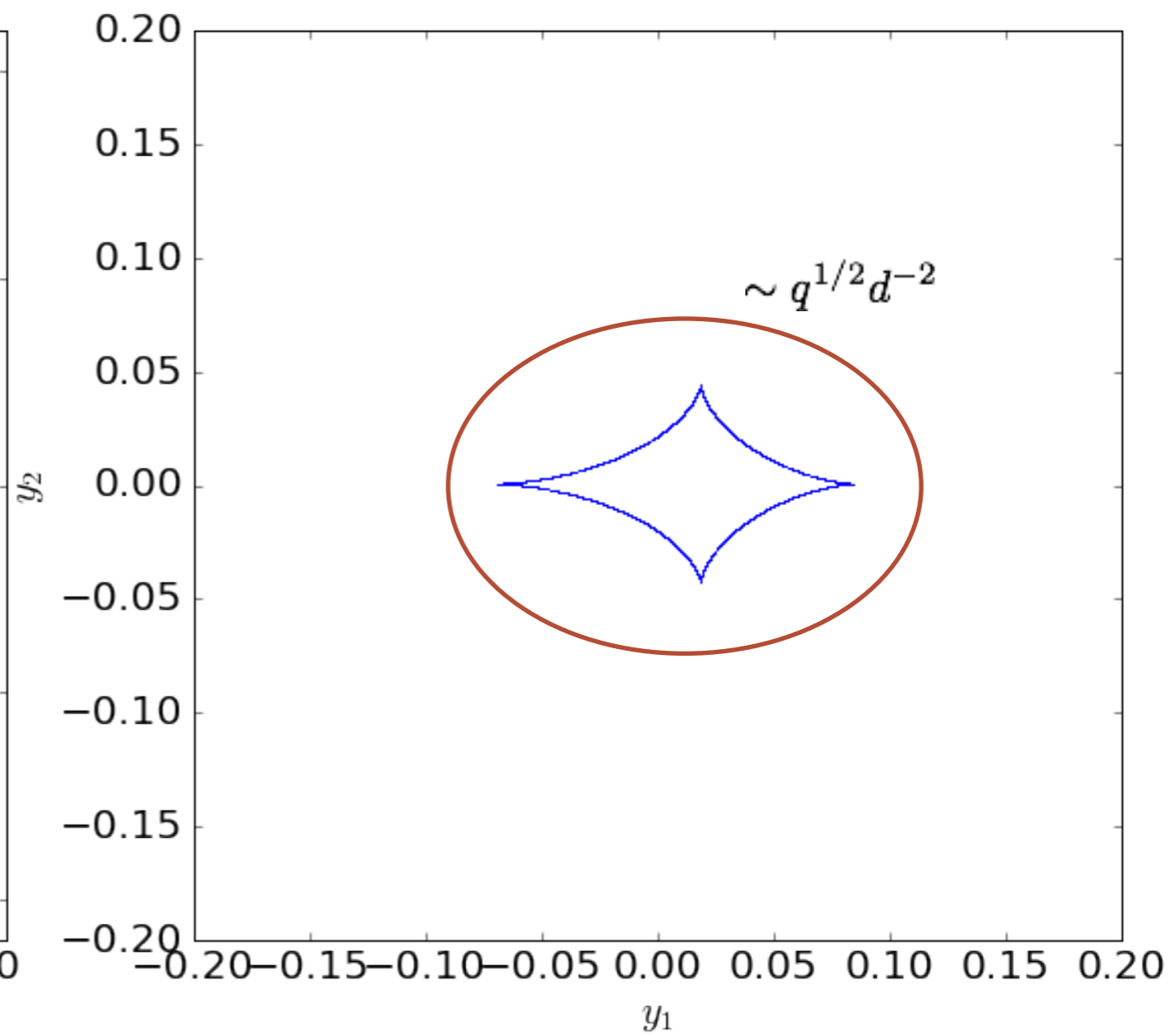
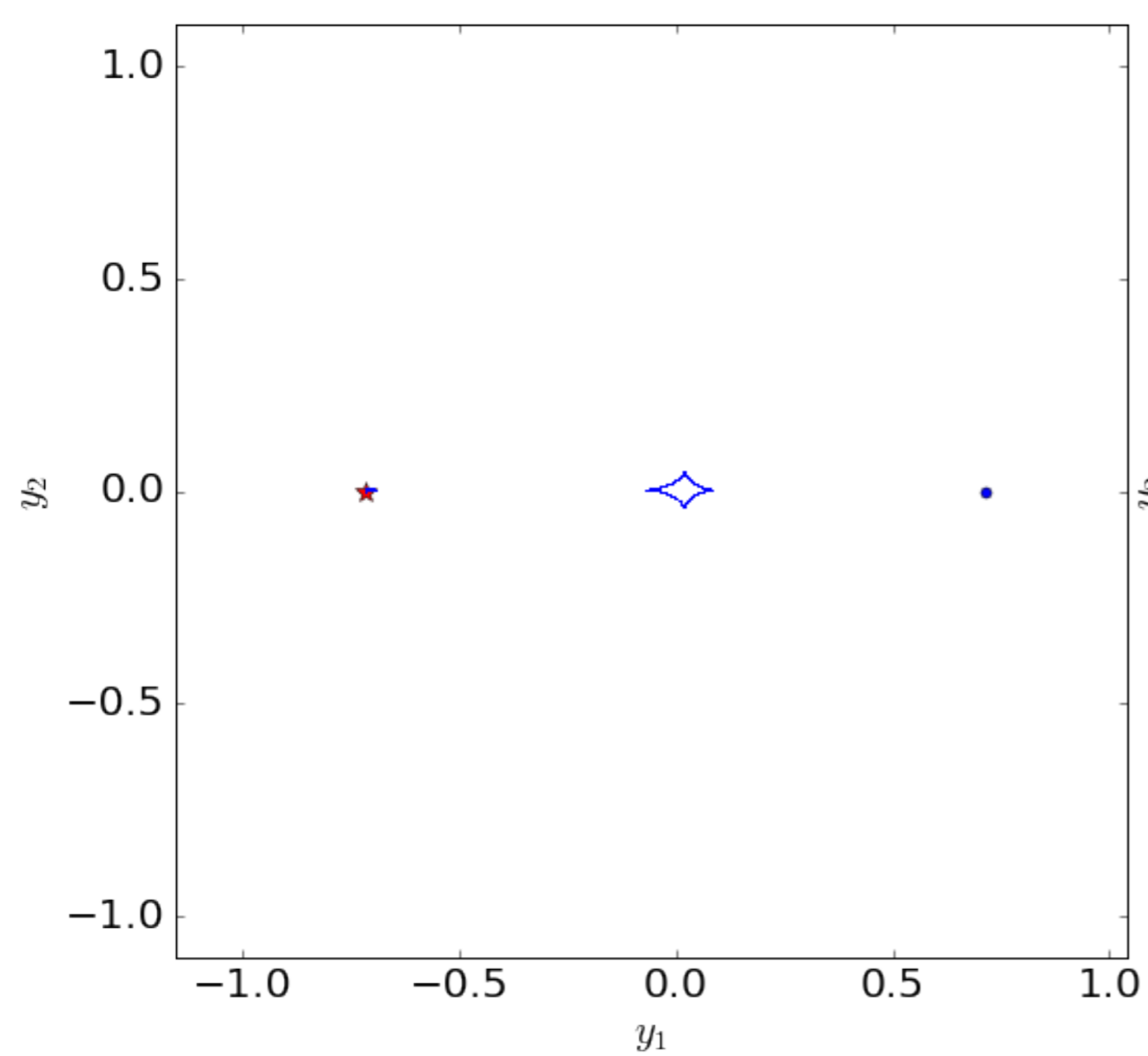
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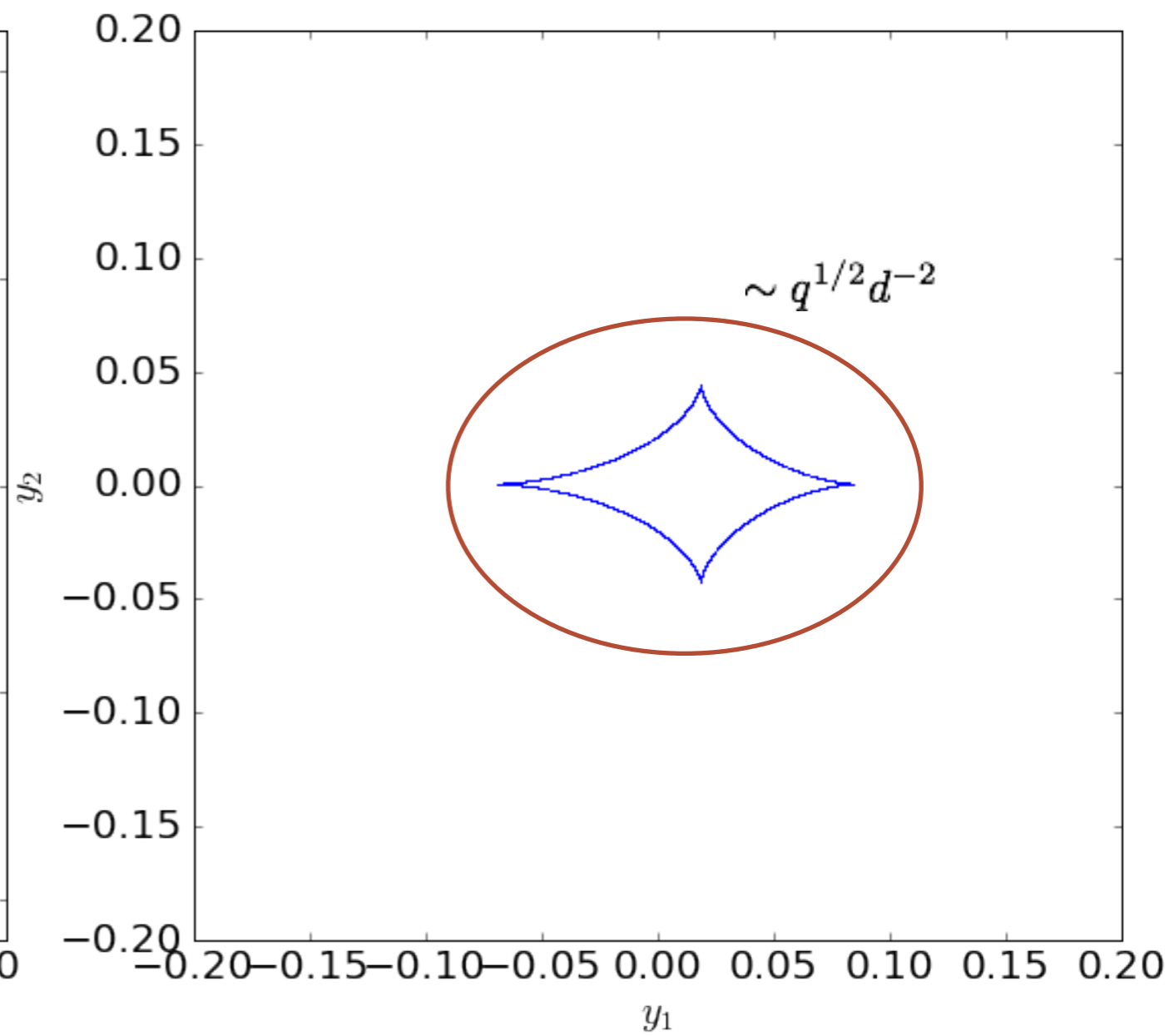
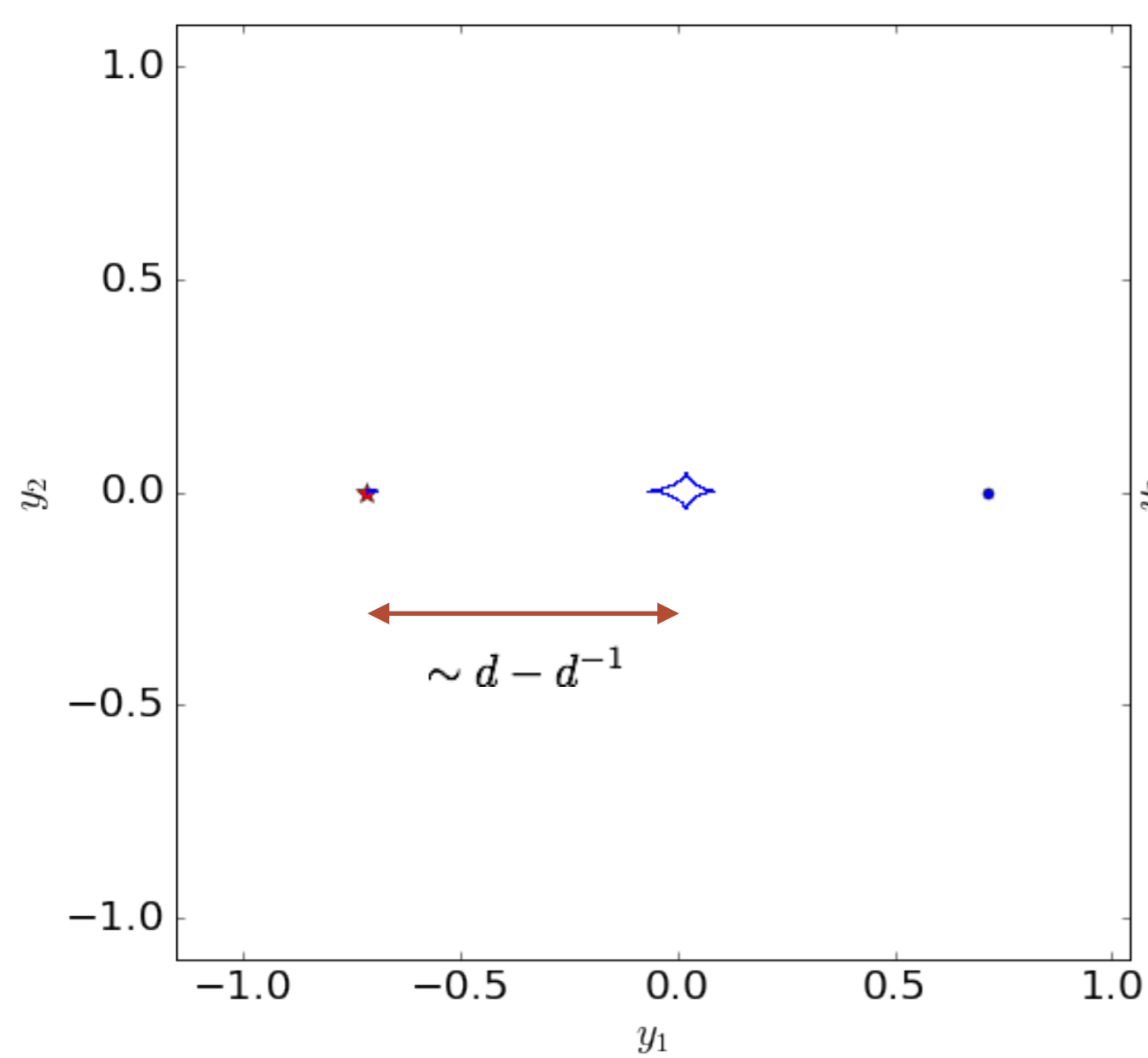
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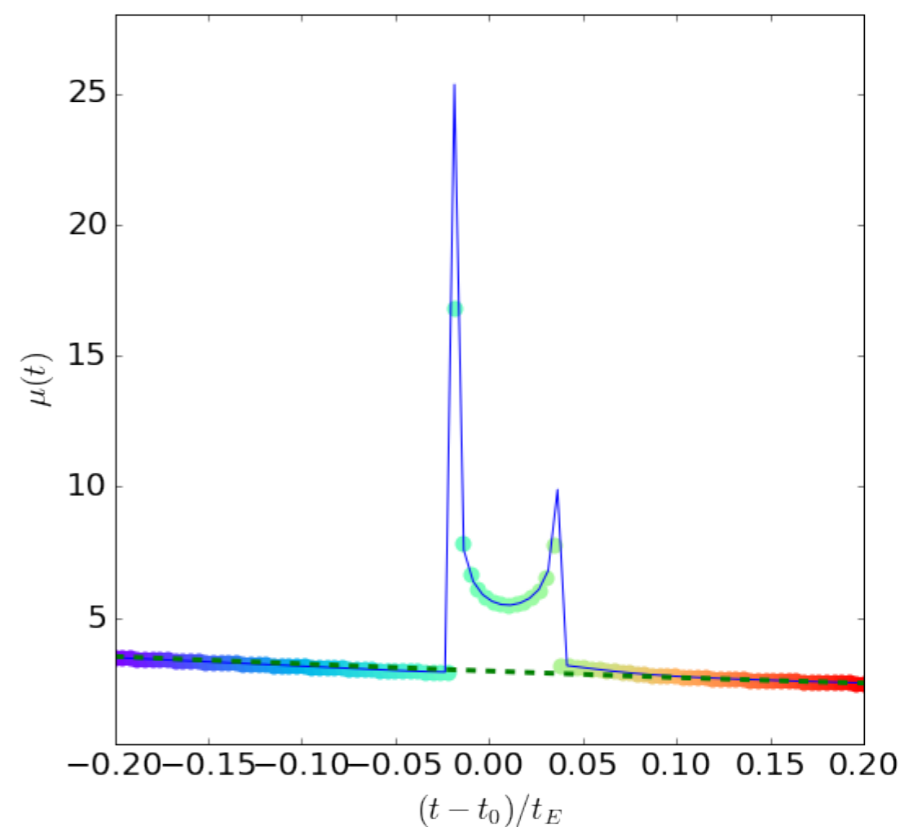
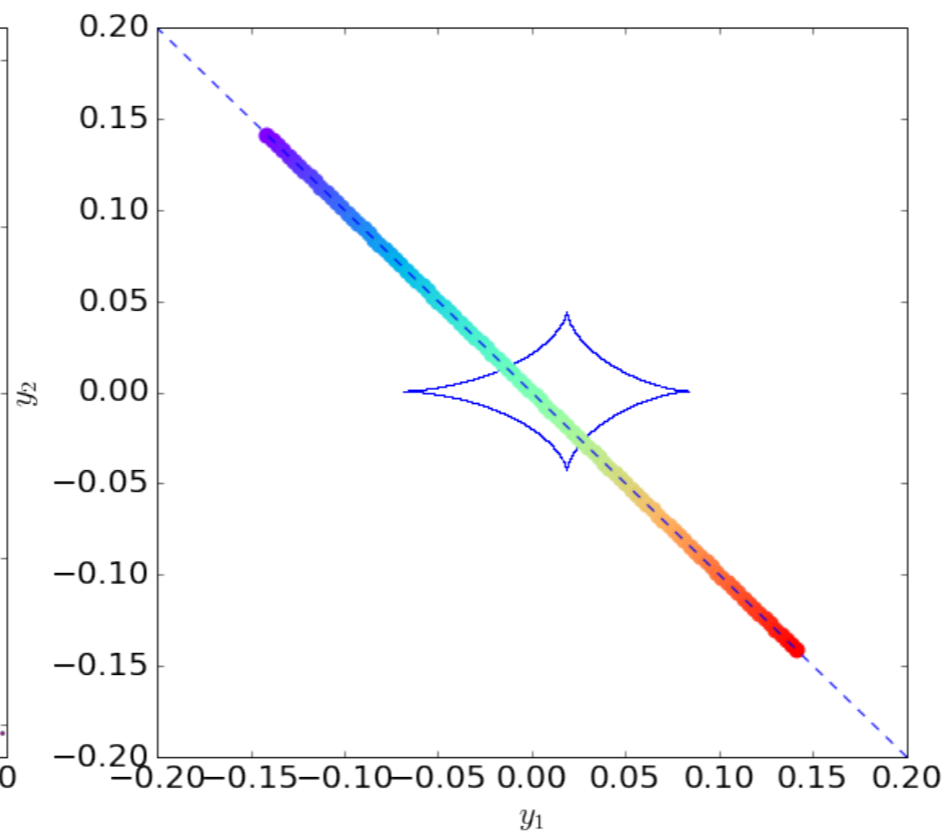
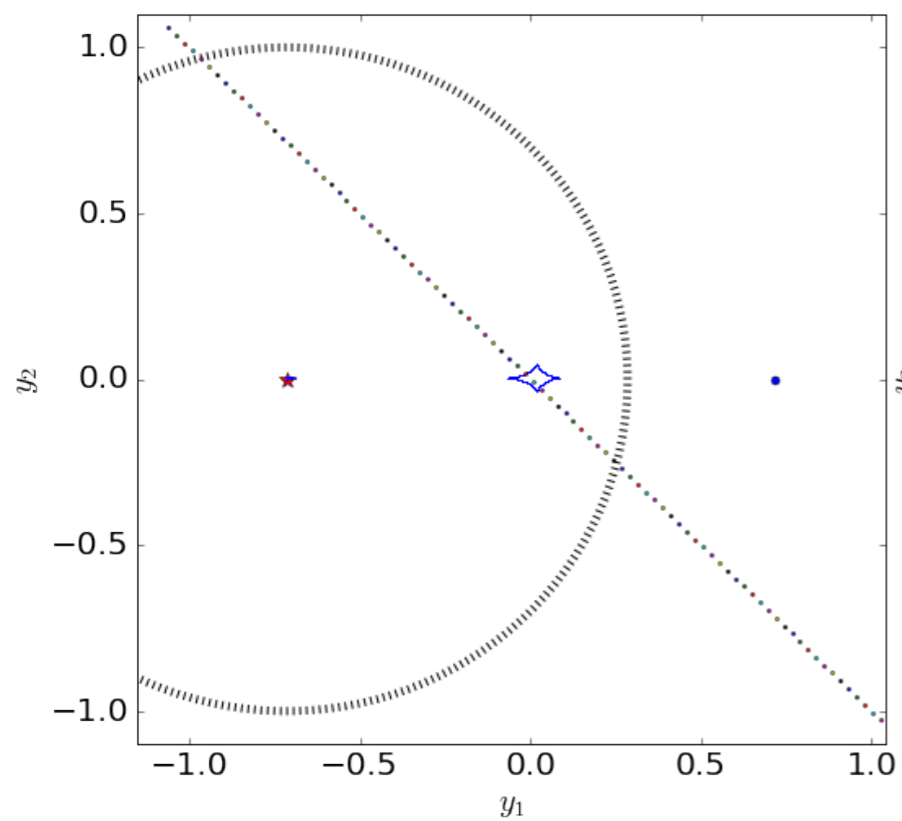
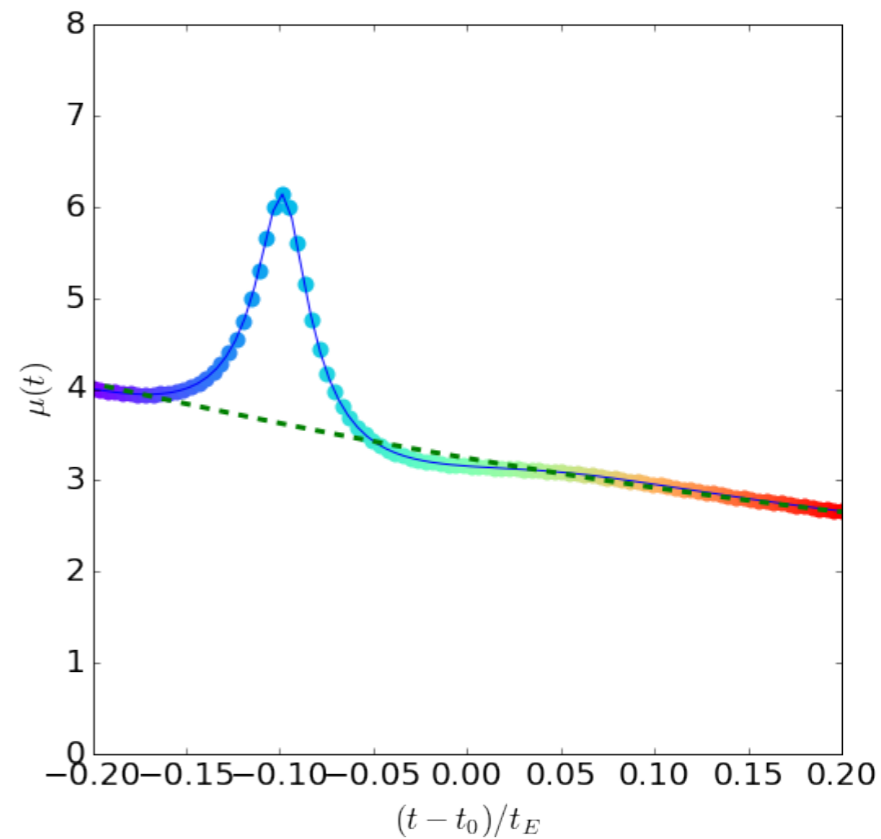
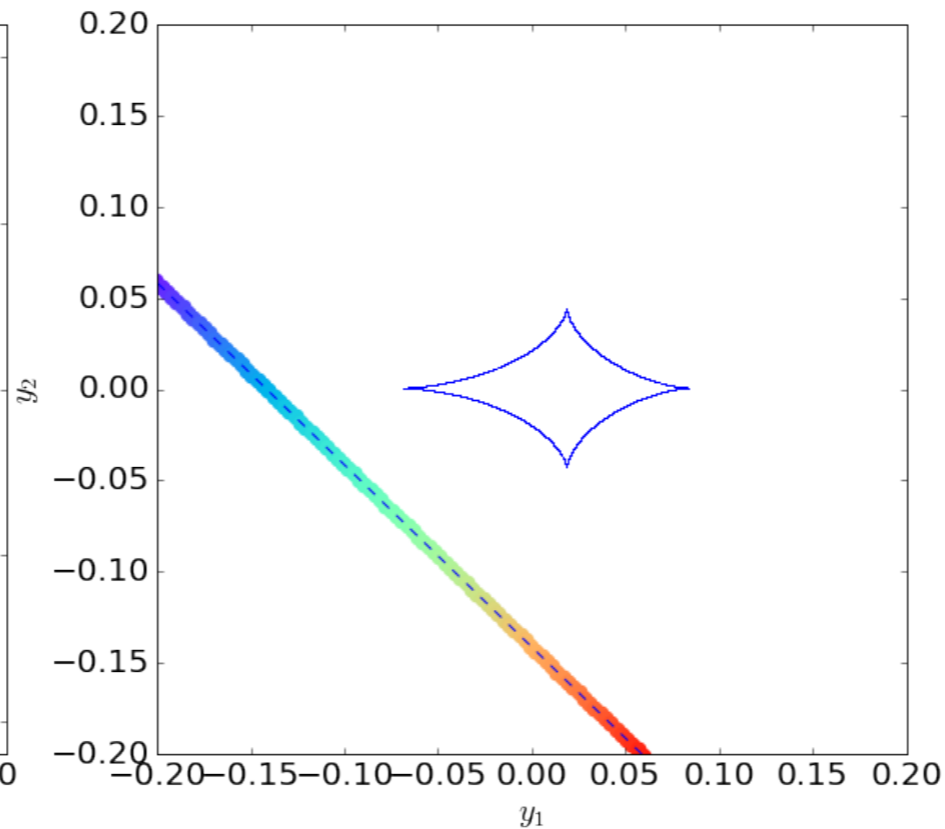
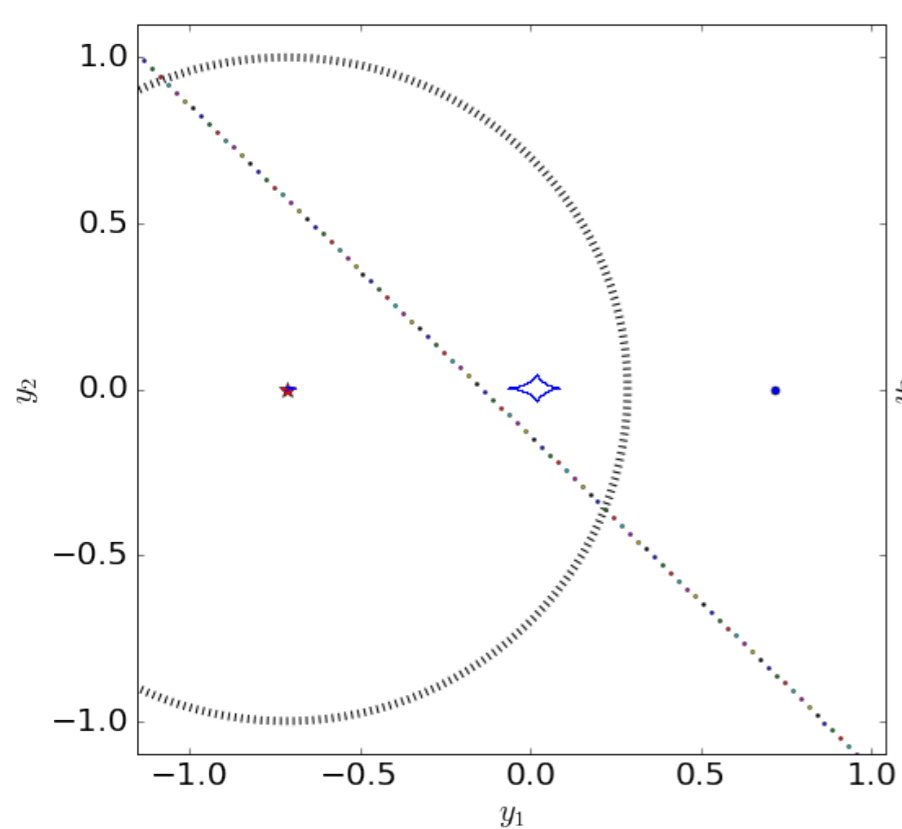


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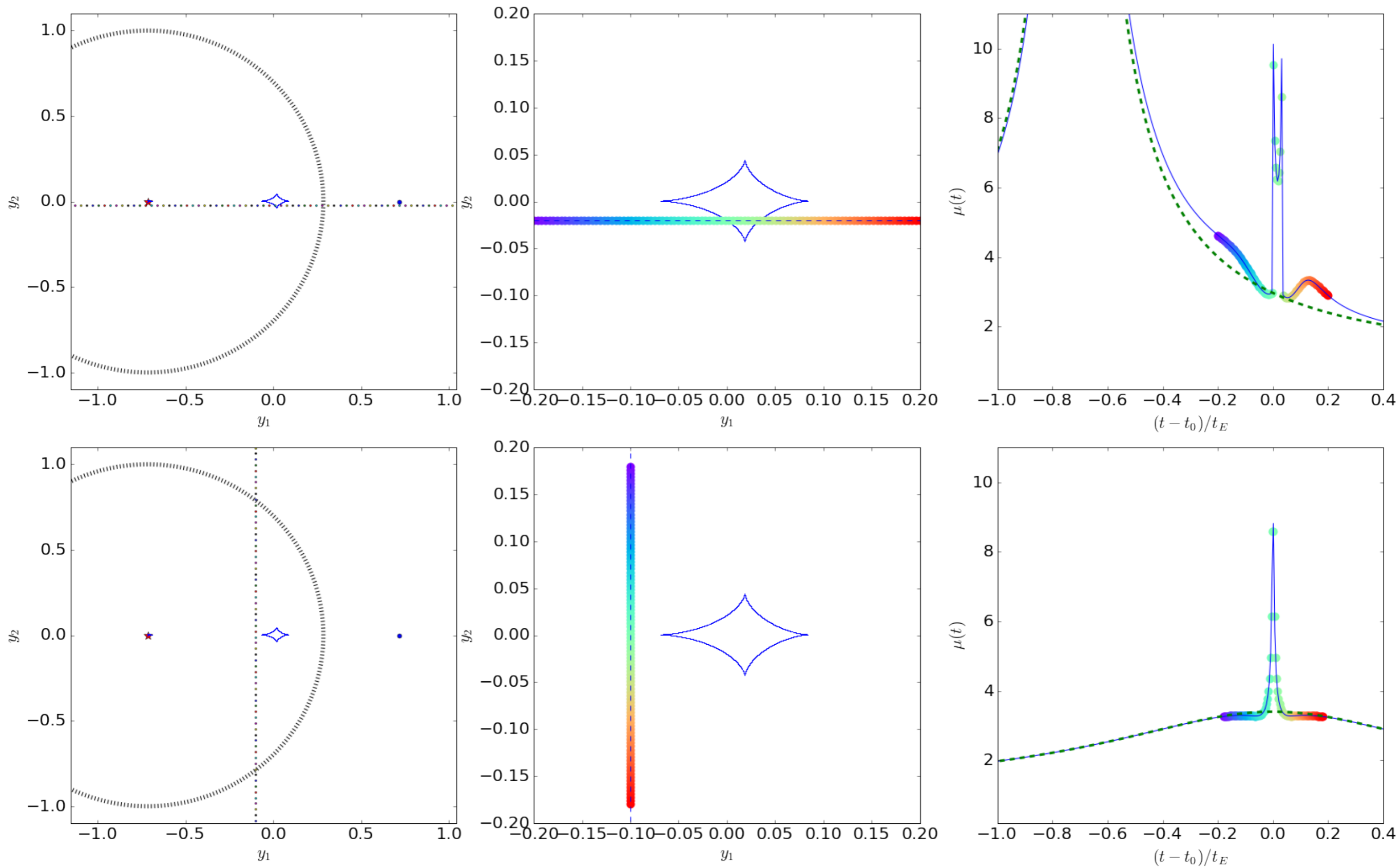
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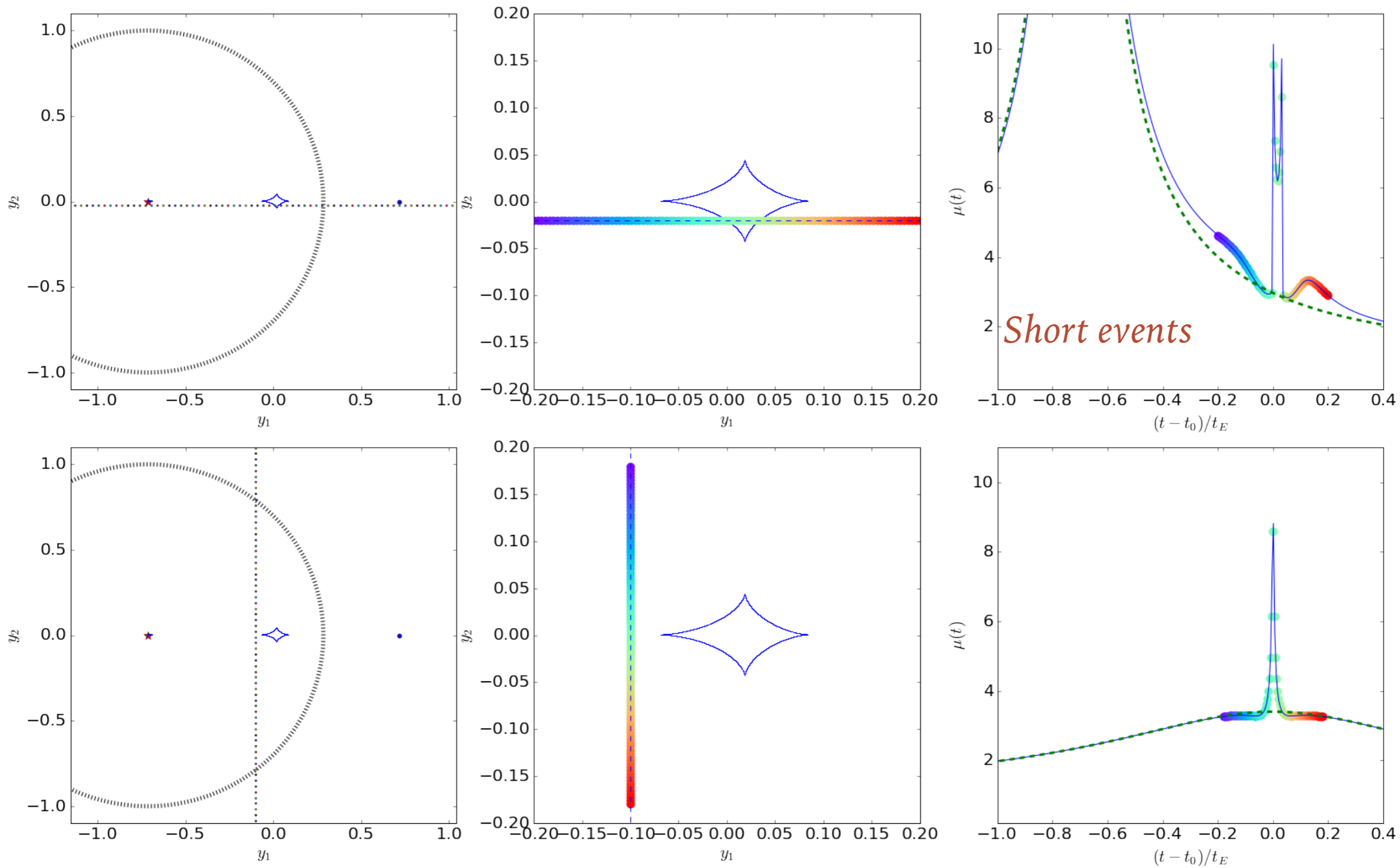
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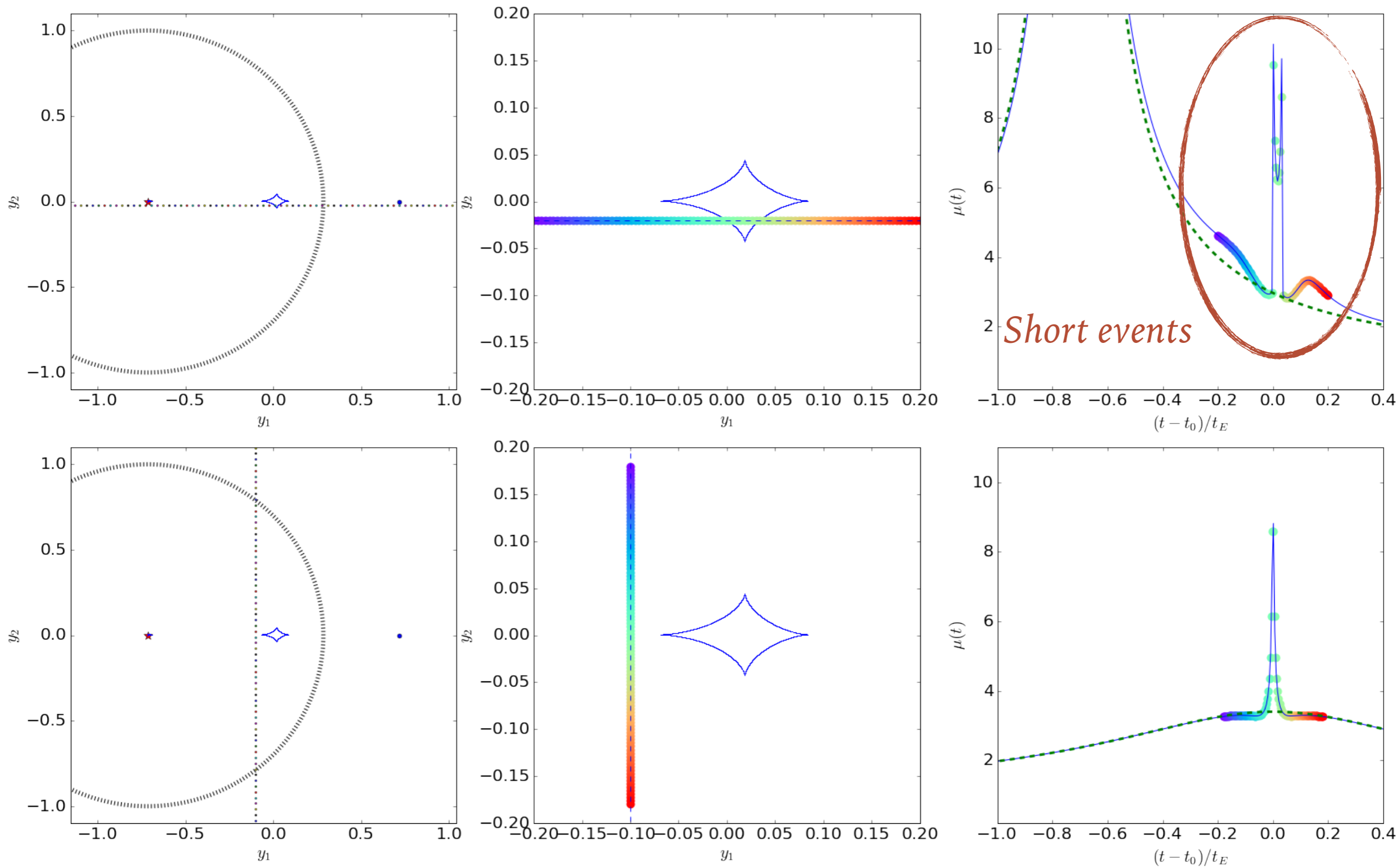
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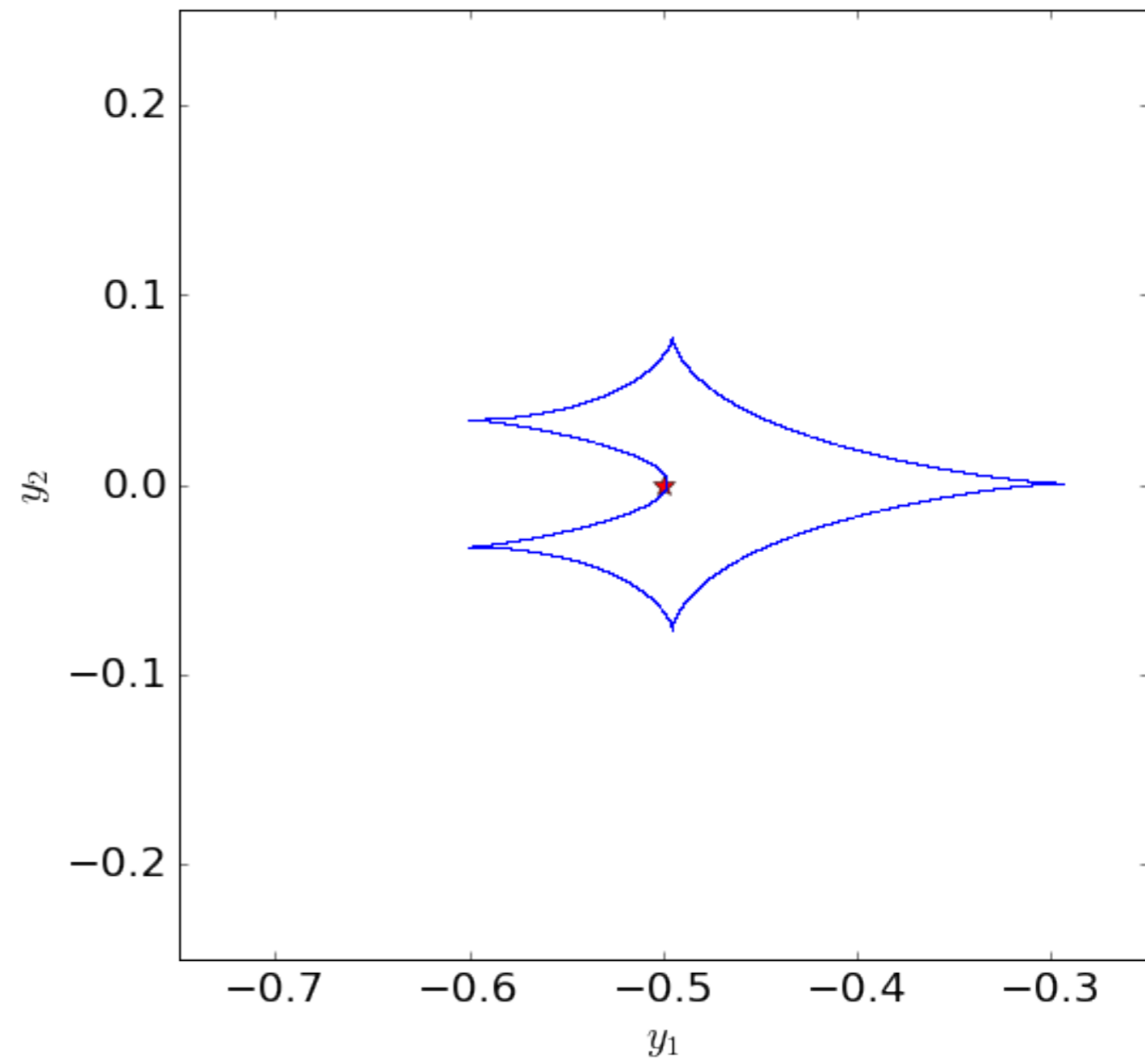
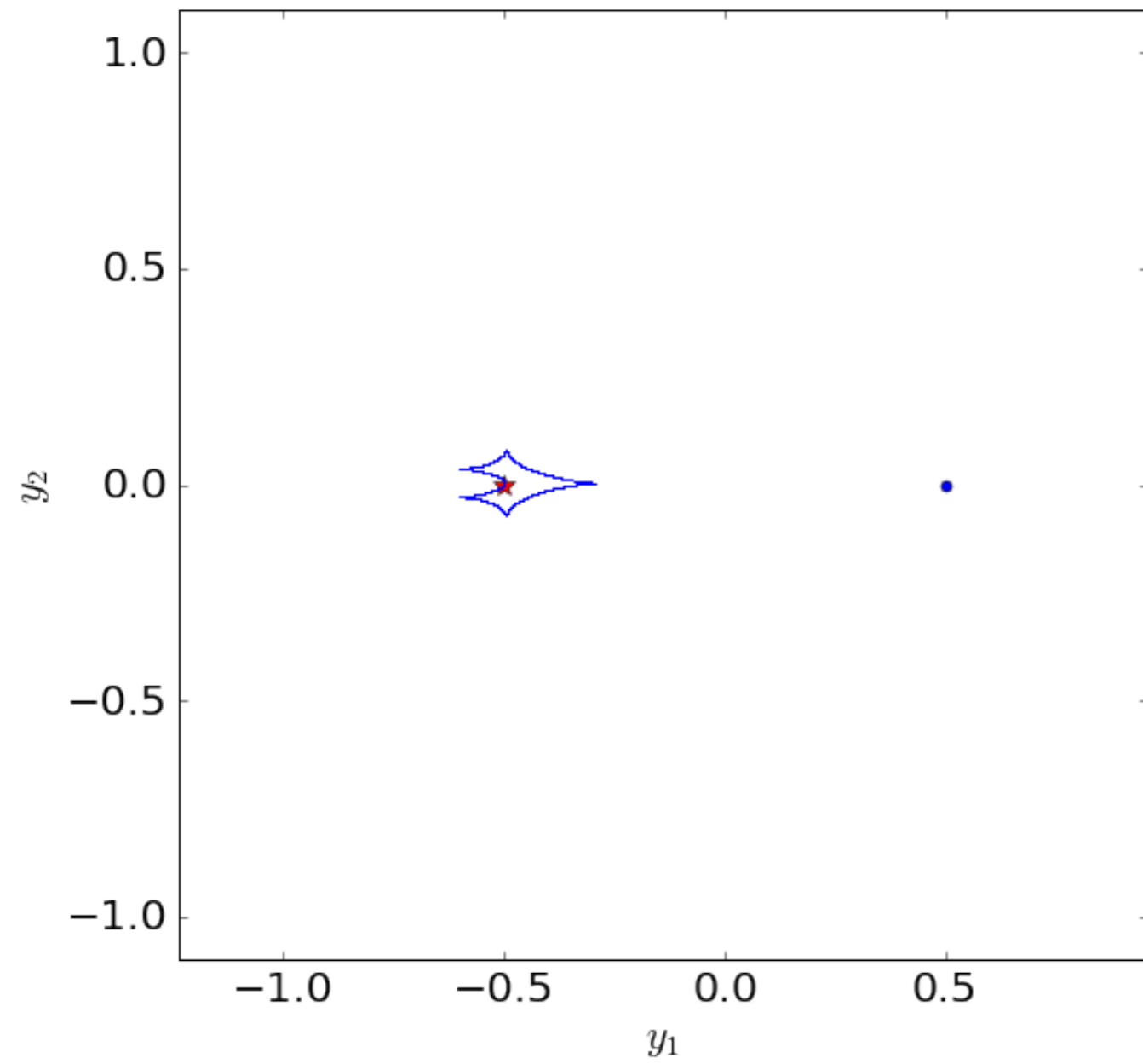


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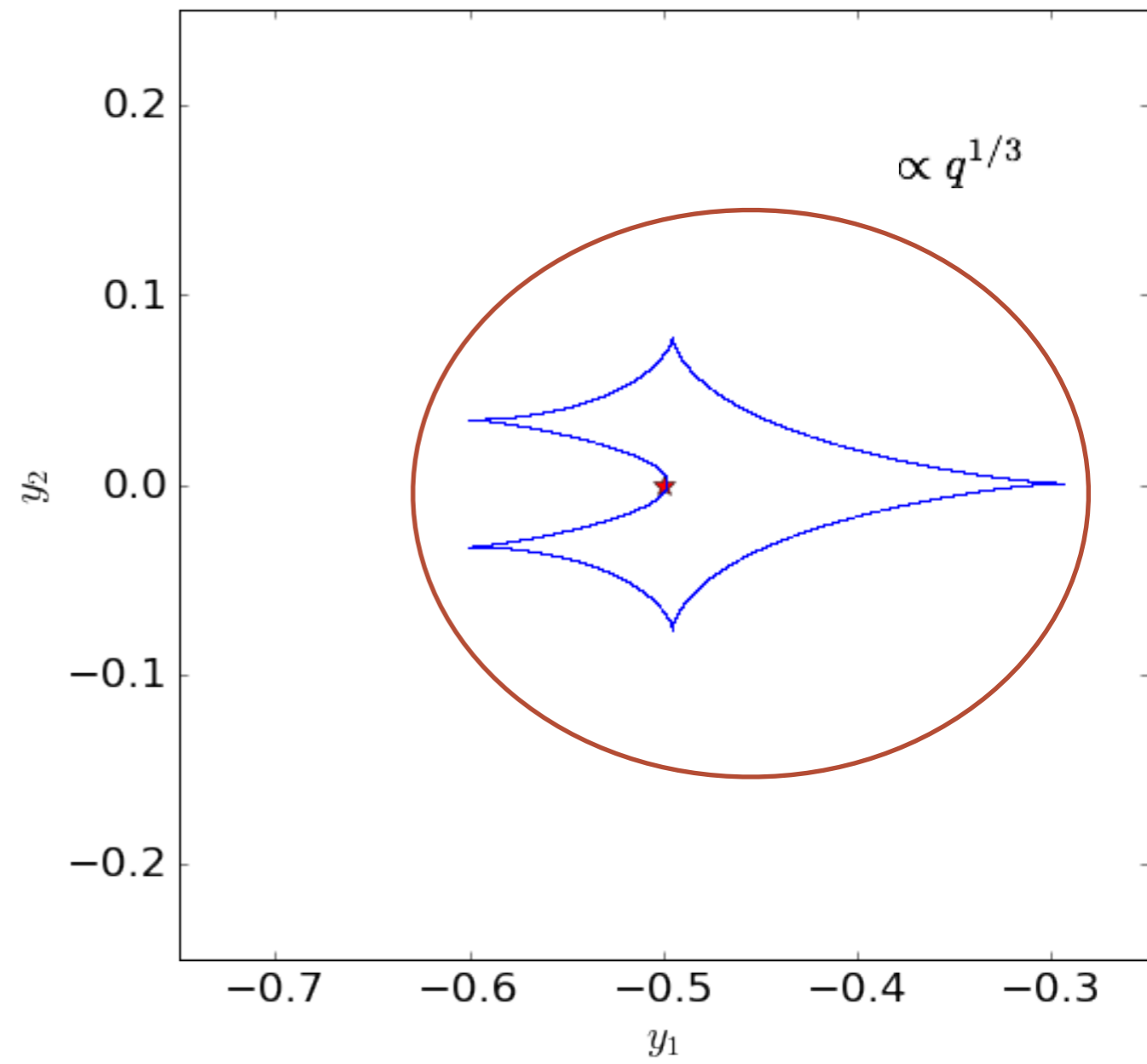
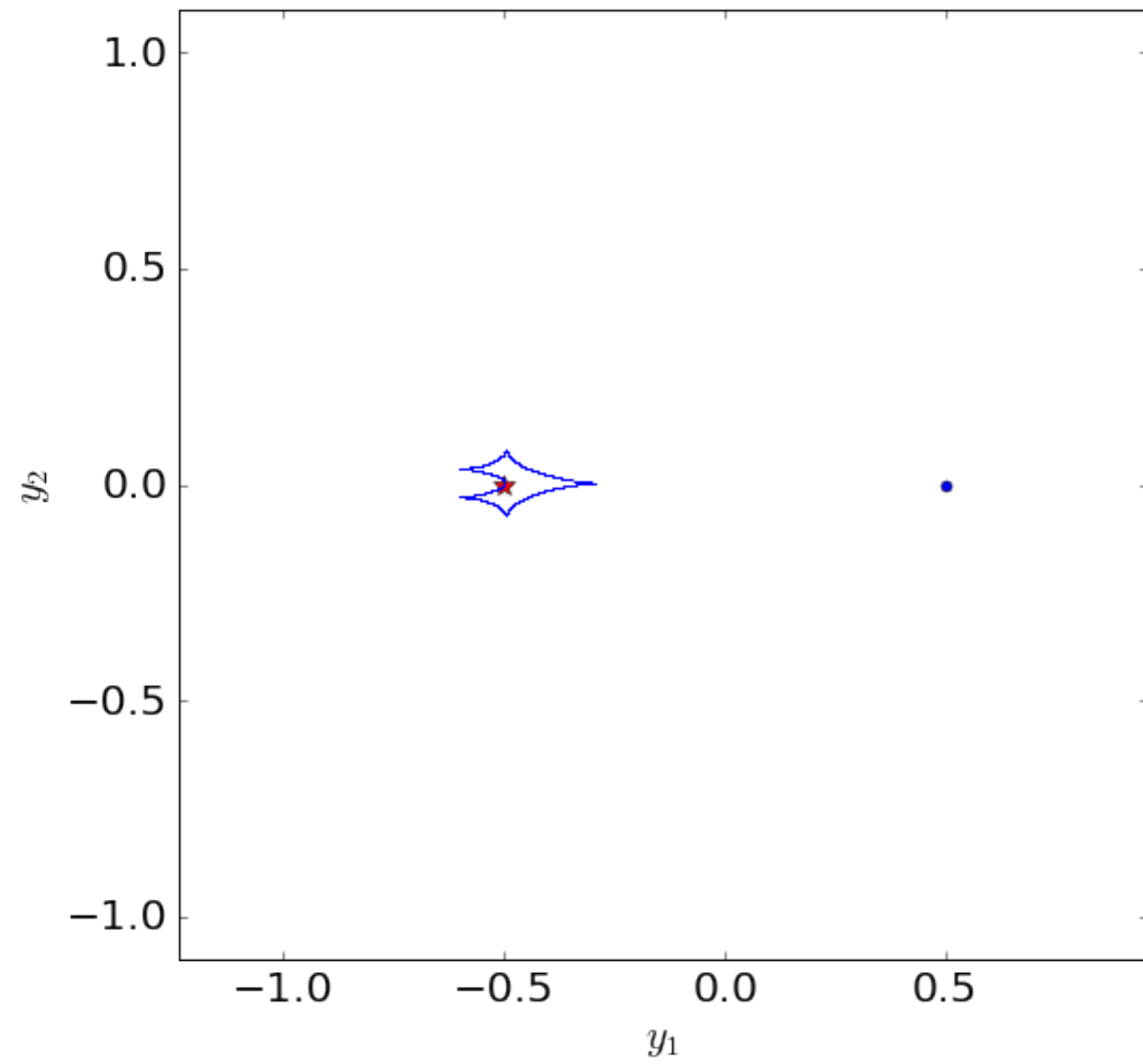
# PLANETARY CAUSTICS IN INTERMEDIATE TOPOLOGIES

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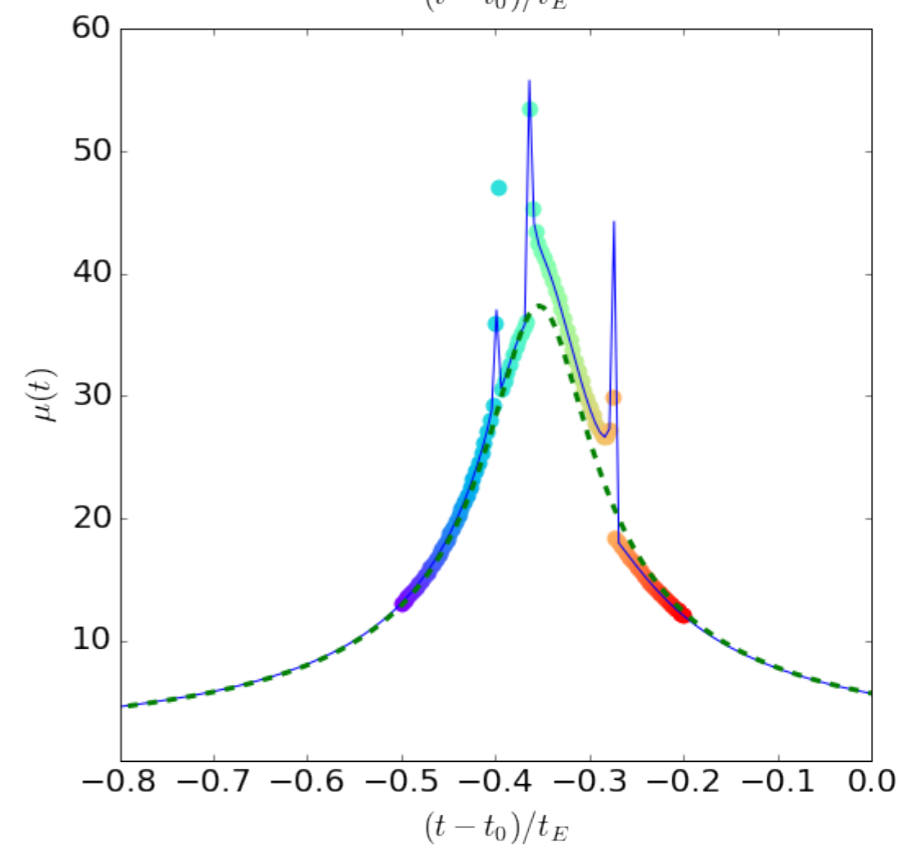
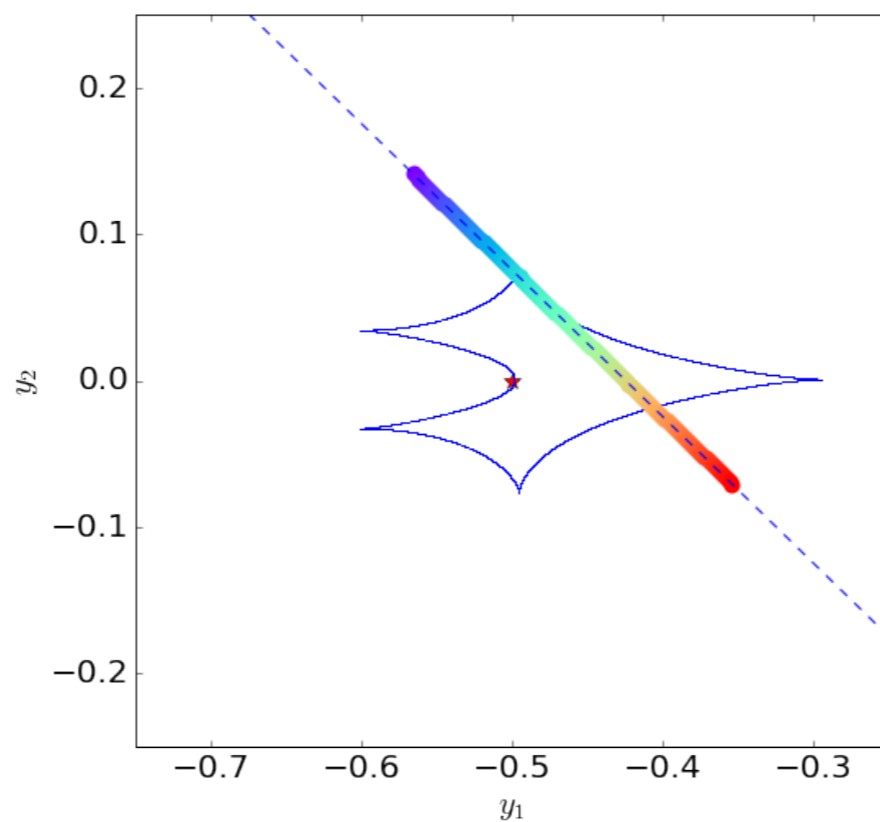
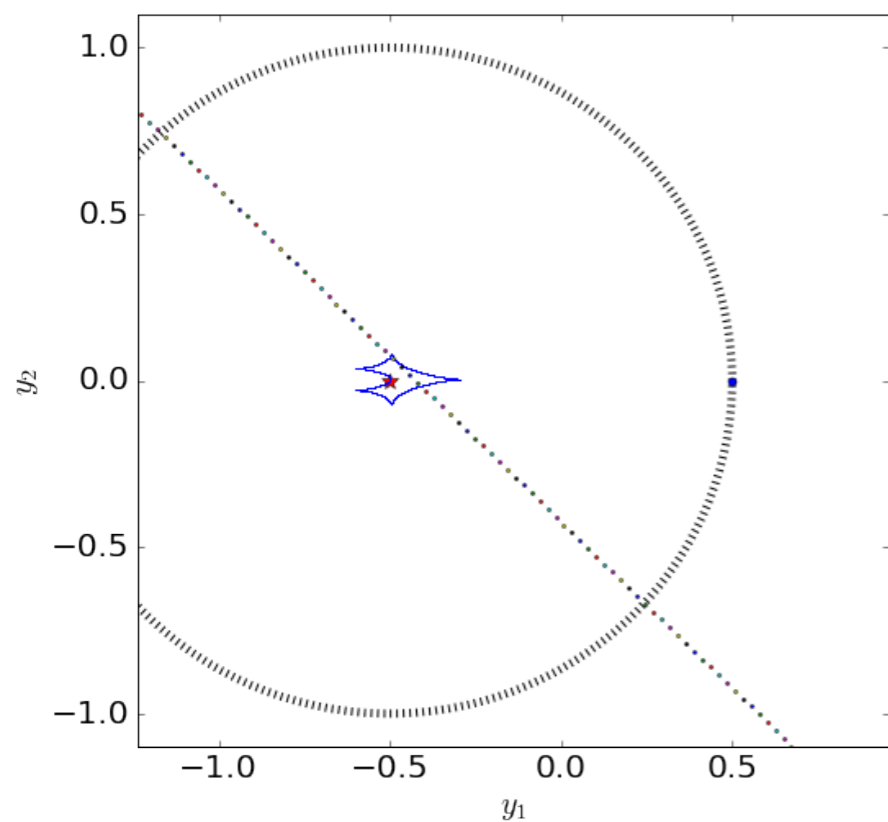
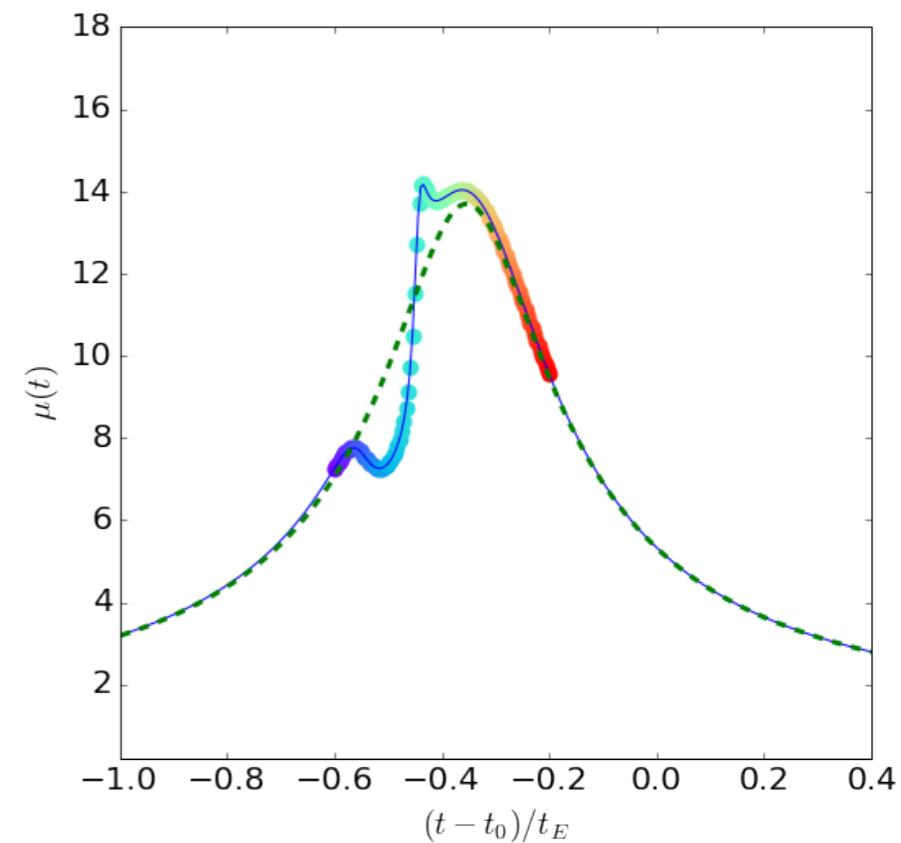
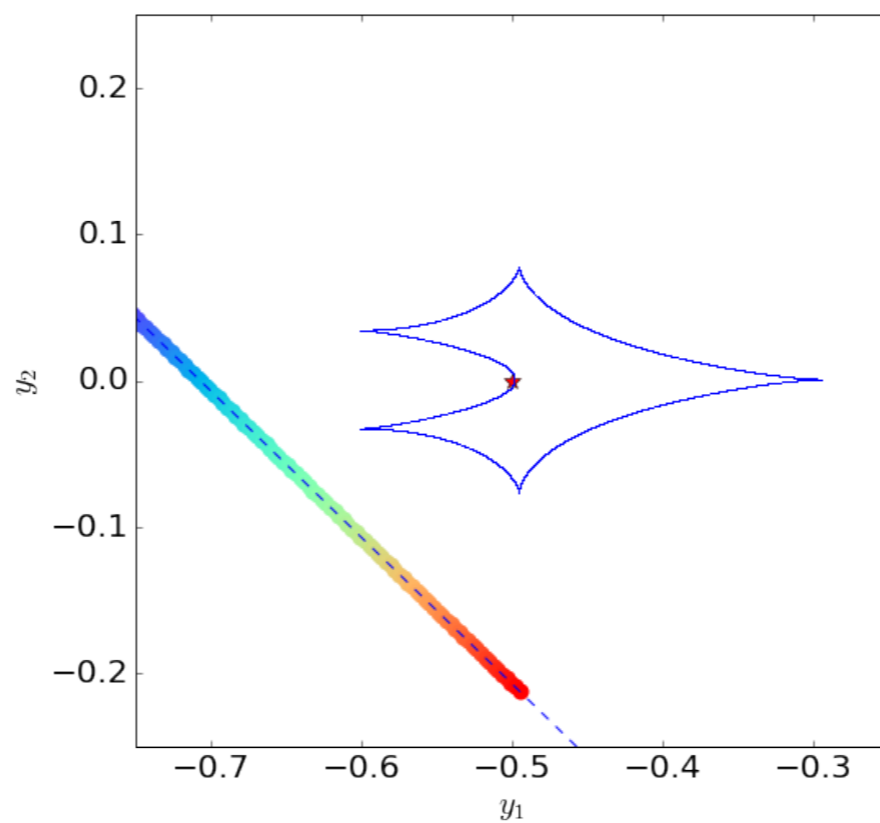
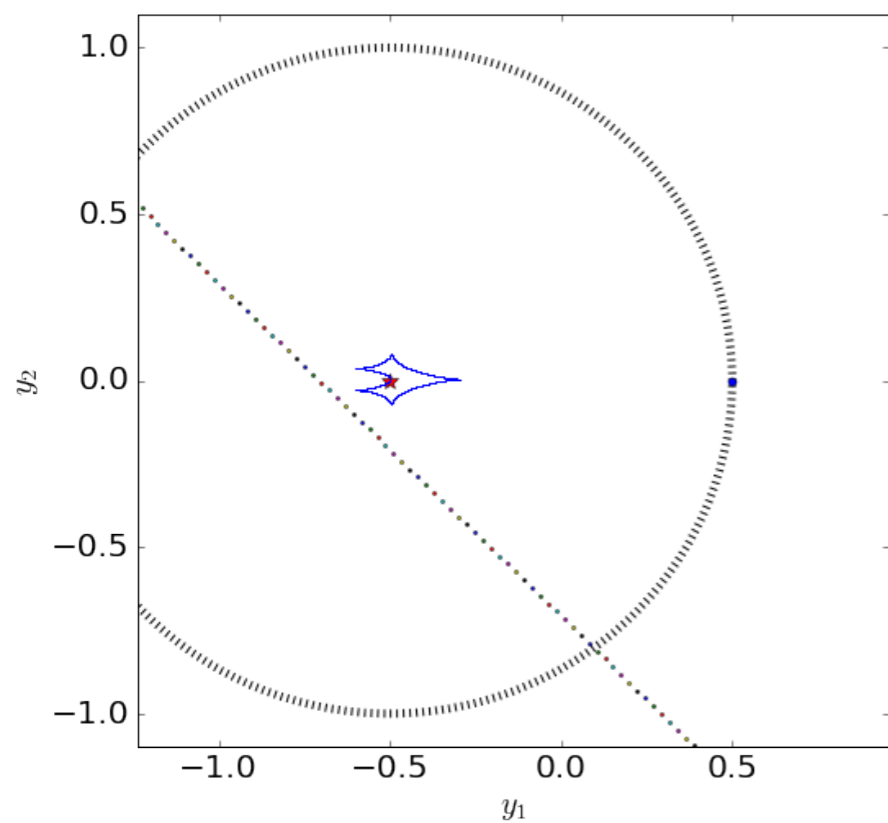
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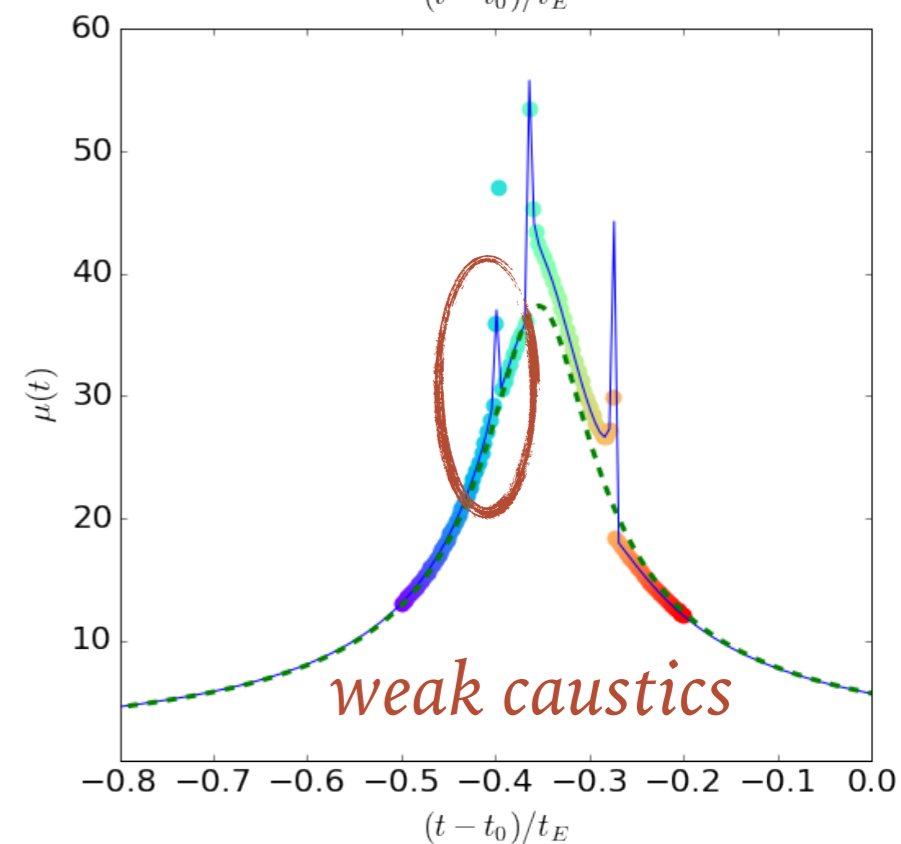
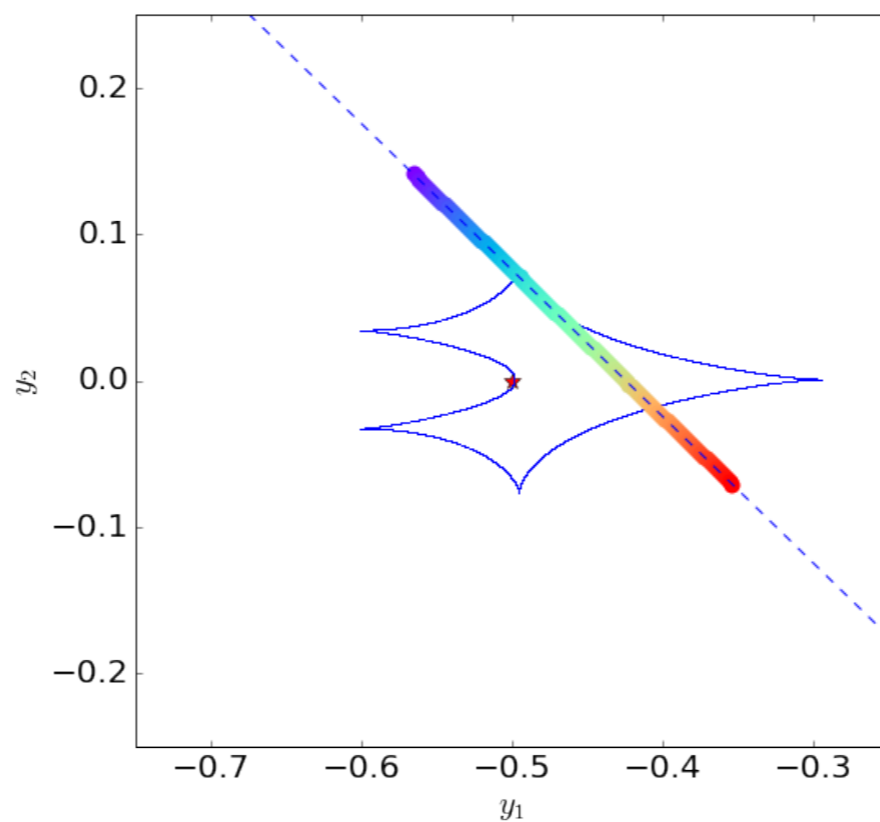
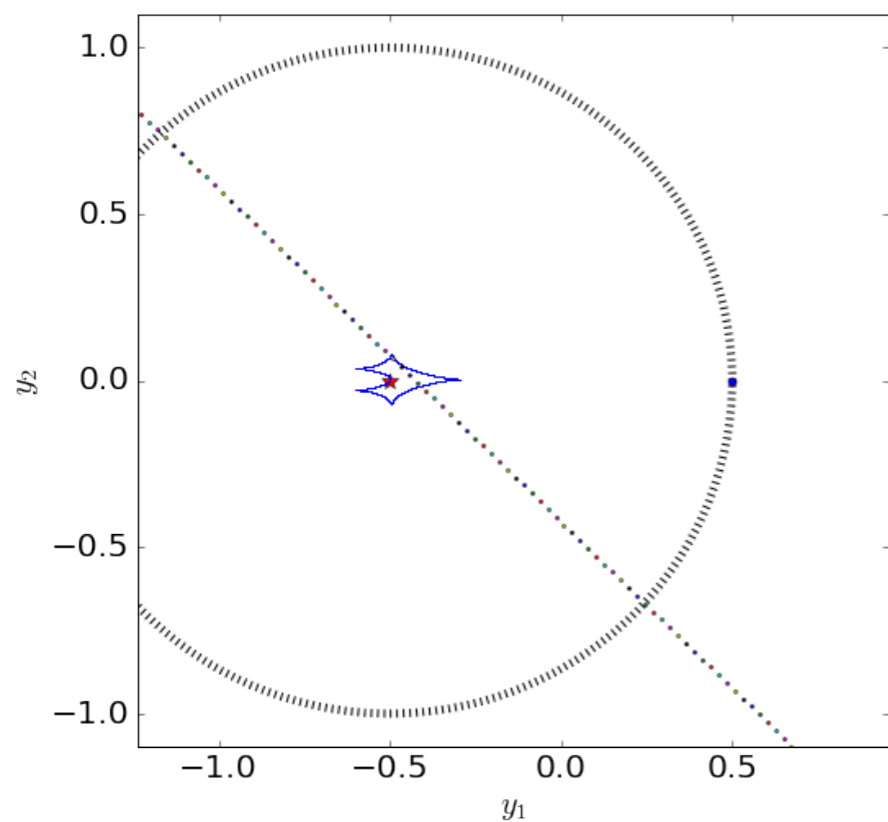
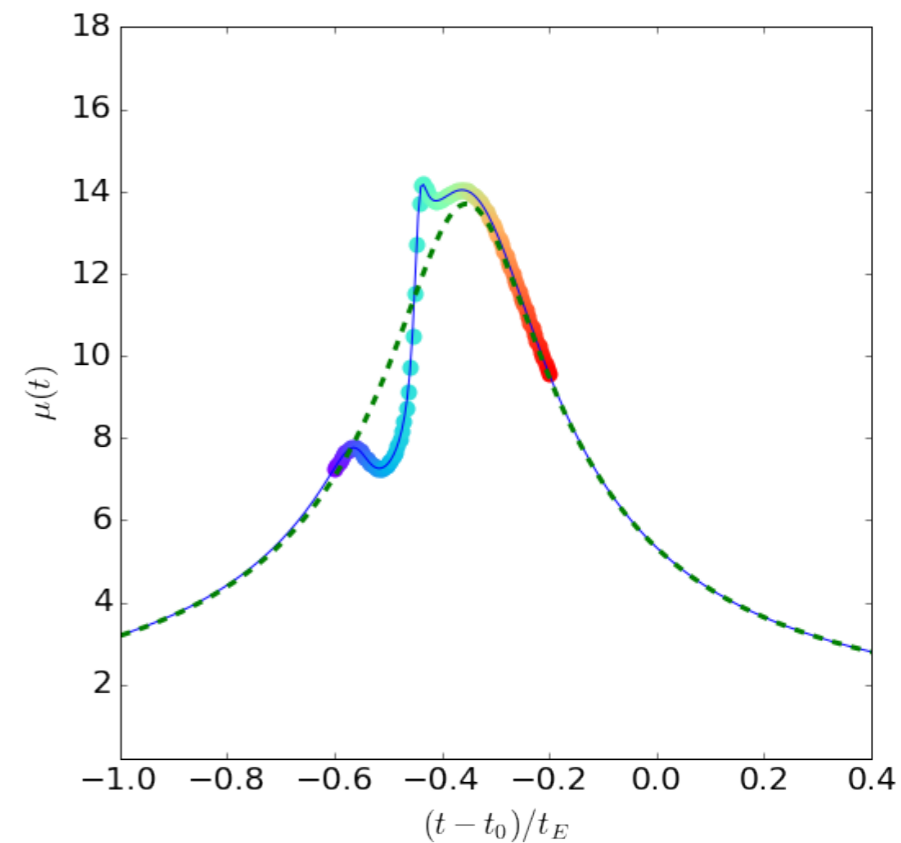
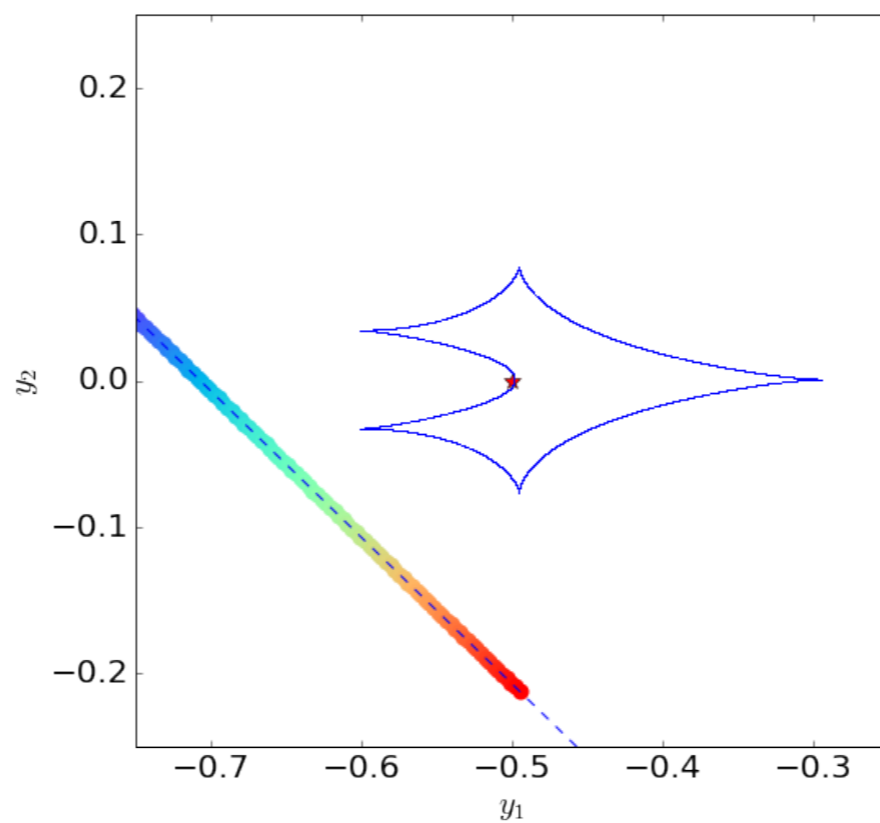
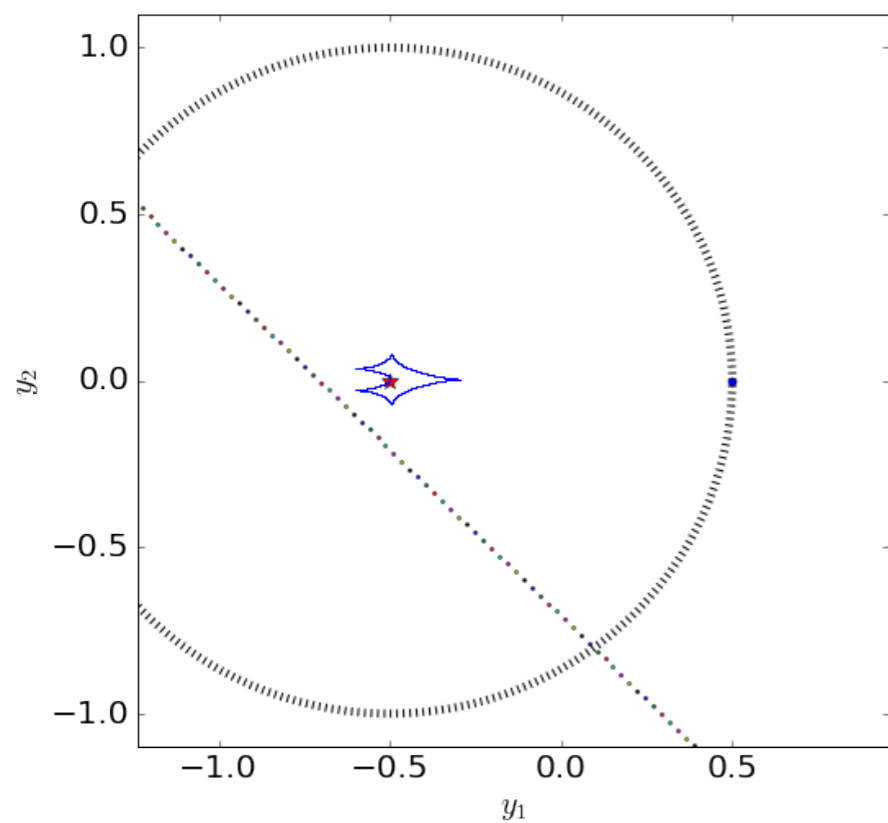




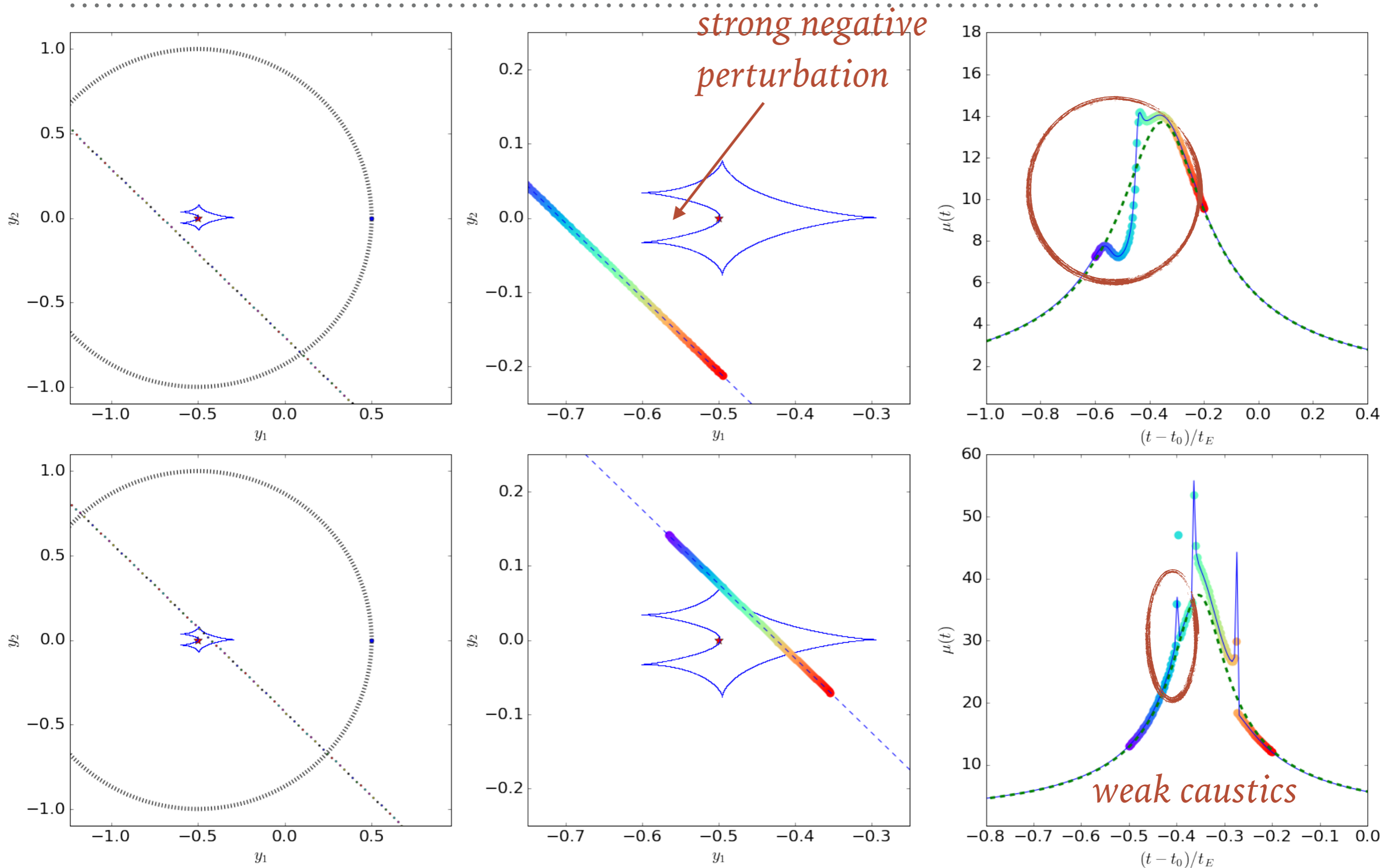
# PLANETARY CAUSTICS PERTURBATIONS IN INTERMEDIATE TOPOLOGIES



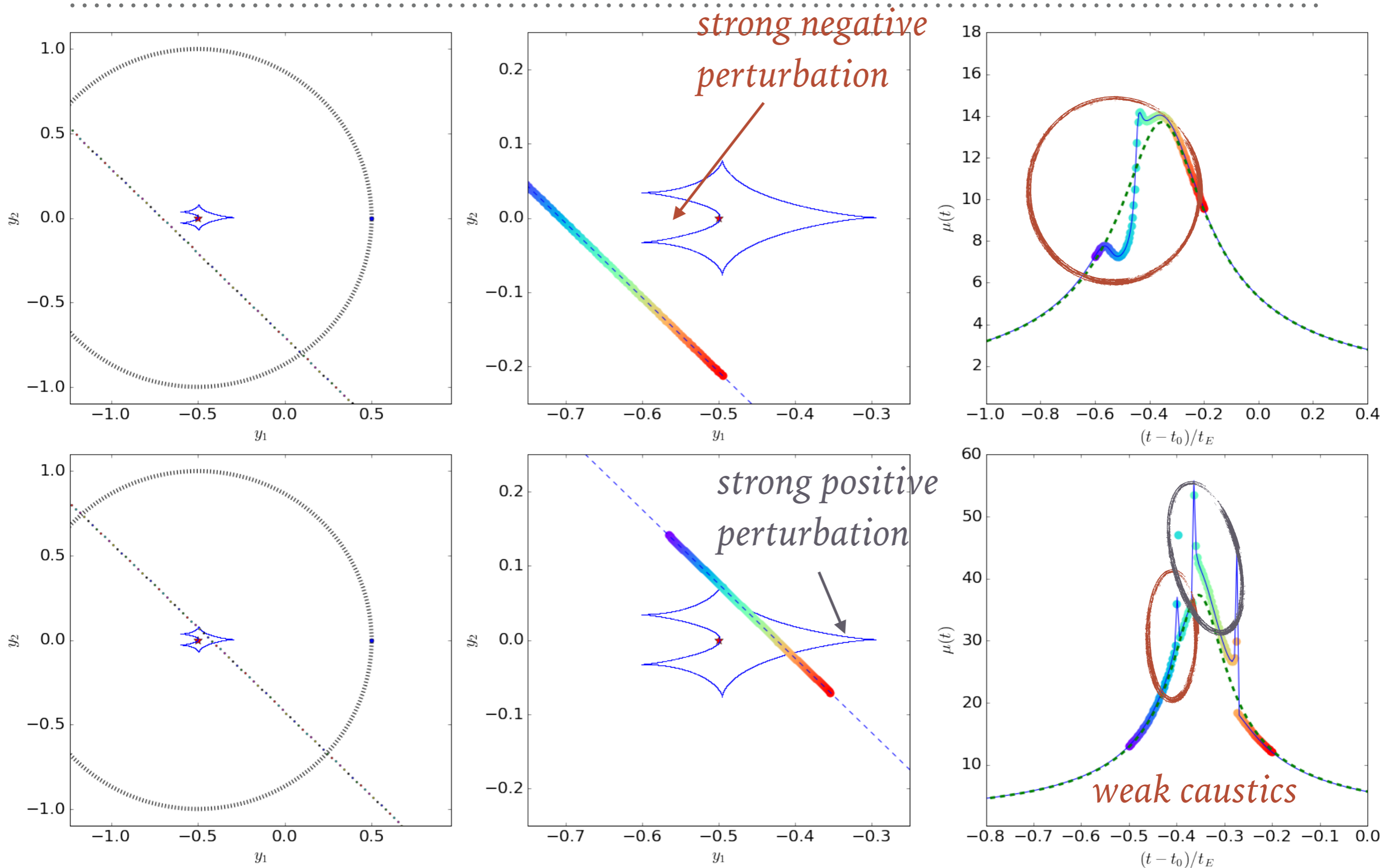
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# TO SUMMARIZE

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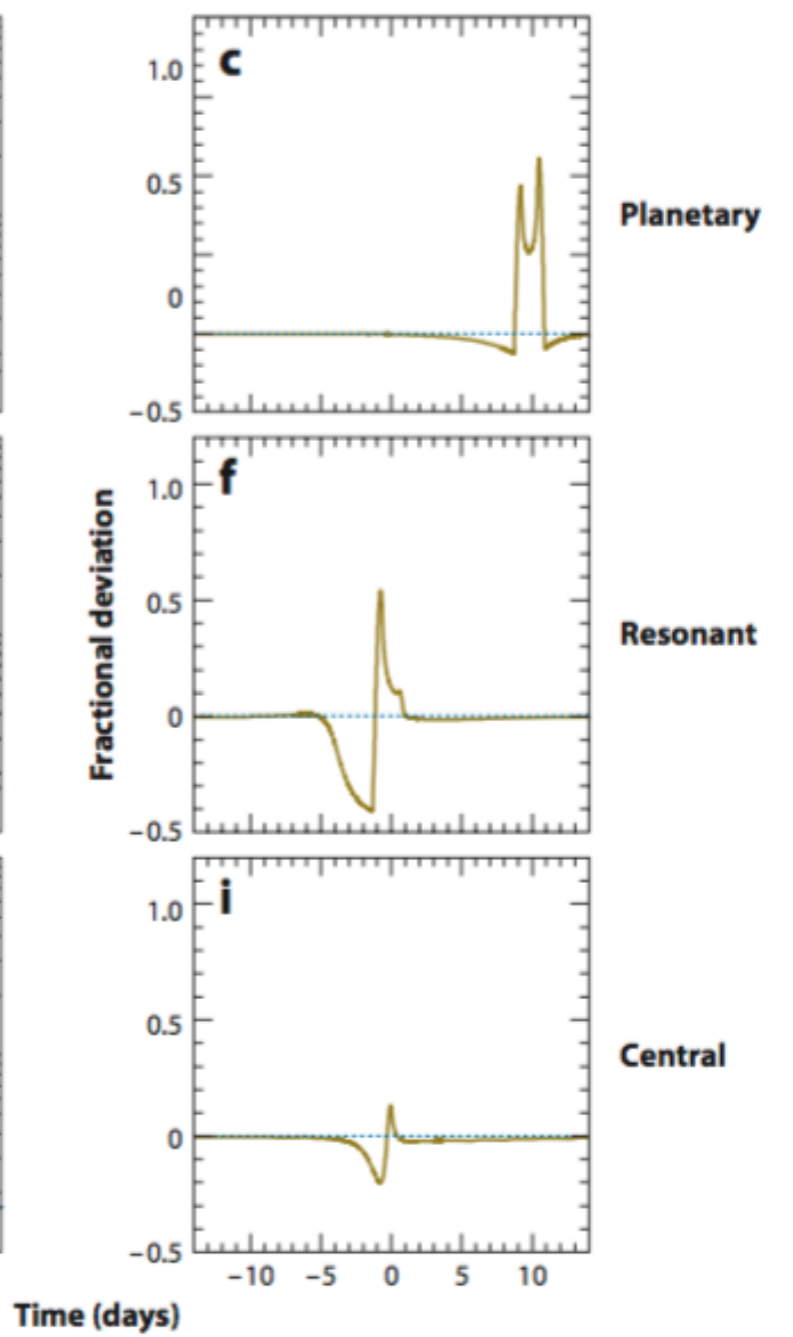
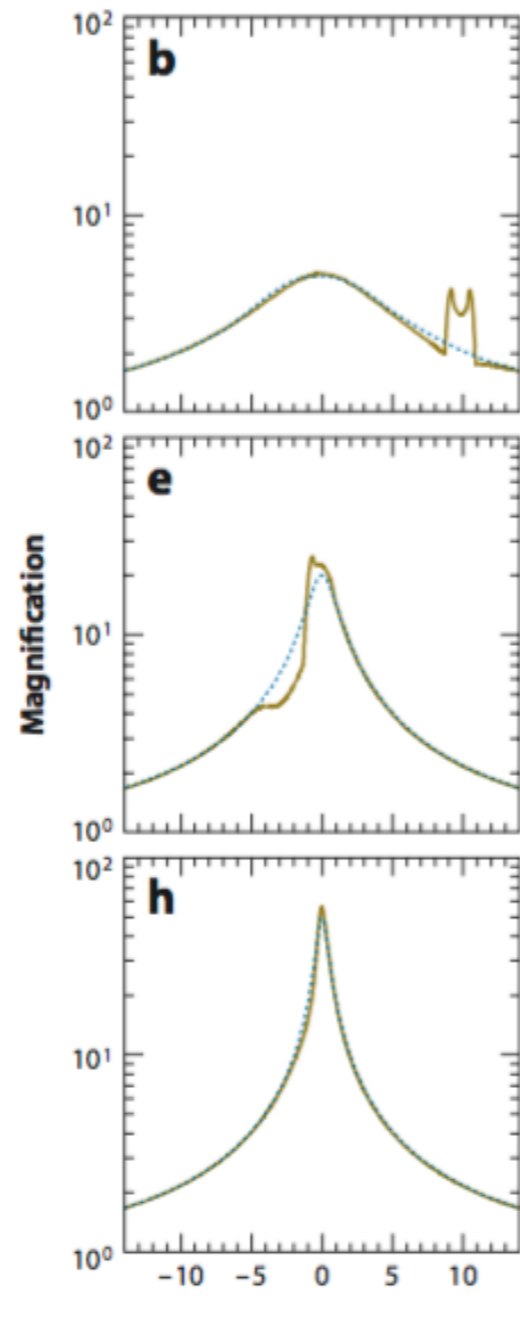
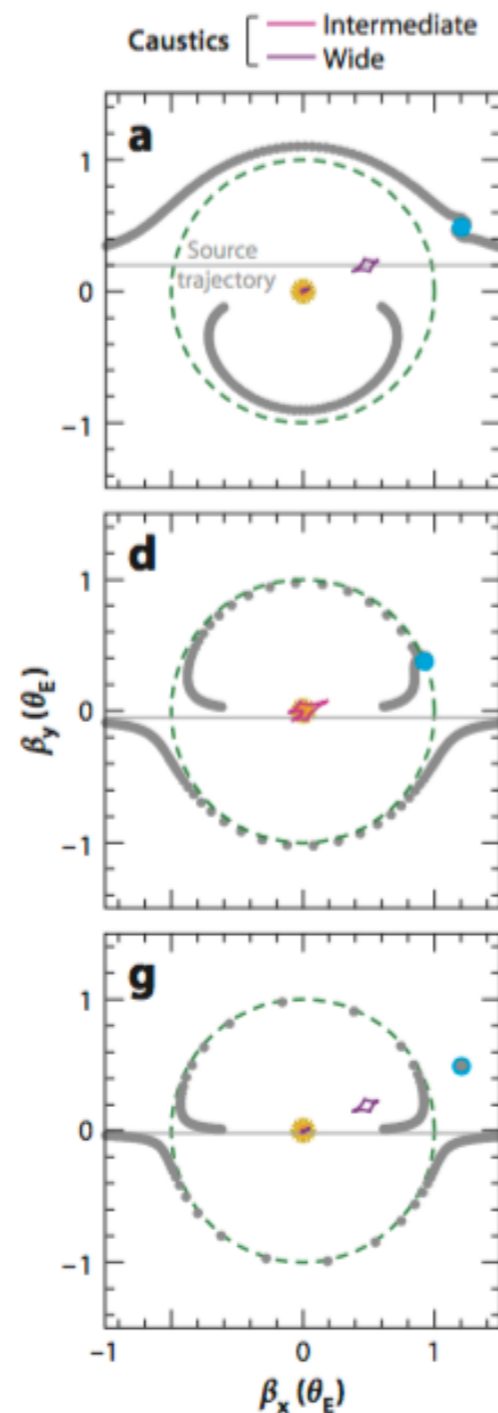
- different caustic topologies give rise to different kind of perturbations on the light curves
- planets can be detected in only a few qualitatively different ways:
  - at relatively low magnification of the primary, if the source crosses the planetary caustics from close or wide planets
  - near the peak of the light curve, if the source has a small impact parameter, in both cases of wide and close planets
  - at modest to high-magnification, through the perturbations from the resonant caustic.
  - in the case of free-floating planets, as single, short time-scale events.

# OF COURSE...

- there is also an astrometric perturbation...

*The planet can be detected when it perturbs one of the two images of the source!*

*This tells us that microlensing is sensitive to planets at distances of the order of the star Einstein radius.*



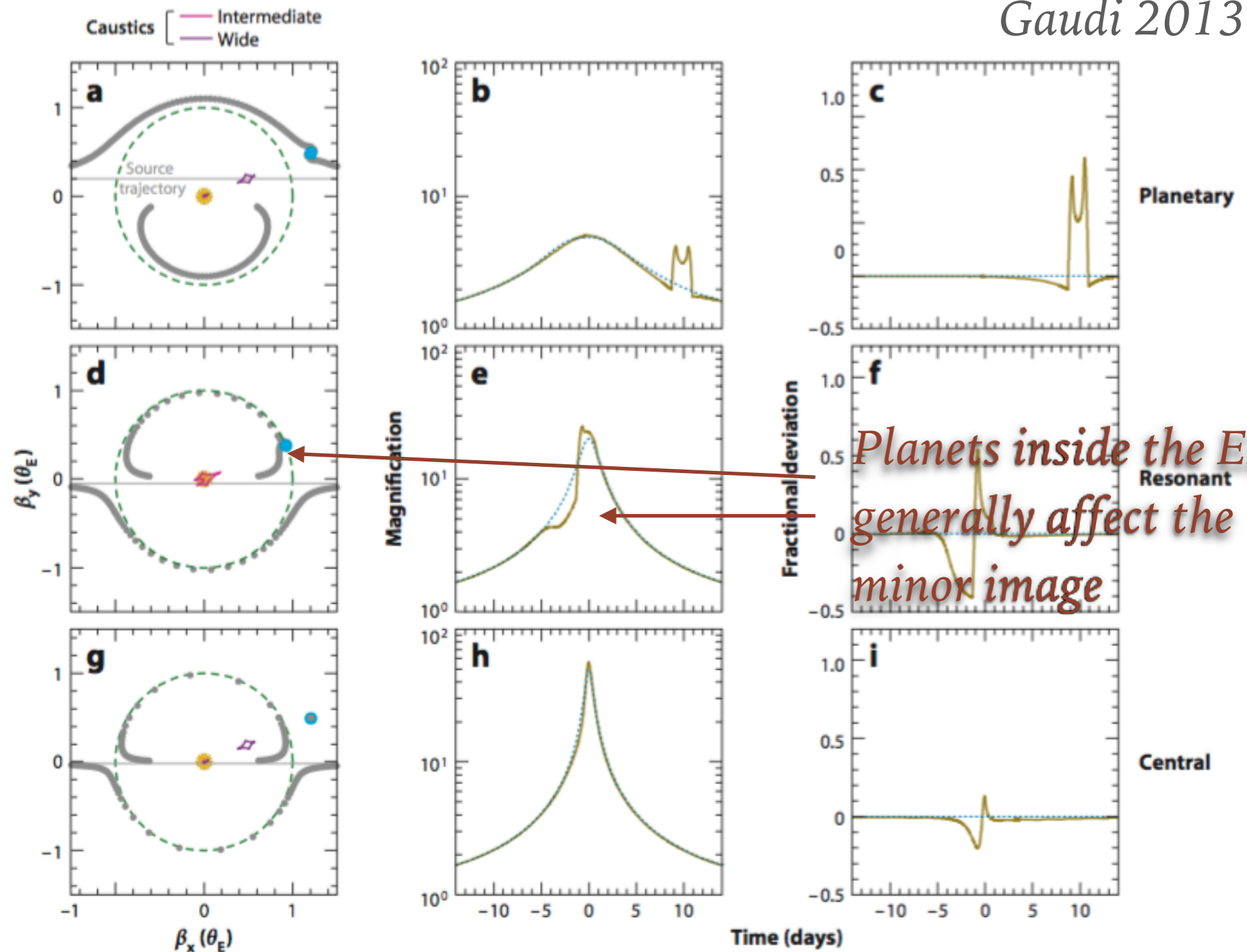
*Gaudi 2013*

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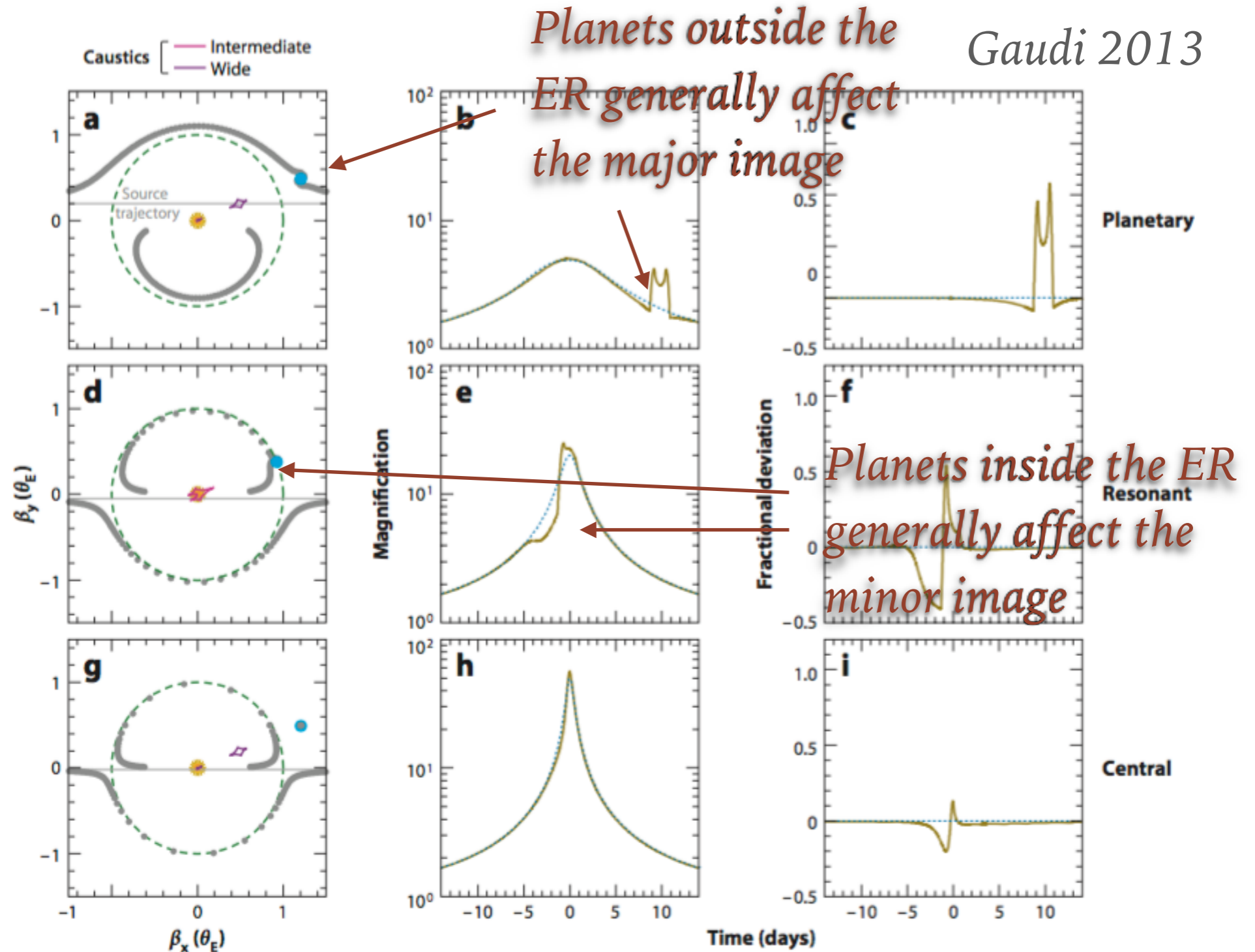


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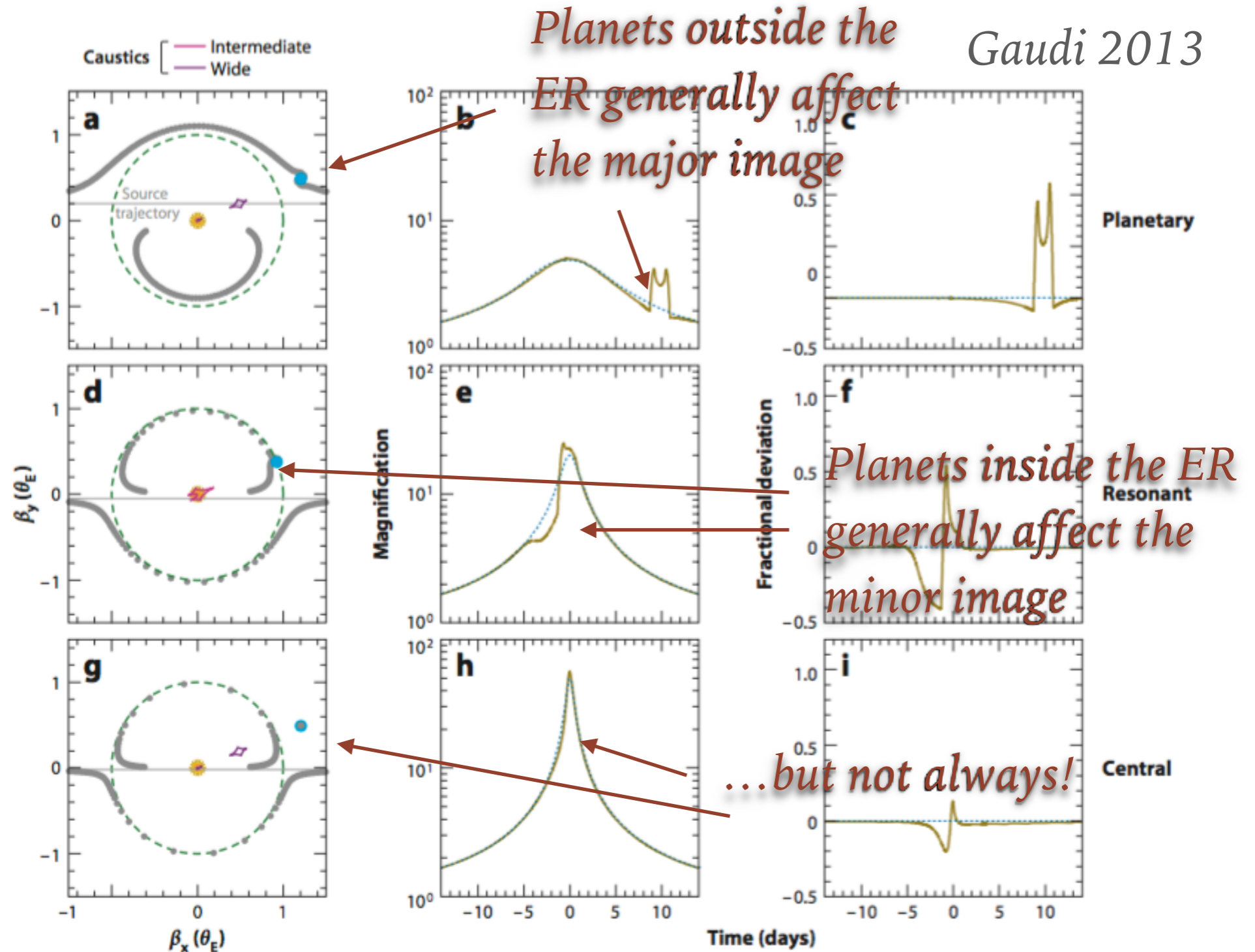


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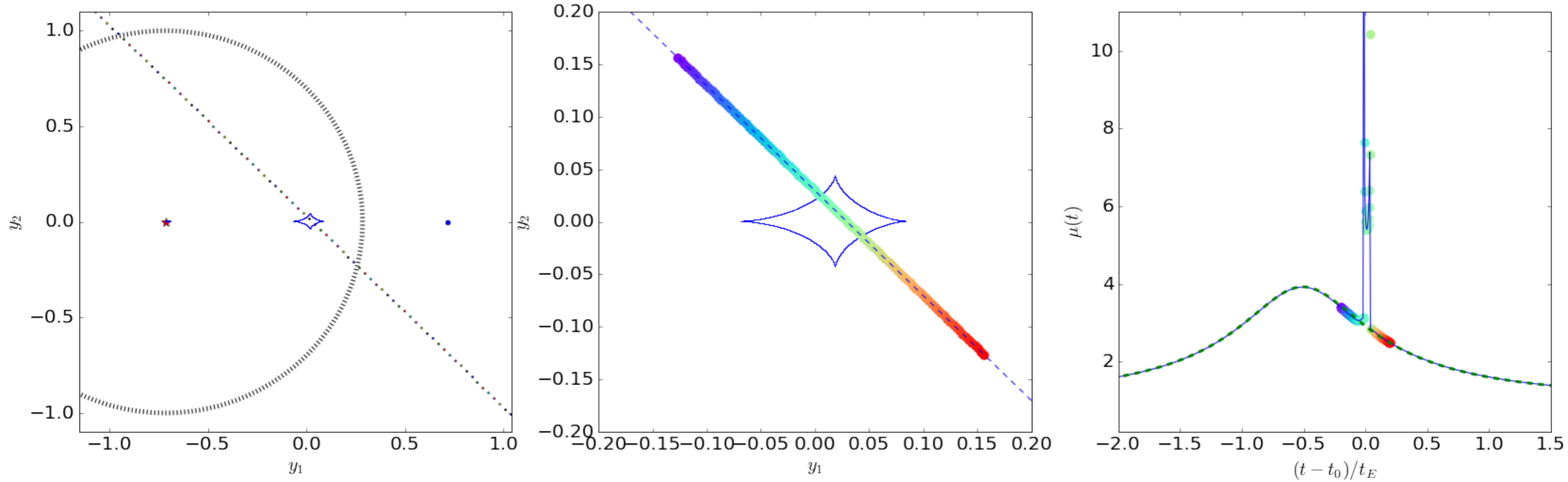
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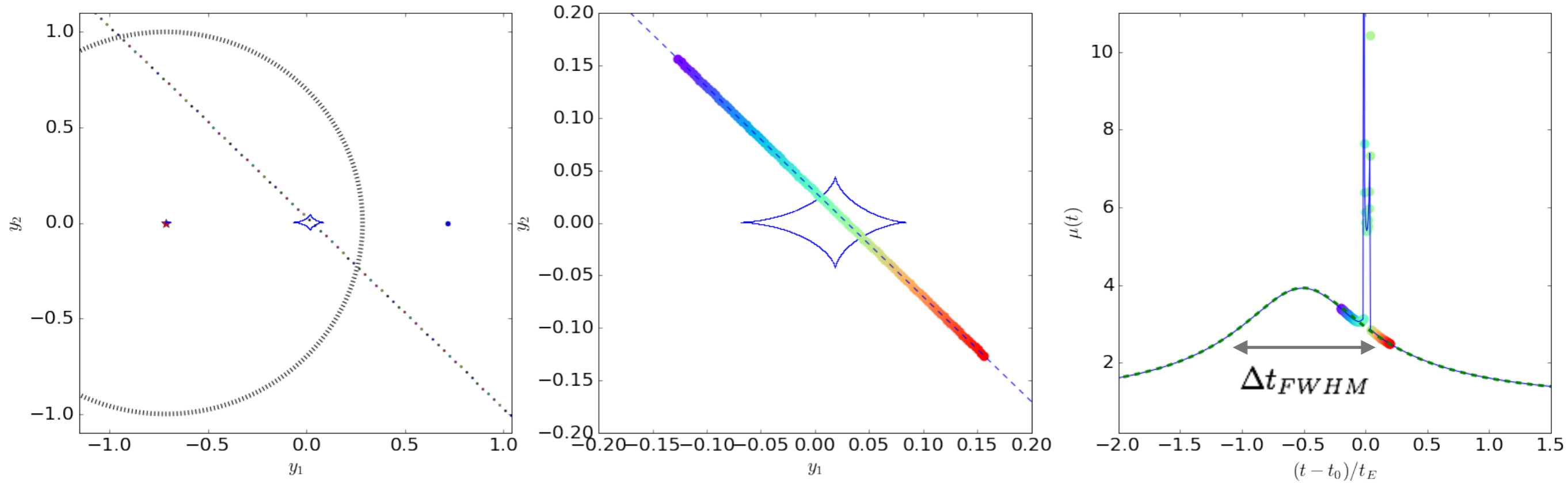


# PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



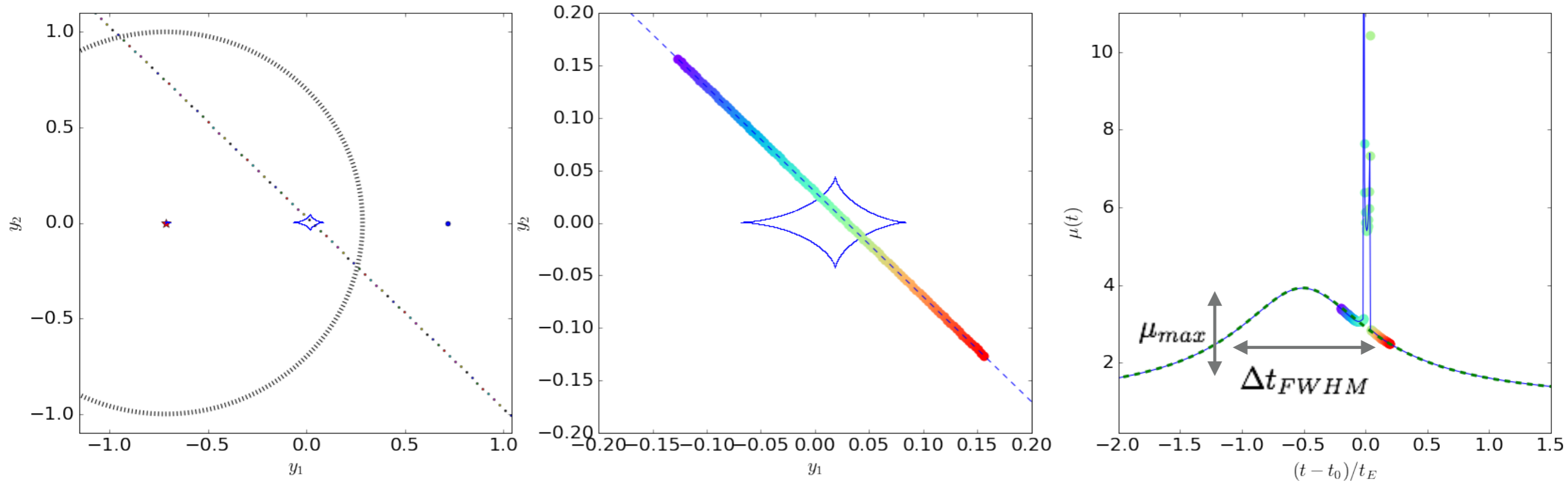
- primary event:
- planetary perturbation:

# PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



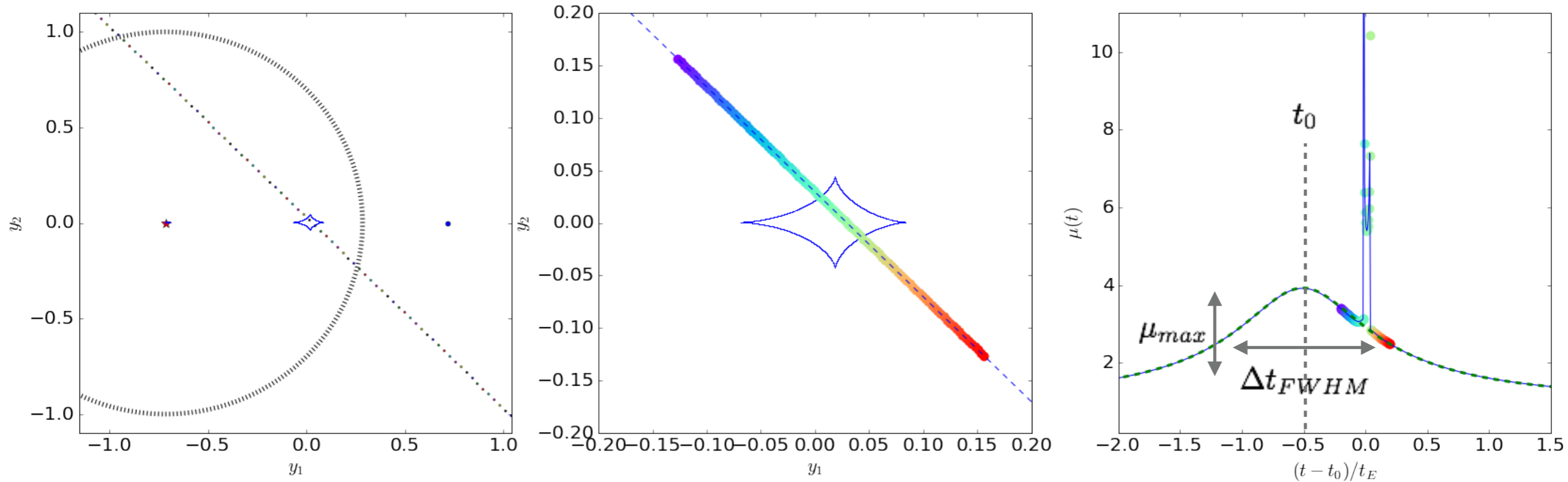
- primary event:  $\Delta t_{FWHM}$
- planetary perturbation:

# PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



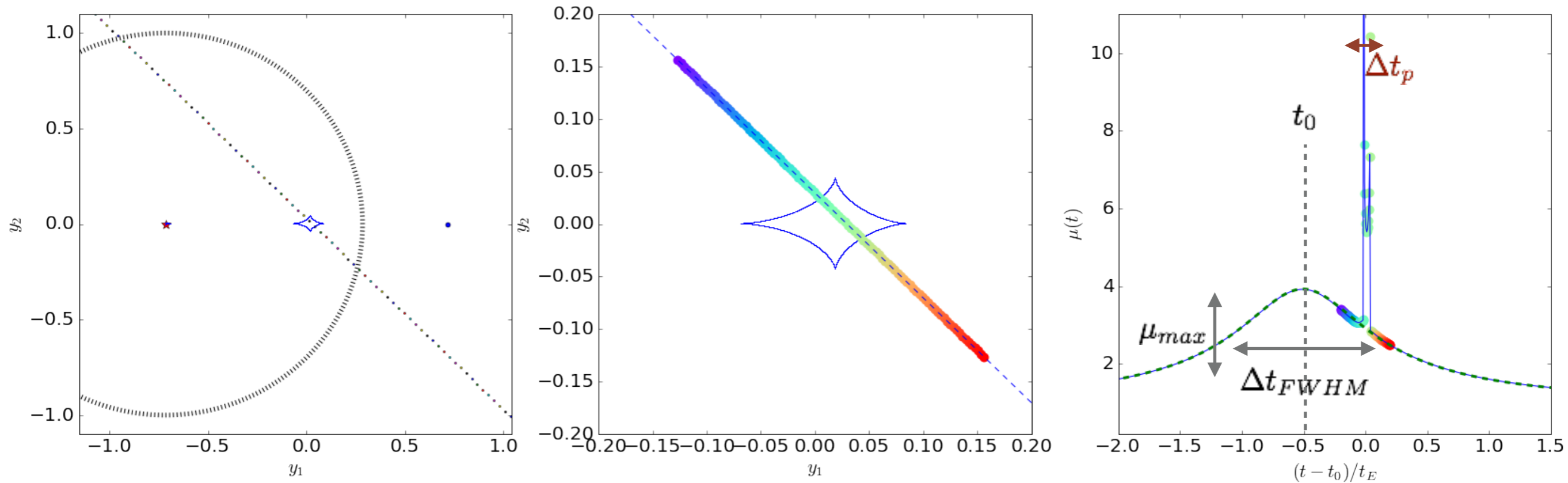
- primary event:  $\Delta t_{FWHM}$   $\mu_{max}$
- planetary perturbation:

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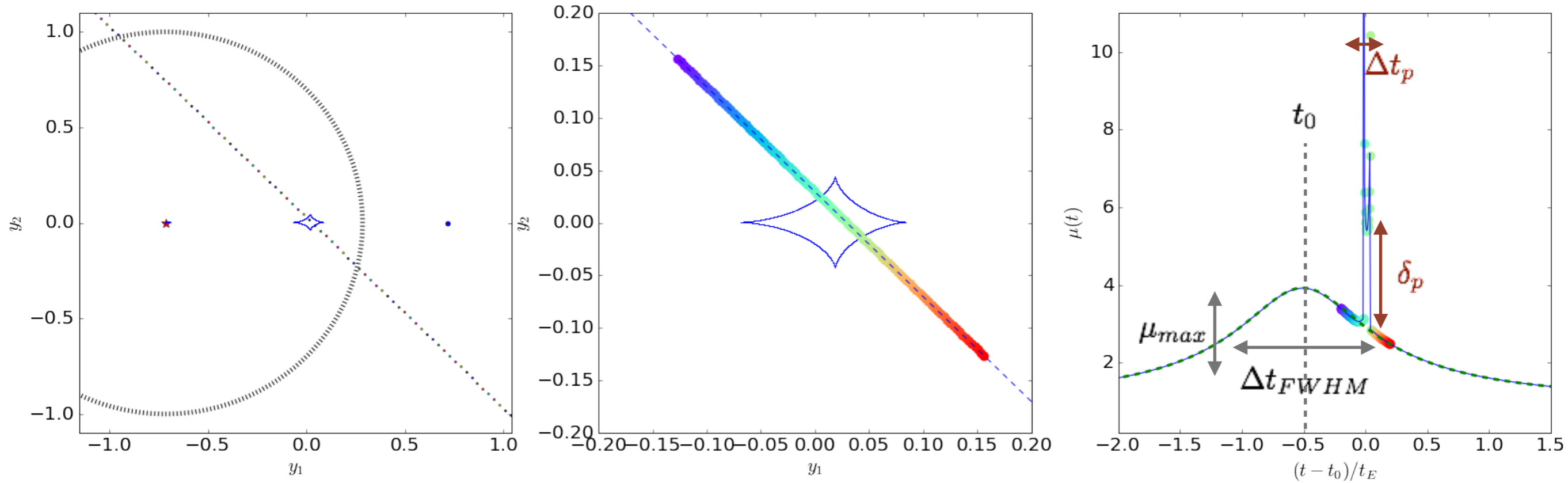
- primary event:  $\Delta t_{FWHM}$   $\mu_{max}$   $t_0$
- planetary perturbation:

# PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



- primary event:  $\Delta t_{FWHM}$   $\mu_{max}$   $t_0$
- planetary perturbation:  $\Delta t_p$

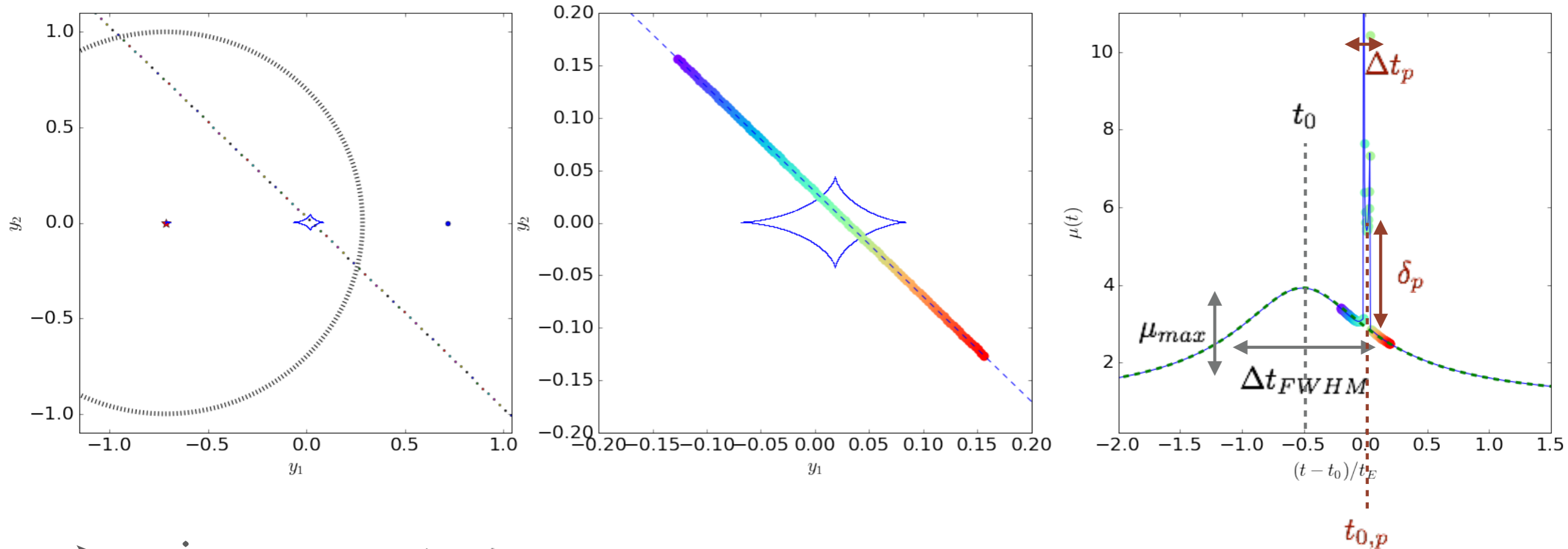
# PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



➤ primary event:  $\Delta t_{FWHM}$   $\mu_{max}$   $t_0$

➤ planetary perturbation:  $\Delta t_p$   $\delta_p$

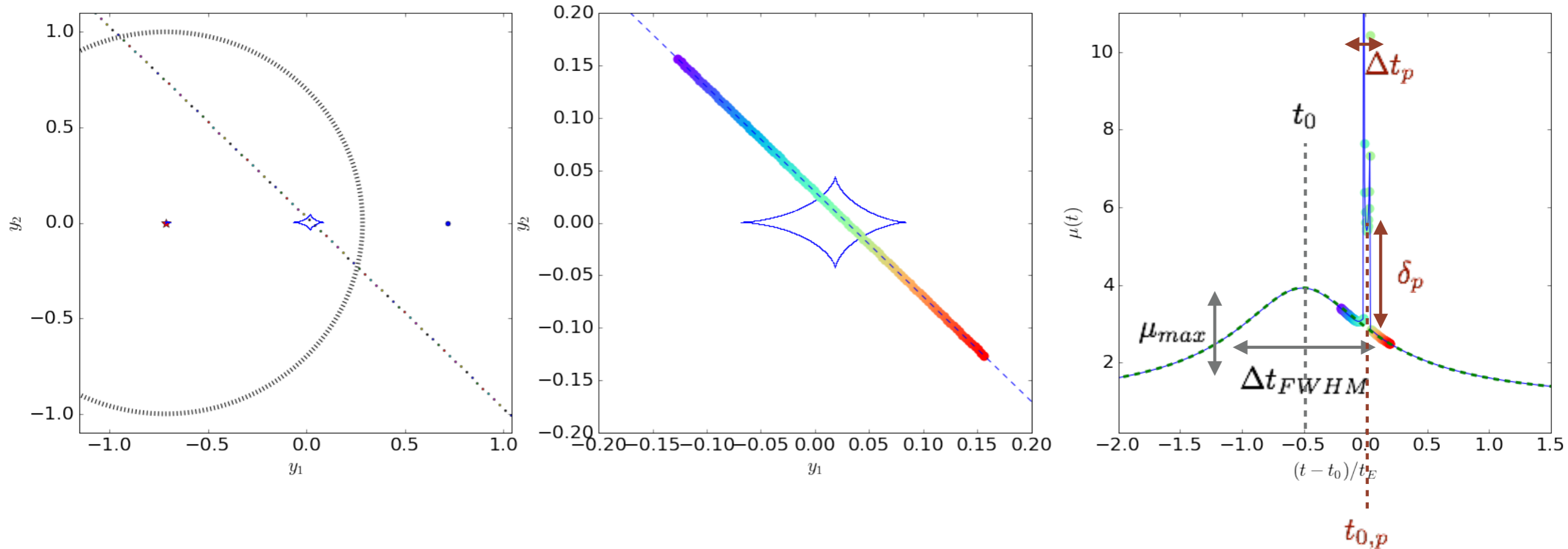
# PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



- primary event:  $\Delta t_{FWHM}$   $\mu_{max}$   $t_0$
- planetary perturbation:  $\Delta t_p$   $\delta_p$   $t_{0,p}$



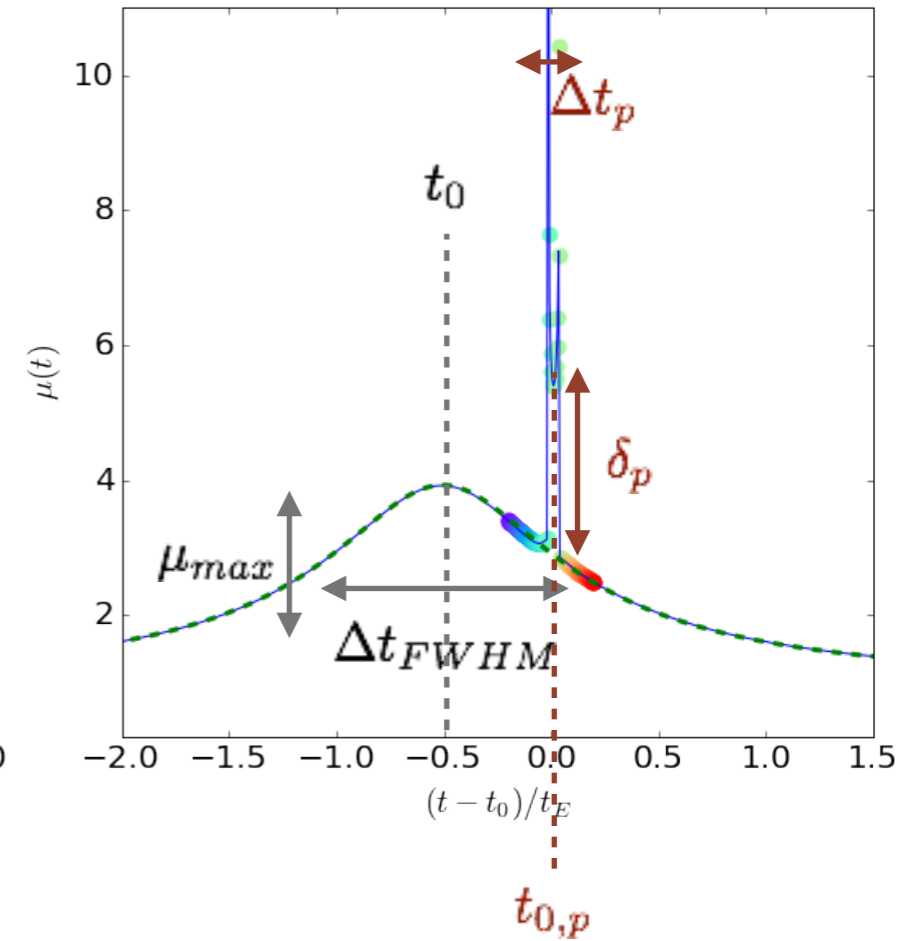
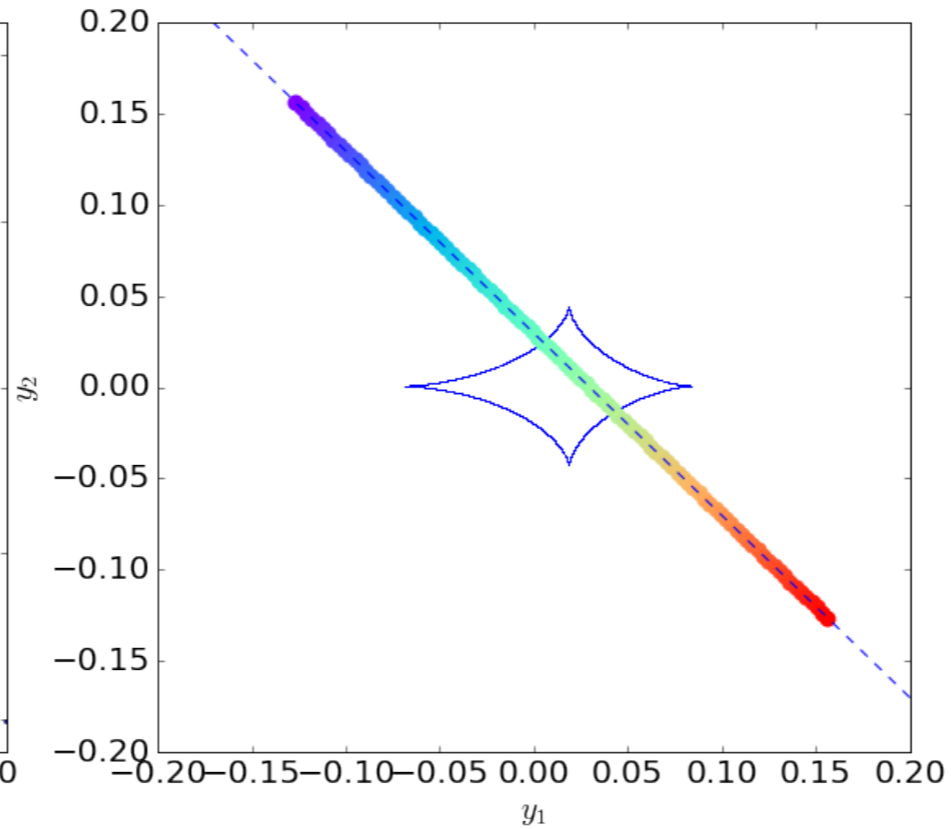
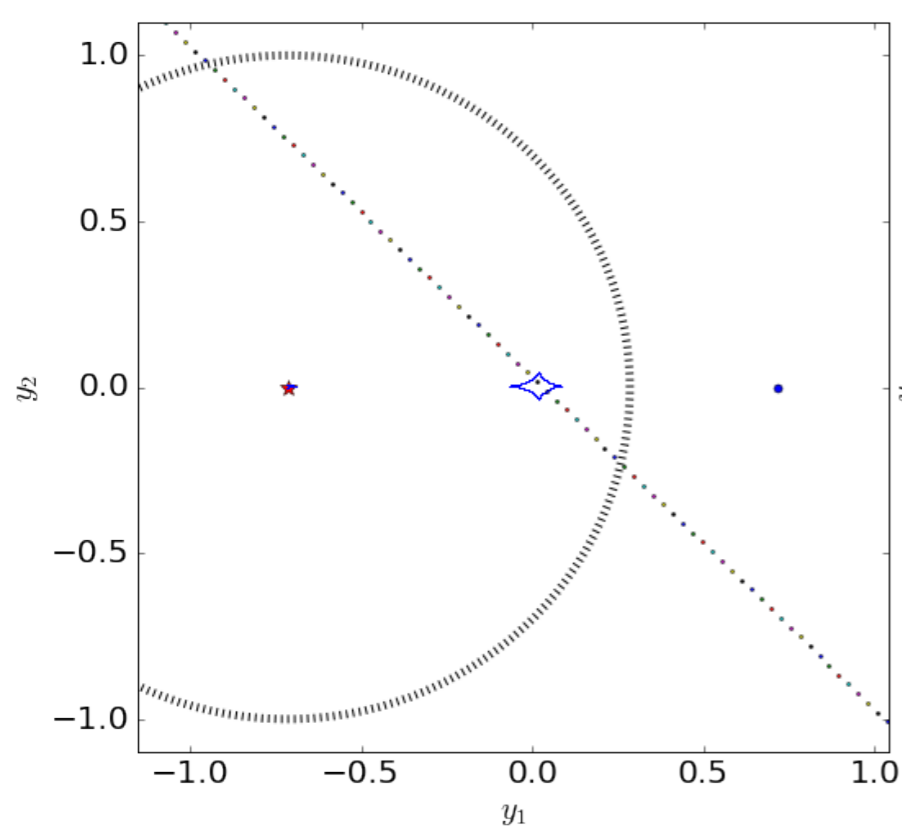
# PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



$$\Delta t_{FWHM}, \mu_{max}, t_0 \Rightarrow \mu(y) = \frac{y^2 + 2}{y\sqrt{y^2 + 4}} \quad y(t) = \sqrt{y_0^2 + \left(\frac{t - t_0}{t_E}\right)^2}$$

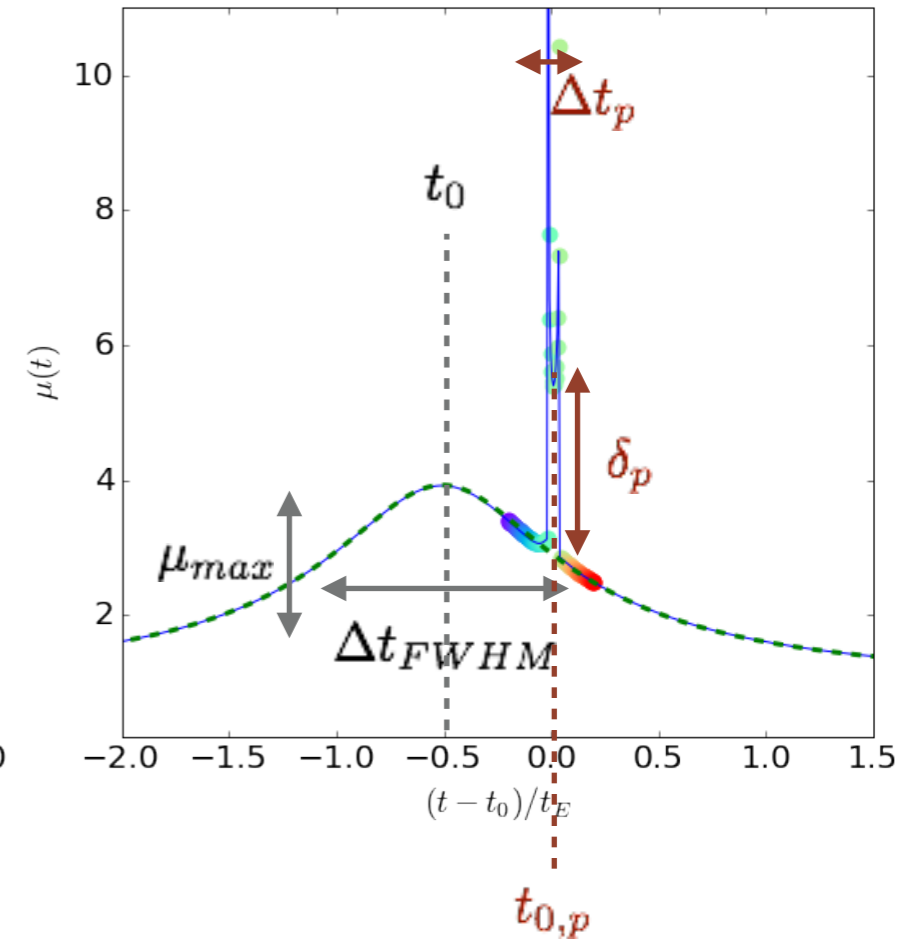
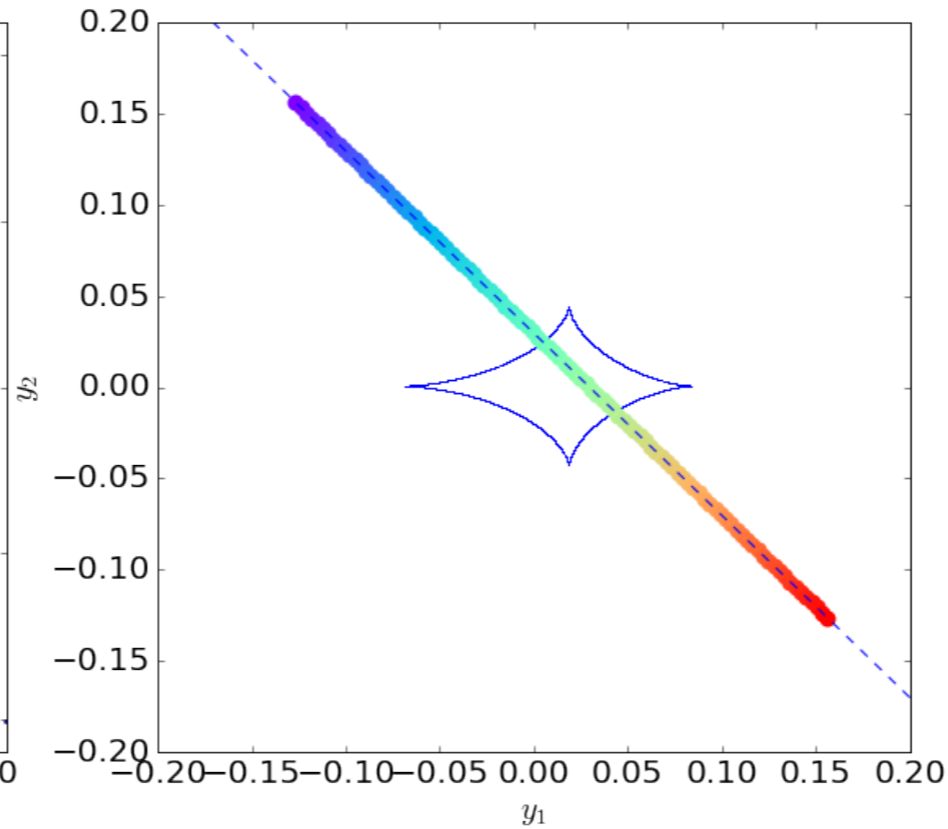
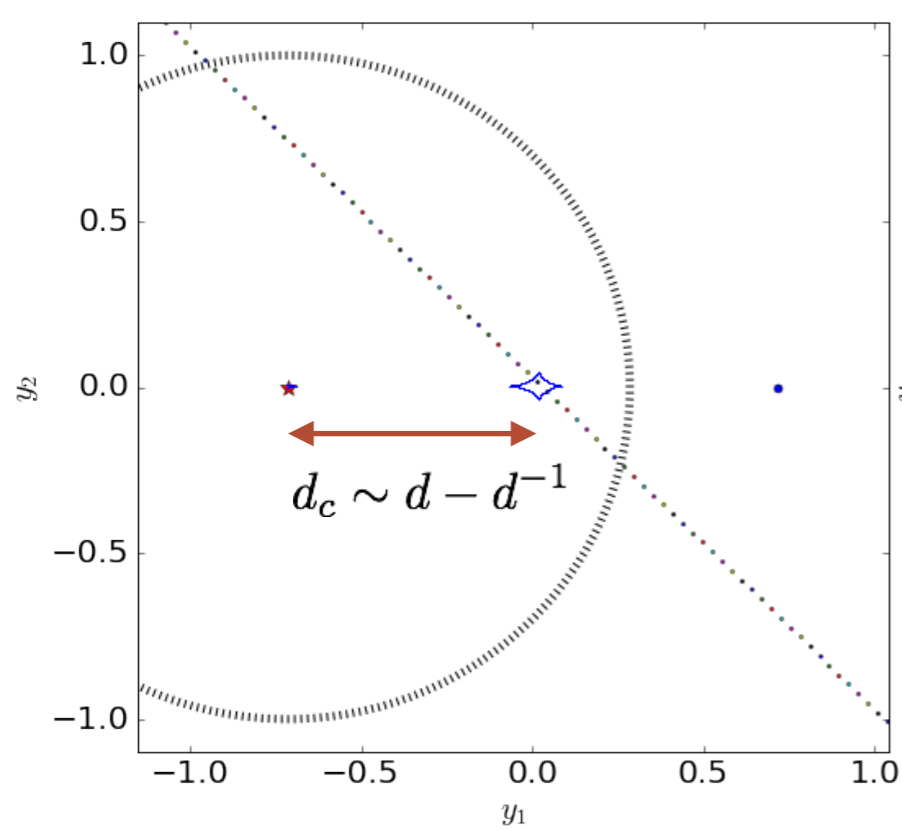
$$\Rightarrow y_0 \quad t_E$$

# PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



$$\Delta t_p \sim t_{E,p} \Rightarrow t_E \Rightarrow q = \left( \frac{t_{E,p}}{t_E} \right)^2$$

# PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES

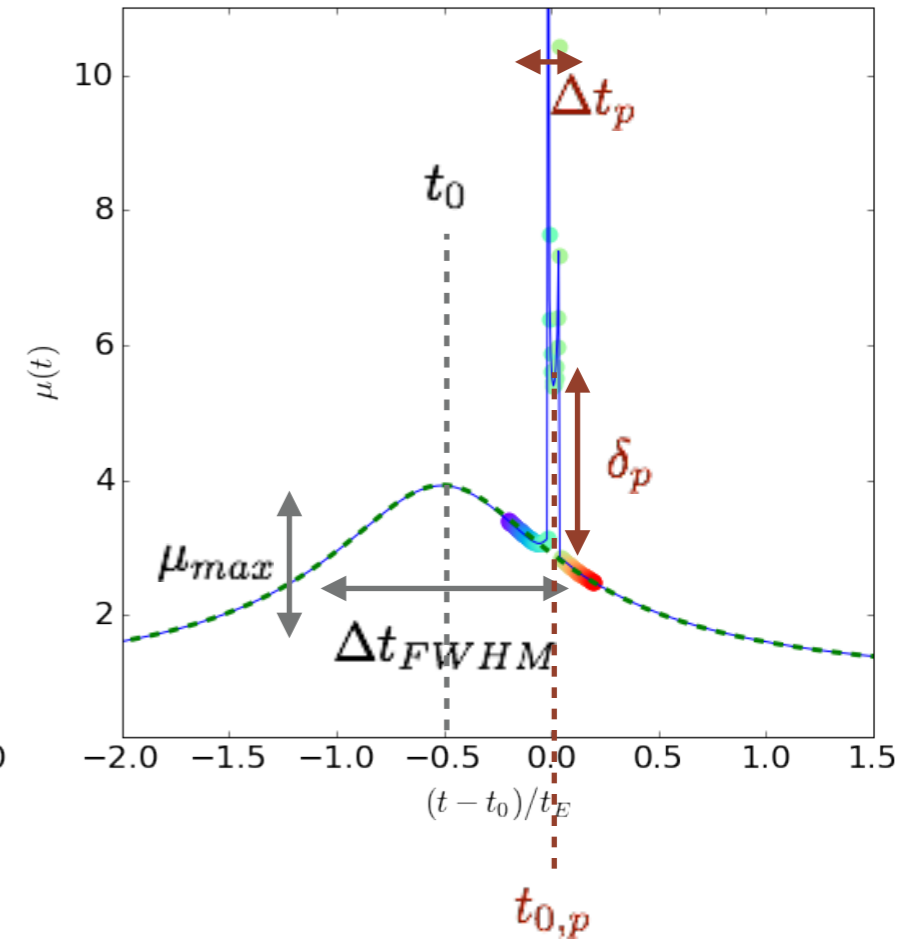
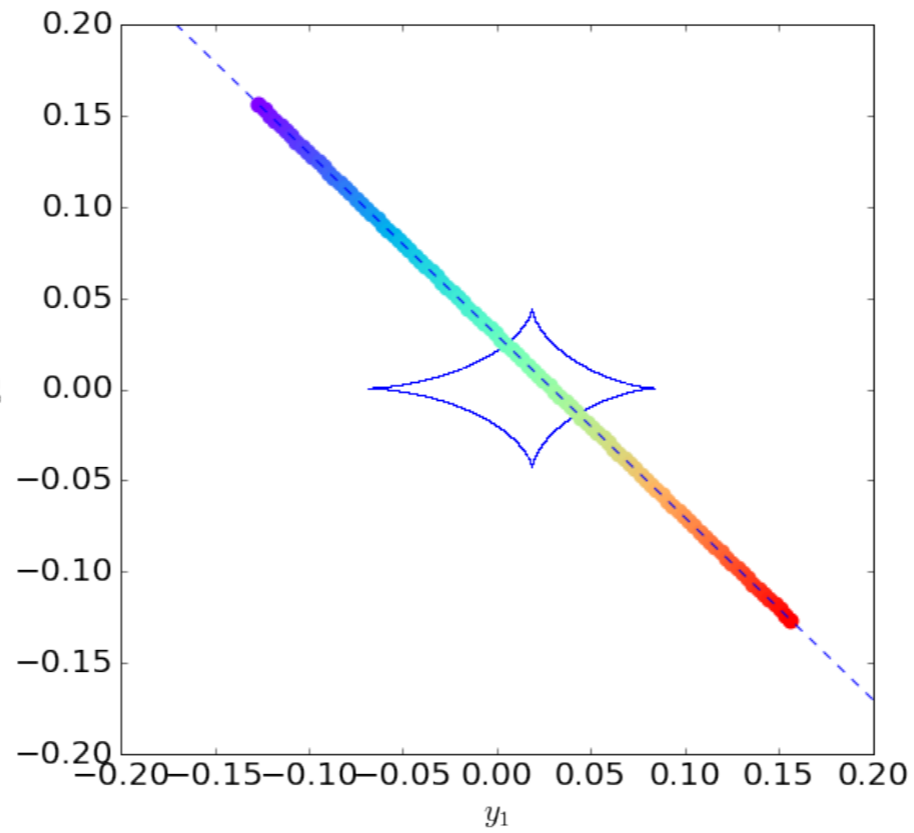
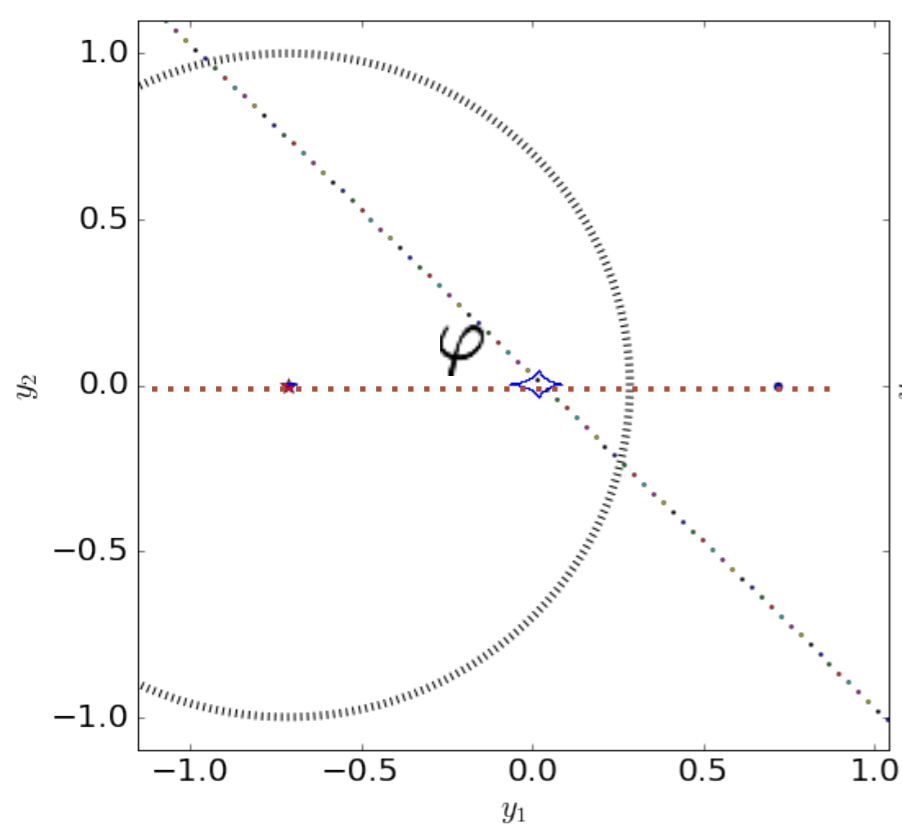


$$\delta_p, t_{0,p} \Rightarrow y_p = \sqrt{y_0^2 + \left(\frac{t_{0,p} - t_0}{t_E}\right)^2}$$

$$\Rightarrow d_c \sim \frac{y_p \pm \sqrt{y_p^2 + 4}}{2} \Rightarrow d$$

*up to the degeneracy in  $d$*

# PLANET PROPERTIES “READ OFF” OF THE LIGHT CURVES



$$y_0, y_p \Rightarrow \varphi = \sin^{-1} \frac{y_0}{y_p}$$

# ADVANTAGES OF USING MICROLENSING FOR PLANET SEARCHES

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- peak sensitivity beyond the snow line
- sensitivity to low-mass planets
- sensitivity to long period and free-floating planets
- sensitivity to a wide range of host stars over a wide range of galactocentric distances
- sensitivity to multiple planets